

Mathematica 11.3 Integration Test Results

Test results for the 653 problems in "4.1.1.2 (g cos)^p (a+b sin)^m.m"

Problem 8: Result more than twice size of optimal antiderivative.

$$\int \sec[c + dx] (a + a \sin[c + dx]) dx$$

Optimal (type 3, 17 leaves, 2 steps):

$$\frac{a \operatorname{Log}[1 - \sin[c + dx]]}{d}$$

Result (type 3, 83 leaves):

$$\frac{a \operatorname{Log}[\cos[c + dx]]}{d} - \frac{a \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] - \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d} + \frac{a \operatorname{Log}\left[\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right]}{d}$$

Problem 10: Result more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^3 (a + a \sin[c + dx]) dx$$

Optimal (type 3, 39 leaves, 4 steps):

$$\frac{a \operatorname{ArcTanh}[\sin[c + dx]]}{2d} + \frac{a^2}{2d(a - a \sin[c + dx])}$$

Result (type 3, 143 leaves):

$$\frac{a \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right]}{2d} + \frac{a \operatorname{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right]}{2d} + \frac{a \sec[c + dx]^2}{2d} + \frac{a}{4d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^2} - \frac{a}{4d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^2}$$

Problem 12: Result more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^5 (a + a \sin[c + dx]) dx$$

Optimal (type 3, 84 leaves, 4 steps):

$$\frac{3 a \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{8 d} + \frac{a^3}{8 d (a-a \operatorname{Sin}[c+d x])^2} + \frac{a^2}{4 d (a-a \operatorname{Sin}[c+d x])} - \frac{a^2}{8 d (a+a \operatorname{Sin}[c+d x])}$$

Result (type 3, 207 leaves):

$$-\frac{3 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{3 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{a \operatorname{Sec}[c+d x]^4}{4 d} + \frac{a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4} + \frac{3 a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} - \frac{a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4} - \frac{3 a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2}$$

Problem 20: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+d x]^2 (a+a \operatorname{Sin}[c+d x])^2 dx$$

Optimal (type 3, 38 leaves, 3 steps):

$$-a^2 x + \frac{2 a^4 \operatorname{Cos}[c+d x]}{d (a^2-a^2 \operatorname{Sin}[c+d x])}$$

Result (type 3, 101 leaves):

$$-\left(\left(a^2\left((c+d x) \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\left(4+c+d x\right) \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)\left(1+\operatorname{Sin}[c+d x]\right)^2\right) / \left(d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4\right)\right)$$

Problem 25: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+d x]^7 (a+a \operatorname{Sin}[c+d x])^2 dx$$

Optimal (type 3, 109 leaves, 4 steps):

$$\frac{a^2 \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{4 d} + \frac{a^5}{12 d (a-a \operatorname{Sin}[c+d x])^3} + \frac{a^4}{8 d (a-a \operatorname{Sin}[c+d x])^2} + \frac{3 a^3}{16 d (a-a \operatorname{Sin}[c+d x])} - \frac{a^3}{16 d (a+a \operatorname{Sin}[c+d x])}$$

Result (type 3, 290 leaves):

$$\left(\left(-3 - 12 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \right. \right. \\ \left. \left. 12 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \right. \right. \\ \left. \left. \frac{4 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^6} + \frac{6 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \right. \right. \\ \left. \left. \frac{9 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right) (a + a \sin [c + d x])^2 \right) / \\ \left(48 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 \right)$$

Problem 32: Result more than twice size of optimal antiderivative.

$$\int \cos [c + d x] (a + a \sin [c + d x])^3 dx$$

Optimal (type 3, 22 leaves, 2 steps):

$$\frac{(a + a \sin [c + d x])^4}{4 a d}$$

Result (type 3, 47 leaves):

$$\frac{1}{32 d} a^3 (-28 \cos [2 (c + d x)] + \cos [4 (c + d x)] + 56 \sin [c + d x] - 8 \sin [3 (c + d x)])$$

Problem 35: Result more than twice size of optimal antiderivative.

$$\int \sec [c + d x]^3 (a + a \sin [c + d x])^3 dx$$

Optimal (type 3, 40 leaves, 3 steps):

$$\frac{a^3 \operatorname{Log}[1 - \sin [c + d x]]}{d} + \frac{2 a^4}{d (a - a \sin [c + d x])}$$

Result (type 3, 92 leaves):

$$- \left(\left(2 a^3 \left(-1 - \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] + \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \right) \right. \right. \\ \left. \left. \sin [c + d x] \right) \right) / \left(d \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 \right)$$

Problem 41: Result more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^5 (a + a \sin [c + d x])^8 dx$$

Optimal (type 3, 67 leaves, 3 steps):

$$\frac{4 (a + a \sin[c + dx])^{11}}{11 a^3 d} - \frac{(a + a \sin[c + dx])^{12}}{3 a^4 d} + \frac{(a + a \sin[c + dx])^{13}}{13 a^5 d}$$

Result (type 3, 139 leaves):

$$-\frac{1}{1757184 d} a^8 (4434144 \cos[2(c + dx)] + 815100 \cos[4(c + dx)] - 354640 \cos[6(c + dx)] - 92664 \cos[8(c + dx)] + 20592 \cos[10(c + dx)] - 572 \cos[12(c + dx)] - 8314020 \sin[c + dx] + 877591 \sin[3(c + dx)] + 872157 \sin[5(c + dx)] + 6006 \sin[7(c + dx)] - 58630 \sin[9(c + dx)] + 4485 \sin[11(c + dx)] - 33 \sin[13(c + dx)])$$

Problem 43: Result more than twice size of optimal antiderivative.

$$\int \cos[c + dx]^3 (a + a \sin[c + dx])^8 dx$$

Optimal (type 3, 45 leaves, 3 steps):

$$\frac{(a + a \sin[c + dx])^{10}}{5 a^2 d} - \frac{(a + a \sin[c + dx])^{11}}{11 a^3 d}$$

Result (type 3, 109 leaves):

$$\frac{1}{56320 d} a^8 (-284240 \cos[2(c + dx)] + 25080 \cos[6(c + dx)] - 3520 \cos[8(c + dx)] + 88 \cos[10(c + dx)] + 461890 \sin[c + dx] - 106590 \sin[3(c + dx)] - 31977 \sin[5(c + dx)] + 11495 \sin[7(c + dx)] - 715 \sin[9(c + dx)] + 5 \sin[11(c + dx)])$$

Problem 45: Result more than twice size of optimal antiderivative.

$$\int \cos[c + dx] (a + a \sin[c + dx])^8 dx$$

Optimal (type 3, 22 leaves, 2 steps):

$$\frac{(a + a \sin[c + dx])^9}{9 a d}$$

Result (type 3, 97 leaves):

$$\frac{1}{2304 d} a^8 (-31824 \cos[2(c + dx)] + 8568 \cos[4(c + dx)] - 816 \cos[6(c + dx)] + 18 \cos[8(c + dx)] + 43758 \sin[c + dx] - 18564 \sin[3(c + dx)] + 3060 \sin[5(c + dx)] - 153 \sin[7(c + dx)] + \sin[9(c + dx)])$$

Problem 49: Result more than twice size of optimal antiderivative.

$$\int \sec [c+d x]^4 (a+a \sin [c+d x])^8 d x$$

Optimal (type 3, 179 leaves, 8 steps):

$$\frac{1155 a^8 x}{8} - \frac{385 a^8 \cos [c+d x]^3}{4 d} + \frac{1155 a^8 \cos [c+d x] \sin [c+d x]}{8 d} + \frac{2 a^{15} \cos [c+d x]^{11}}{3 d (a-a \sin [c+d x])^7} - \frac{22 a^{13} \cos [c+d x]^9}{3 d (a-a \sin [c+d x])^5} - \frac{66 a^{14} \cos [c+d x]^7}{d (a^2-a^2 \sin [c+d x])^3} - \frac{231 a^{16} \cos [c+d x]^5}{4 d (a^8-a^8 \sin [c+d x])}$$

Result (type 3, 465 leaves):

$$\frac{1155 (c+d x) (a+a \sin [c+d x])^8}{8 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^{16}} - \frac{78 \cos [c+d x] (a+a \sin [c+d x])^8}{d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^{16}} + \frac{2 \cos [3(c+d x)] (a+a \sin [c+d x])^8}{3 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^{16}} + \left(64 (a+a \sin [c+d x])^8\right) / \left(3 d \left(\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right)^2 \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^{16}\right) + \left(128 \sin \left[\frac{1}{2}(c+d x)\right] (a+a \sin [c+d x])^8\right) / \left(3 d \left(\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right)^3 \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^{16}\right) - \left(1024 \sin \left[\frac{1}{2}(c+d x)\right] (a+a \sin [c+d x])^8\right) / \left(3 d \left(\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right) \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^{16}\right) - \frac{31 (a+a \sin [c+d x])^8 \sin [2(c+d x)]}{4 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^{16}} + \frac{(a+a \sin [c+d x])^8 \sin [4(c+d x)]}{32 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^{16}}$$

Problem 50: Result more than twice size of optimal antiderivative.

$$\int \sec [c+d x]^5 (a+a \sin [c+d x])^8 d x$$

Optimal (type 3, 110 leaves, 3 steps):

$$-\frac{80 a^8 \operatorname{Log}[1-\sin [c+d x]]}{d} - \frac{31 a^8 \sin [c+d x]}{d} - \frac{4 a^8 \sin [c+d x]^2}{d} - \frac{a^8 \sin [c+d x]^3}{3 d} + \frac{16 a^{10}}{d (a-a \sin [c+d x])^2} - \frac{80 a^9}{d (a-a \sin [c+d x])}$$

Result (type 3, 341 leaves):

$$\frac{2 \operatorname{Cos}\left[2(c+dx)\right] (a+a \operatorname{Sin}[c+dx])^8}{d\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^{16}} - \frac{160 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right] (a+a \operatorname{Sin}[c+dx])^8}{d\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^{16}} + \left(16(a+a \operatorname{Sin}[c+dx])^8\right) / \left(d\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^4\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^{16}\right) - \left(80(a+a \operatorname{Sin}[c+dx])^8\right) / \left(d\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^2\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^{16}\right) - \frac{125 \operatorname{Sin}[c+dx] (a+a \operatorname{Sin}[c+dx])^8}{4 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^{16}} + \frac{(a+a \operatorname{Sin}[c+dx])^8 \operatorname{Sin}[3(c+dx)]}{12 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^{16}}$$

Problem 57: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[c+dx]}{a+a \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 37 leaves, 4 steps):

$$\frac{\operatorname{ArcTanh}[\operatorname{Sin}[c+dx]]}{2 a d} - \frac{1}{2 d(a+a \operatorname{Sin}[c+dx])}$$

Result (type 3, 126 leaves):

$$\left(-1-\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]+\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]\right) + \left(-\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]+\operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right]\right) \operatorname{Sin}[c+dx] / (2 a d(1+\operatorname{Sin}[c+dx]))$$

Problem 58: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[c+dx]^2}{a+a \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 42 leaves, 3 steps):

$$-\frac{\operatorname{Sec}[c+dx]}{3 d(a+a \operatorname{Sin}[c+dx])} + \frac{2 \operatorname{Tan}[c+dx]}{3 a d}$$

Result (type 3, 103 leaves):

$$\begin{aligned} & (2 \operatorname{Cos}[c+d x]-4 \operatorname{Cos}[2(c+d x)]+8 \operatorname{Sin}[c+d x]+\operatorname{Sin}[2(c+d x)]) / \\ & \left(12 a d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)\right. \\ & \left.\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)\left(1+\operatorname{Sin}[c+d x]\right)\right) \end{aligned}$$

Problem 59: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[c+d x]^3}{a+a \operatorname{Sin}[c+d x]} dx$$

Optimal (type 3, 77 leaves, 4 steps):

$$\frac{3 \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{8 a d} + \frac{1}{8 d(a-a \operatorname{Sin}[c+d x])} - \frac{a}{8 d(a+a \operatorname{Sin}[c+d x])^2} - \frac{1}{4 d(a+a \operatorname{Sin}[c+d x])}$$

Result (type 3, 190 leaves):

$$\begin{aligned} & - \left(\left(2 + \frac{1}{\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} + \right. \right. \\ & 3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2 - \\ & 3 \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2 - \\ & \left. \frac{\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2}{\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} \right) / (8 d(a+a \operatorname{Sin}[c+d x])) \end{aligned}$$

Problem 61: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[c+d x]^5}{a+a \operatorname{Sin}[c+d x]} dx$$

Optimal (type 3, 120 leaves, 4 steps):

$$\begin{aligned} & \frac{5 \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{16 a d} + \frac{a}{32 d(a-a \operatorname{Sin}[c+d x])^2} + \frac{1}{8 d(a-a \operatorname{Sin}[c+d x])} - \\ & \frac{a^2}{24 d(a+a \operatorname{Sin}[c+d x])^3} - \frac{3 a}{32 d(a+a \operatorname{Sin}[c+d x])^2} - \frac{3}{16 d(a+a \operatorname{Sin}[c+d x])} \end{aligned}$$

Result (type 3, 267 leaves):

$$\frac{1}{96 d (a + a \sin [c + d x])} \left(-18 - \frac{4}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} - \frac{9}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} - 30 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + 30 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \frac{3 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4} + \frac{12 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)$$

Problem 68: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c + d x]^2}{(a + a \sin [c + d x])^2} dx$$

Optimal (type 3, 34 leaves, 2 steps):

$$-\frac{x}{a^2} - \frac{2 \cos [c + d x]}{d (a^2 + a^2 \sin [c + d x])}$$

Result (type 3, 75 leaves):

$$-\left(\left(\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) \right)^3 \left((c + d x) \cos \left[\frac{1}{2} (c + d x) \right] + (-4 + c + d x) \sin \left[\frac{1}{2} (c + d x) \right] \right) / \left(a^2 d (1 + \sin [c + d x])^2 \right) \right)$$

Problem 70: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x]}{(a + a \sin [c + d x])^2} dx$$

Optimal (type 3, 60 leaves, 4 steps):

$$\frac{\text{ArcTanh}[\sin [c + d x]]}{4 a^2 d} - \frac{1}{4 d (a + a \sin [c + d x])^2} - \frac{1}{4 d (a^2 + a^2 \sin [c + d x])}$$

Result (type 3, 139 leaves):

$$\begin{aligned}
 & - \left(\left(1 + \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \right. \right. \\
 & \quad \left. \left. \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 - \right. \right. \\
 & \quad \left. \left. \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 \right) / \left(4 \right. \\
 & \quad \left. d (a + a \sin [c + d x])^2 \right)
 \end{aligned}$$

Problem 72: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec [c + d x]^3}{(a + a \sin [c + d x])^2} dx$$

Optimal (type 3, 104 leaves, 4 steps):

$$\frac{\operatorname{ArcTanh}[\sin [c + d x]]}{4 a^2 d} - \frac{a}{12 d (a + a \sin [c + d x])^3} - \frac{1}{8 d (a + a \sin [c + d x])^2} + \frac{1}{16 d (a^2 - a^2 \sin [c + d x])} - \frac{3}{16 d (a^2 + a^2 \sin [c + d x])}$$

Result (type 3, 217 leaves):

$$\begin{aligned}
 & - \left(\left(6 + \frac{4}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} + 9 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \right. \right. \\
 & \quad 12 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 - \\
 & \quad 12 \log \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 - \\
 & \quad \left. \frac{3 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right) / \left(48 d (a + a \sin [c + d x])^2 \right)
 \end{aligned}$$

Problem 76: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c + d x]^7}{(a + a \sin [c + d x])^3} dx$$

Optimal (type 3, 23 leaves, 2 steps):

$$- \frac{(a - a \sin [c + d x])^4}{4 a^7 d}$$

Result (type 3, 48 leaves):

$$- \frac{1}{32 a^3 d} \left(-28 \cos [2 (c + d x)] + \cos [4 (c + d x)] + 8 (-7 \sin [c + d x] + \sin [3 (c + d x)]) \right)$$

Problem 80: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + dx]^3}{(a + a \sin[c + dx])^3} dx$$

Optimal (type 3, 39 leaves, 3 steps):

$$-\frac{\text{Log}[1 + \sin[c + dx]]}{a^3 d} - \frac{2}{d (a^3 + a^3 \sin[c + dx])}$$

Result (type 3, 89 leaves):

$$\left(2 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4 \right. \\ \left. \left(-1 - \text{Log}\left[\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right] \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^2 \right) \right) / \left(d (a + a \sin[c + dx])^3 \right)$$

Problem 81: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c + dx]^2}{(a + a \sin[c + dx])^3} dx$$

Optimal (type 3, 27 leaves, 1 step):

$$-\frac{\cos[c + dx]^3}{3 d (a + a \sin[c + dx])^3}$$

Result (type 3, 66 leaves):

$$\left(\left(-3 \cos\left[\frac{1}{2}(c + dx)\right] + \cos\left[\frac{3}{2}(c + dx)\right] \right) \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^3 \right) / \left(3 a^3 d (1 + \sin[c + dx])^3 \right)$$

Problem 83: Result more than twice size of optimal antiderivative.

$$\int \frac{\sec[c + dx]}{(a + a \sin[c + dx])^3} dx$$

Optimal (type 3, 82 leaves, 4 steps):

$$\frac{\text{ArcTanh}[\sin[c + dx]]}{8 a^3 d} - \frac{1}{6 d (a + a \sin[c + dx])^3} - \\ \frac{1}{8 a d (a + a \sin[c + dx])^2} - \frac{1}{8 d (a^3 + a^3 \sin[c + dx])}$$

Result (type 3, 167 leaves):

$$\begin{aligned}
 & - \left(\left(4 + 3 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) \right)^2 + 3 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) \right)^4 + \\
 & \quad 3 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 - \\
 & \quad 3 \operatorname{Log} \left[\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 \Big/ \\
 & \quad \left(24 d (a + a \sin [c + d x])^3 \right)
 \end{aligned}$$

Problem 88: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c + d x]^8}{(a + a \sin [c + d x])^8} dx$$

Optimal (type 3, 127 leaves, 5 steps):

$$\begin{aligned}
 & \frac{x}{a^8} - \frac{2 \cos [c + d x]^7}{7 a d (a + a \sin [c + d x])^7} + \frac{2 \cos [c + d x]^5}{5 a^3 d (a + a \sin [c + d x])^5} - \\
 & \frac{2 \cos [c + d x]^3}{3 a^2 d (a^2 + a^2 \sin [c + d x])^3} + \frac{2 \cos [c + d x]}{d (a^8 + a^8 \sin [c + d x])}
 \end{aligned}$$

Result (type 3, 263 leaves):

$$\begin{aligned}
 & \frac{1}{105 d (a + a \sin [c + d x])^8} \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^9 \\
 & \quad \left(480 \sin \left[\frac{1}{2} (c + d x) \right] - 240 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) - \right. \\
 & \quad \quad 1056 \sin \left[\frac{1}{2} (c + d x) \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \\
 & \quad \quad 528 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 + 976 \sin \left[\frac{1}{2} (c + d x) \right] \\
 & \quad \quad \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 - 488 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^5 - \\
 & \quad \quad 704 \sin \left[\frac{1}{2} (c + d x) \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^6 + \\
 & \quad \quad \left. 105 (c + d x) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^7 \right)
 \end{aligned}$$

Problem 90: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c + d x]^6}{(a + a \sin [c + d x])^8} dx$$

Optimal (type 3, 58 leaves, 2 steps):

$$- \frac{\cos [c + d x]^7}{9 d (a + a \sin [c + d x])^8} - \frac{\cos [c + d x]^7}{63 a d (a + a \sin [c + d x])^7}$$

Result (type 3, 128 leaves):

$$- \left(\left(315 \operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - 189 \operatorname{Cos} \left[\frac{3}{2} (c + d x) \right] - 63 \operatorname{Cos} \left[\frac{5}{2} (c + d x) \right] + 9 \operatorname{Cos} \left[\frac{7}{2} (c + d x) \right] - 189 \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] - 105 \operatorname{Sin} \left[\frac{3}{2} (c + d x) \right] + 27 \operatorname{Sin} \left[\frac{5}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{9}{2} (c + d x) \right] \right) / \left(504 a^8 d \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^9 \right)$$

Problem 101: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c + d x]^7 \sqrt{a + a \operatorname{Sin}[c + d x]} dx$$

Optimal (type 3, 97 leaves, 3 steps):

$$\frac{16 (a + a \operatorname{Sin}[c + d x])^{9/2}}{9 a^4 d} - \frac{24 (a + a \operatorname{Sin}[c + d x])^{11/2}}{11 a^5 d} + \frac{12 (a + a \operatorname{Sin}[c + d x])^{13/2}}{13 a^6 d} - \frac{2 (a + a \operatorname{Sin}[c + d x])^{15/2}}{15 a^7 d}$$

Result (type 3, 1137 leaves):

$$\frac{35 \operatorname{Cos} \left[\frac{d x}{2} \right] \left(\operatorname{Cos} \left[\frac{c}{2} \right] + \operatorname{Sin} \left[\frac{c}{2} \right] \right) \sqrt{a (1 + \operatorname{Sin}[c + d x])}}{64 d \left(\operatorname{Cos} \left[\frac{c}{2} + \frac{d x}{2} \right] + \operatorname{Sin} \left[\frac{c}{2} + \frac{d x}{2} \right] \right)} - \frac{35 \operatorname{Cos} \left[\frac{3 d x}{2} \right] \left(\operatorname{Cos} \left[\frac{3 c}{2} \right] - \operatorname{Sin} \left[\frac{3 c}{2} \right] \right) \sqrt{a (1 + \operatorname{Sin}[c + d x])}}{192 d \left(\operatorname{Cos} \left[\frac{c}{2} + \frac{d x}{2} \right] + \operatorname{Sin} \left[\frac{c}{2} + \frac{d x}{2} \right] \right)} + \frac{21 \operatorname{Cos} \left[\frac{5 d x}{2} \right] \left(\operatorname{Cos} \left[\frac{5 c}{2} \right] + \operatorname{Sin} \left[\frac{5 c}{2} \right] \right) \sqrt{a (1 + \operatorname{Sin}[c + d x])}}{320 d \left(\operatorname{Cos} \left[\frac{c}{2} + \frac{d x}{2} \right] + \operatorname{Sin} \left[\frac{c}{2} + \frac{d x}{2} \right] \right)} - \frac{3 \operatorname{Cos} \left[\frac{7 d x}{2} \right] \left(\operatorname{Cos} \left[\frac{7 c}{2} \right] - \operatorname{Sin} \left[\frac{7 c}{2} \right] \right) \sqrt{a (1 + \operatorname{Sin}[c + d x])}}{64 d \left(\operatorname{Cos} \left[\frac{c}{2} + \frac{d x}{2} \right] + \operatorname{Sin} \left[\frac{c}{2} + \frac{d x}{2} \right] \right)} + \frac{7 \operatorname{Cos} \left[\frac{9 d x}{2} \right] \left(\operatorname{Cos} \left[\frac{9 c}{2} \right] + \operatorname{Sin} \left[\frac{9 c}{2} \right] \right) \sqrt{a (1 + \operatorname{Sin}[c + d x])}}{576 d \left(\operatorname{Cos} \left[\frac{c}{2} + \frac{d x}{2} \right] + \operatorname{Sin} \left[\frac{c}{2} + \frac{d x}{2} \right] \right)} - \frac{7 \operatorname{Cos} \left[\frac{11 d x}{2} \right] \left(\operatorname{Cos} \left[\frac{11 c}{2} \right] - \operatorname{Sin} \left[\frac{11 c}{2} \right] \right) \sqrt{a (1 + \operatorname{Sin}[c + d x])}}{704 d \left(\operatorname{Cos} \left[\frac{c}{2} + \frac{d x}{2} \right] + \operatorname{Sin} \left[\frac{c}{2} + \frac{d x}{2} \right] \right)} + \frac{\operatorname{Cos} \left[\frac{13 d x}{2} \right] \left(\operatorname{Cos} \left[\frac{13 c}{2} \right] + \operatorname{Sin} \left[\frac{13 c}{2} \right] \right) \sqrt{a (1 + \operatorname{Sin}[c + d x])}}{832 d \left(\operatorname{Cos} \left[\frac{c}{2} + \frac{d x}{2} \right] + \operatorname{Sin} \left[\frac{c}{2} + \frac{d x}{2} \right] \right)}$$

$$\begin{aligned}
 & \frac{\cos\left[\frac{15dx}{2}\right] \left(\cos\left[\frac{15c}{2}\right] - \sin\left[\frac{15c}{2}\right]\right) \sqrt{a(1 + \sin[c + dx])}}{960d \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{35 \left(\cos\left[\frac{c}{2}\right] - \sin\left[\frac{c}{2}\right]\right) \sin\left[\frac{dx}{2}\right] \sqrt{a(1 + \sin[c + dx])}}{64d \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{35 \left(\cos\left[\frac{3c}{2}\right] + \sin\left[\frac{3c}{2}\right]\right) \sin\left[\frac{3dx}{2}\right] \sqrt{a(1 + \sin[c + dx])}}{192d \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{21 \left(\cos\left[\frac{5c}{2}\right] - \sin\left[\frac{5c}{2}\right]\right) \sin\left[\frac{5dx}{2}\right] \sqrt{a(1 + \sin[c + dx])}}{320d \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{3 \left(\cos\left[\frac{7c}{2}\right] + \sin\left[\frac{7c}{2}\right]\right) \sin\left[\frac{7dx}{2}\right] \sqrt{a(1 + \sin[c + dx])}}{64d \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{7 \left(\cos\left[\frac{9c}{2}\right] - \sin\left[\frac{9c}{2}\right]\right) \sin\left[\frac{9dx}{2}\right] \sqrt{a(1 + \sin[c + dx])}}{576d \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{7 \left(\cos\left[\frac{11c}{2}\right] + \sin\left[\frac{11c}{2}\right]\right) \sin\left[\frac{11dx}{2}\right] \sqrt{a(1 + \sin[c + dx])}}{704d \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{\left(\cos\left[\frac{13c}{2}\right] - \sin\left[\frac{13c}{2}\right]\right) \sin\left[\frac{13dx}{2}\right] \sqrt{a(1 + \sin[c + dx])}}{832d \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{\left(\cos\left[\frac{15c}{2}\right] + \sin\left[\frac{15c}{2}\right]\right) \sin\left[\frac{15dx}{2}\right] \sqrt{a(1 + \sin[c + dx])}}{960d \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)}
 \end{aligned}$$

Problem 102: Result more than twice size of optimal antiderivative.

$$\int \cos[c + dx]^6 \sqrt{a + a \sin[c + dx]} dx$$

Optimal (type 3, 127 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{256 a^4 \cos[c + dx]^7}{3003 d (a + a \sin[c + dx])^{7/2}} - \frac{64 a^3 \cos[c + dx]^7}{429 d (a + a \sin[c + dx])^{5/2}} - \\
 & \frac{24 a^2 \cos[c + dx]^7}{143 d (a + a \sin[c + dx])^{3/2}} - \frac{2 a \cos[c + dx]^7}{13 d \sqrt{a + a \sin[c + dx]}}
 \end{aligned}$$

Result (type 3, 995 leaves):

$$\begin{aligned}
 & - \frac{5 \operatorname{Cos}\left[\frac{dx}{2}\right] \left(\operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right]\right) \sqrt{a(1 + \operatorname{Sin}[c + dx])}}{8 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{5 \operatorname{Cos}\left[\frac{3dx}{2}\right] \left(\operatorname{Cos}\left[\frac{3c}{2}\right] + \operatorname{Sin}\left[\frac{3c}{2}\right]\right) \sqrt{a(1 + \operatorname{Sin}[c + dx])}}{32 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} - \\
 & \frac{3 \operatorname{Cos}\left[\frac{5dx}{2}\right] \left(\operatorname{Cos}\left[\frac{5c}{2}\right] - \operatorname{Sin}\left[\frac{5c}{2}\right]\right) \sqrt{a(1 + \operatorname{Sin}[c + dx])}}{32 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{3 \operatorname{Cos}\left[\frac{7dx}{2}\right] \left(\operatorname{Cos}\left[\frac{7c}{2}\right] + \operatorname{Sin}\left[\frac{7c}{2}\right]\right) \sqrt{a(1 + \operatorname{Sin}[c + dx])}}{112 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} - \\
 & \frac{\operatorname{Cos}\left[\frac{9dx}{2}\right] \left(\operatorname{Cos}\left[\frac{9c}{2}\right] - \operatorname{Sin}\left[\frac{9c}{2}\right]\right) \sqrt{a(1 + \operatorname{Sin}[c + dx])}}{48 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{\operatorname{Cos}\left[\frac{11dx}{2}\right] \left(\operatorname{Cos}\left[\frac{11c}{2}\right] + \operatorname{Sin}\left[\frac{11c}{2}\right]\right) \sqrt{a(1 + \operatorname{Sin}[c + dx])}}{352 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} - \\
 & \frac{\operatorname{Cos}\left[\frac{13dx}{2}\right] \left(\operatorname{Cos}\left[\frac{13c}{2}\right] - \operatorname{Sin}\left[\frac{13c}{2}\right]\right) \sqrt{a(1 + \operatorname{Sin}[c + dx])}}{416 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{5 \left(\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]\right) \operatorname{Sin}\left[\frac{dx}{2}\right] \sqrt{a(1 + \operatorname{Sin}[c + dx])}}{8 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{5 \left(\operatorname{Cos}\left[\frac{3c}{2}\right] - \operatorname{Sin}\left[\frac{3c}{2}\right]\right) \operatorname{Sin}\left[\frac{3dx}{2}\right] \sqrt{a(1 + \operatorname{Sin}[c + dx])}}{32 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{3 \left(\operatorname{Cos}\left[\frac{5c}{2}\right] + \operatorname{Sin}\left[\frac{5c}{2}\right]\right) \operatorname{Sin}\left[\frac{5dx}{2}\right] \sqrt{a(1 + \operatorname{Sin}[c + dx])}}{32 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{3 \left(\operatorname{Cos}\left[\frac{7c}{2}\right] - \operatorname{Sin}\left[\frac{7c}{2}\right]\right) \operatorname{Sin}\left[\frac{7dx}{2}\right] \sqrt{a(1 + \operatorname{Sin}[c + dx])}}{112 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{\left(\operatorname{Cos}\left[\frac{9c}{2}\right] + \operatorname{Sin}\left[\frac{9c}{2}\right]\right) \operatorname{Sin}\left[\frac{9dx}{2}\right] \sqrt{a(1 + \operatorname{Sin}[c + dx])}}{48 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} + \\
 & \frac{\left(\operatorname{Cos}\left[\frac{11c}{2}\right] - \operatorname{Sin}\left[\frac{11c}{2}\right]\right) \operatorname{Sin}\left[\frac{11dx}{2}\right] \sqrt{a(1 + \operatorname{Sin}[c + dx])}}{352 d \left(\operatorname{Cos}\left[\frac{c}{2} + \frac{dx}{2}\right] + \operatorname{Sin}\left[\frac{c}{2} + \frac{dx}{2}\right]\right)} +
 \end{aligned}$$

$$\frac{\left(\cos\left[\frac{13c}{2}\right] + \sin\left[\frac{13c}{2}\right]\right) \sin\left[\frac{13dx}{2}\right] \sqrt{a(1 + \sin[c + dx])}}{416d \left(\cos\left[\frac{c}{2} + \frac{dx}{2}\right] + \sin\left[\frac{c}{2} + \frac{dx}{2}\right]\right)}$$

Problem 108: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \sec[c + dx] \sqrt{a + a \sin[c + dx]} dx$$

Optimal (type 3, 40 leaves, 3 steps):

$$\frac{\sqrt{2} \sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin[c+dx]}}{\sqrt{2} \sqrt{a}}\right]}{d}$$

Result (type 3, 95 leaves):

$$-\left(\left((2 - 2i) (-1)^{1/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \sec\left[\frac{dx}{4}\right] \left(\cos\left[\frac{1}{4}(2c + dx)\right] + \sin\left[\frac{1}{4}(2c + dx)\right]\right)\right] \sqrt{a(1 + \sin[c + dx])}\right) / \left(d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)\right)\right)$$

Problem 109: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec[c + dx]^2 \sqrt{a + a \sin[c + dx]} dx$$

Optimal (type 3, 72 leaves, 3 steps):

$$-\frac{\sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{2} \sqrt{a+a \sin[c+dx]}}\right]}{\sqrt{2} d} + \frac{\sec[c + dx] \sqrt{a + a \sin[c + dx]}}{d}$$

Result (type 3, 106 leaves):

$$\frac{1}{d} \sec[c + dx] \left(1 - (1 + i) (-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \sec\left[\frac{dx}{4}\right] \left(\cos\left[\frac{1}{4}(2c + dx)\right] - \sin\left[\frac{1}{4}(2c + dx)\right]\right)\right] \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)\right) \sqrt{a(1 + \sin[c + dx])}$$

Problem 110: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^3 \sqrt{a + a \sin[c + dx]} dx$$

Optimal (type 3, 95 leaves, 5 steps):

$$\frac{3 \sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin [c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{4 \sqrt{2} d}-\frac{3 a}{4 d \sqrt{a+a \sin [c+d x]}}+\frac{\operatorname{Sec}[c+d x]^2 \sqrt{a+a \sin [c+d x]}}{2 d}$$

Result (type 3, 271 leaves):

$$\left(\left(-2-(3-3 i)(-1)^{1 / 4} \operatorname{ArcTanh}\left[\frac{1}{2}+\frac{i}{2}\right](-1)^{3 / 4} \operatorname{Sec}\left[\frac{d x}{4}\right]\right.\right. \\ \left.\left.\left(\cos\left[\frac{1}{4}(2 c+d x)\right]+\sin\left[\frac{1}{4}(2 c+d x)\right]\right)\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)\right)+\right. \\ \left.\frac{2 \sin\left[\frac{d x}{2}\right]\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)}{\left(\cos\left[\frac{c}{2}\right]-\sin\left[\frac{c}{2}\right]\right)\left(\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)^2}+\right. \\ \left.\frac{\left(\cos\left[\frac{c}{2}\right]+\sin\left[\frac{c}{2}\right]\right)\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)}{\left(\cos\left[\frac{c}{2}\right]-\sin\left[\frac{c}{2}\right]\right)\left(\cos\left[\frac{1}{2}(c+d x)\right]-\sin\left[\frac{1}{2}(c+d x)\right]\right)}\right) \\ \left.\sqrt{a(1+\sin [c+d x])}\right) / \left(4 d\left(\cos\left[\frac{1}{2}(c+d x)\right]+\sin\left[\frac{1}{2}(c+d x)\right]\right)^2\right)$$

Problem 111: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+d x]^4 \sqrt{a+a \sin [c+d x]} d x$$

Optimal (type 3, 137 leaves, 5 steps):

$$-\frac{5 \sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}}\right]}{8 \sqrt{2} d}-\frac{5 a^2 \cos [c+d x]}{8 d(a+a \sin [c+d x])^{3 / 2}}+ \\ \frac{5 a \operatorname{Sec}[c+d x]}{6 d \sqrt{a+a \sin [c+d x]}}+\frac{\operatorname{Sec}[c+d x]^3 \sqrt{a+a \sin [c+d x]}}{3 d}$$

Result (type 3, 302 leaves):

$$\left(\left(\frac{6 \operatorname{Sin}\left[\frac{dx}{2}\right]}{\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]} - \frac{3 \left(\operatorname{Cos}\left[\frac{c}{2}\right] - \operatorname{Sin}\left[\frac{c}{2}\right] \right) \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)}{\operatorname{Cos}\left[\frac{c}{2}\right] + \operatorname{Sin}\left[\frac{c}{2}\right]} - (15 + 15i) \right. \right. \\ \left. \left. (-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \operatorname{Sec}\left[\frac{dx}{4}\right] \left(\operatorname{Cos}\left[\frac{1}{4}(2c+dx)\right] - \operatorname{Sin}\left[\frac{1}{4}(2c+dx)\right] \right)\right] \right) \right. \\ \left. \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2 + \frac{4 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2}{\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^3} + \right. \\ \left. \frac{12 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^2}{\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]} \right) \sqrt{a(1 + \operatorname{Sin}[c+dx])} \Bigg/ \\ \left(24d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^3 \right)$$

Problem 112: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Sec}[c+dx]^5 \sqrt{a+a \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 149 leaves, 7 steps):

$$\frac{35 \sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \operatorname{Sin}[c+dx]}}{\sqrt{2} \sqrt{a}}\right]}{64 \sqrt{2} d} - \frac{35 a^2}{96 d (a+a \operatorname{Sin}[c+dx])^{3/2}} - \\ \frac{35 a}{64 d \sqrt{a+a \operatorname{Sin}[c+dx]}} + \frac{7 a \operatorname{Sec}[c+dx]^2}{16 d \sqrt{a+a \operatorname{Sin}[c+dx]}} + \frac{\operatorname{Sec}[c+dx]^4 \sqrt{a+a \operatorname{Sin}[c+dx]}}{4 d}$$

Result (type 3, 179 leaves):

$$\left(\sqrt{a(1 + \operatorname{Sin}[c+dx])} \left((-420 + 420i) (-1)^{1/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \operatorname{Sec}\left[\frac{dx}{4}\right] \right. \right. \right. \\ \left. \left. \left(\operatorname{Cos}\left[\frac{1}{4}(2c+dx)\right] + \operatorname{Sin}\left[\frac{1}{4}(2c+dx)\right] \right)\right] \right) \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^3 + \\ (-102 - 70 \operatorname{Cos}[2(c+dx)] + 329 \operatorname{Sin}[c+dx] + 105 \operatorname{Sin}[3(c+dx)]) \Bigg/ \\ \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4 \Bigg) \Bigg/ \\ \left(768d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^4 \right)$$

Problem 113: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Sec}[c+dx]^6 \sqrt{a+a \operatorname{Sin}[c+dx]} dx$$

Optimal (type 3, 197 leaves, 7 steps):

$$\begin{aligned}
& - \frac{63 \sqrt{a} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{2} \sqrt{a+a \sin[c+dx]}}\right]}{128 \sqrt{2} d} - \frac{63 a^2 \cos[c+dx]}{128 d (a+a \sin[c+dx])^{3/2}} - \frac{21 a^2 \sec[c+dx]}{80 d (a+a \sin[c+dx])^{3/2}} + \\
& \frac{21 a \sec[c+dx]}{32 d \sqrt{a+a \sin[c+dx]}} + \frac{3 a \sec[c+dx]^3}{10 d \sqrt{a+a \sin[c+dx]}} + \frac{\sec[c+dx]^5 \sqrt{a+a \sin[c+dx]}}{5 d}
\end{aligned}$$

Result (type 3, 191 leaves):

$$\begin{aligned}
& \left(\sqrt{a(1+\sin[c+dx])} \left((-2520 - 2520 i) (-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \sec\left[\frac{dx}{4}\right]\right. \right. \right. \\
& \quad \left. \left. \left(\cos\left[\frac{1}{4}(2c+dx)\right] - \sin\left[\frac{1}{4}(2c+dx)\right] \right) \right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) \right)^4 + \\
& \quad \left. \left(649 + 1092 \cos[2(c+dx)] + 315 \cos[4(c+dx)] + 1572 \sin[c+dx] + 420 \sin[3(c+dx)] \right) \right) / \\
& \quad \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^5 \Bigg) / \\
& \quad \left(5120 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^5 \right)
\end{aligned}$$

Problem 114: Result more than twice size of optimal antiderivative.

$$\int \cos[c+dx]^7 (a+a \sin[c+dx])^{3/2} dx$$

Optimal (type 3, 97 leaves, 3 steps):

$$\begin{aligned}
& \frac{16 (a+a \sin[c+dx])^{11/2}}{11 a^4 d} - \frac{24 (a+a \sin[c+dx])^{13/2}}{13 a^5 d} + \\
& \frac{4 (a+a \sin[c+dx])^{15/2}}{5 a^6 d} - \frac{2 (a+a \sin[c+dx])^{17/2}}{17 a^7 d}
\end{aligned}$$

Result (type 3, 865 leaves):

$$\begin{aligned}
 & \frac{35 \cos\left[\frac{1}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{64 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{7 \cos\left[\frac{3}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{32 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \\
 & \frac{7 \cos\left[\frac{5}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{160 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{\cos\left[\frac{7}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \\
 & \frac{5 \cos\left[\frac{11}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{352 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{\cos\left[\frac{13}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{416 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \\
 & \frac{\cos\left[\frac{15}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{640 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{\cos\left[\frac{17}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{2176 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \\
 & \frac{35 \sin\left[\frac{1}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{3/2}}{64 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \frac{7 (a(1+\sin[c+dx]))^{3/2} \sin\left[\frac{3}{2}(c+dx)\right]}{32 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \\
 & \frac{7 (a(1+\sin[c+dx]))^{3/2} \sin\left[\frac{5}{2}(c+dx)\right]}{160 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \frac{(a(1+\sin[c+dx]))^{3/2} \sin\left[\frac{7}{2}(c+dx)\right]}{16 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \\
 & \frac{5 (a(1+\sin[c+dx]))^{3/2} \sin\left[\frac{11}{2}(c+dx)\right]}{352 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{(a(1+\sin[c+dx]))^{3/2} \sin\left[\frac{13}{2}(c+dx)\right]}{416 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \\
 & \frac{(a(1+\sin[c+dx]))^{3/2} \sin\left[\frac{15}{2}(c+dx)\right]}{640 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{(a(1+\sin[c+dx]))^{3/2} \sin\left[\frac{17}{2}(c+dx)\right]}{2176 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3}
 \end{aligned}$$

Problem 115: Result more than twice size of optimal antiderivative.

$$\int \cos[c+dx]^6 (a+a \sin[c+dx])^{3/2} dx$$

Optimal (type 3, 159 leaves, 5 steps):

$$\begin{aligned}
 & - \frac{4096 a^5 \cos[c+dx]^7}{45045 d (a+a \sin[c+dx])^{7/2}} - \frac{1024 a^4 \cos[c+dx]^7}{6435 d (a+a \sin[c+dx])^{5/2}} - \\
 & \frac{128 a^3 \cos[c+dx]^7}{715 d (a+a \sin[c+dx])^{3/2}} - \frac{32 a^2 \cos[c+dx]^7}{195 d \sqrt{a+a \sin[c+dx]}} - \frac{2 a \cos[c+dx]^7 \sqrt{a+a \sin[c+dx]}}{15 d}
 \end{aligned}$$

Result (type 3, 865 leaves):

$$\begin{aligned}
 & - \frac{45 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{3/2}}{64 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} + \frac{25 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{3/2}}{192 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} \\
 & - \frac{39 \operatorname{Cos}\left[\frac{5}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{3/2}}{320 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} + \frac{3 \operatorname{Cos}\left[\frac{7}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{3/2}}{448 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} \\
 & - \frac{17 \operatorname{Cos}\left[\frac{9}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{3/2}}{576 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} + \frac{3 \operatorname{Cos}\left[\frac{11}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{3/2}}{704 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} \\
 & - \frac{3 \operatorname{Cos}\left[\frac{13}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{3/2}}{832 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} + \frac{\operatorname{Cos}\left[\frac{15}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{3/2}}{960 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} \\
 & + \frac{45 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{3/2}}{64 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} + \frac{25 (a(1+\operatorname{Sin}[c+dx]))^{3/2} \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right]}{192 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} \\
 & + \frac{39 (a(1+\operatorname{Sin}[c+dx]))^{3/2} \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]}{320 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} + \frac{3 (a(1+\operatorname{Sin}[c+dx]))^{3/2} \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right]}{448 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} \\
 & + \frac{17 (a(1+\operatorname{Sin}[c+dx]))^{3/2} \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right]}{576 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} + \frac{3 (a(1+\operatorname{Sin}[c+dx]))^{3/2} \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right]}{704 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} \\
 & - \frac{3 (a(1+\operatorname{Sin}[c+dx]))^{3/2} \operatorname{Sin}\left[\frac{13}{2}(c+dx)\right]}{832 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3} + \frac{(a(1+\operatorname{Sin}[c+dx]))^{3/2} \operatorname{Sin}\left[\frac{15}{2}(c+dx)\right]}{960 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^3}
 \end{aligned}$$

Problem 121: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Sec}[c+dx] (a+a \operatorname{Sin}[c+dx])^{3/2} dx$$

Optimal (type 3, 62 leaves, 4 steps):

$$\frac{2 \sqrt{2} a^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \operatorname{Sin}[c+dx]}}{\sqrt{2} \sqrt{a}}\right]}{d} - \frac{2 a \sqrt{a+a \operatorname{Sin}[c+dx]}}{d}$$

Result (type 3, 98 leaves):

$$\begin{aligned}
 & - \left(\left(2 \left((2+2i) (-1)^{1/4} \operatorname{ArcTan}\left[\frac{1}{2} + \frac{i}{2}\right] (-1)^{1/4} \left(1 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]\right) \right) + \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \left. \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right) (a(1+\operatorname{Sin}[c+dx]))^{3/2} \Big/ \left(d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^3 \right) \right)
 \end{aligned}$$

Problem 122: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+dx]^2 (a+a \operatorname{Sin}[c+dx])^{3/2} dx$$

Optimal (type 3, 26 leaves, 1 step):

$$\frac{2 a \operatorname{Sec}[c+d x] \sqrt{a+a \operatorname{Sin}[c+d x]}}{d}$$

Result (type 3, 67 leaves):

$$\left(2 (a (1 + \operatorname{Sin}[c+d x]))^{3/2}\right) / \left(d \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right) \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^3\right)$$

Problem 123: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Sec}[c+d x]^3 (a+a \operatorname{Sin}[c+d x])^{3/2} dx$$

Optimal (type 3, 73 leaves, 4 steps):

$$\frac{a^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \operatorname{Sin}[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{2 \sqrt{2} d} + \frac{\operatorname{Sec}[c+d x]^2 (a+a \operatorname{Sin}[c+d x])^{3/2}}{2 d}$$

Result (type 3, 134 leaves):

$$\left(a \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] + (1+i)(-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right)(-1)^{1/4} \left(1 + \operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]\right)\right] (-1 + \operatorname{Sin}[c+d x])\right) \sqrt{a(1 + \operatorname{Sin}[c+d x])}\right) / \left(2 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)\right)$$

Problem 124: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Sec}[c+d x]^4 (a+a \operatorname{Sin}[c+d x])^{3/2} dx$$

Optimal (type 3, 107 leaves, 4 steps):

$$-\frac{a^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \operatorname{Cos}[c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sin}[c+d x]}}\right]}{2 \sqrt{2} d} + \frac{a \operatorname{Sec}[c+d x] \sqrt{a+a \operatorname{Sin}[c+d x]}}{2 d} + \frac{\operatorname{Sec}[c+d x]^3 (a+a \operatorname{Sin}[c+d x])^{3/2}}{3 d}$$

Result (type 3, 130 leaves):

$$\frac{1}{d} \left(\frac{1}{12} + \frac{i}{12} \right) a \operatorname{Sec}[c + dx]^3 \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^2$$

$$\sqrt{a (1 + \sin[c + dx])} \left(6 (-1)^{3/4} \operatorname{ArcTanh} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left(-1 + \tan \left[\frac{1}{4} (c + dx) \right] \right) \right] \right)$$

$$\left(\cos \left[\frac{1}{2} (c + dx) \right] - \sin \left[\frac{1}{2} (c + dx) \right] \right)^3 - (1 - i) (-5 + 3 \sin[c + dx]) \right)$$

Problem 125: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Sec}[c + dx]^5 (a + a \sin[c + dx])^{3/2} dx$$

Optimal (type 3, 127 leaves, 6 steps):

$$\frac{15 a^{3/2} \operatorname{ArcTanh} \left[\frac{\sqrt{a + a \sin[c + dx]}}{\sqrt{2} \sqrt{a}} \right]}{32 \sqrt{2} d} - \frac{15 a^2}{32 d \sqrt{a + a \sin[c + dx]}} +$$

$$\frac{5 a \operatorname{Sec}[c + dx]^2 \sqrt{a + a \sin[c + dx]}}{16 d} + \frac{\operatorname{Sec}[c + dx]^4 (a + a \sin[c + dx])^{3/2}}{4 d}$$

Result (type 3, 161 leaves):

$$\frac{1}{d} \left(\frac{1}{128} + \frac{i}{128} \right) a \operatorname{Sec}[c + dx]^4 \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right)^2$$

$$\sqrt{a (1 + \sin[c + dx])} \left(-60 (-1)^{1/4} \operatorname{ArcTan} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \left(1 + \tan \left[\frac{1}{4} (c + dx) \right] \right) \right] \right)$$

$$\left(\cos \left[\frac{1}{2} (c + dx) \right] - \sin \left[\frac{1}{2} (c + dx) \right] \right)^4 \left(\cos \left[\frac{1}{2} (c + dx) \right] + \sin \left[\frac{1}{2} (c + dx) \right] \right) +$$

$$(1 - i) (-9 + 15 \cos[2(c + dx)] + 40 \sin[c + dx]) \right)$$

Problem 126: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Sec}[c + dx]^6 (a + a \sin[c + dx])^{3/2} dx$$

Optimal (type 3, 169 leaves, 6 steps):

$$-\frac{7 a^{3/2} \operatorname{ArcTanh} \left[\frac{\sqrt{a} \cos[c + dx]}{\sqrt{2} \sqrt{a + a \sin[c + dx]}} \right]}{16 \sqrt{2} d} - \frac{7 a^3 \cos[c + dx]}{16 d (a + a \sin[c + dx])^{3/2}} + \frac{7 a^2 \operatorname{Sec}[c + dx]}{12 d \sqrt{a + a \sin[c + dx]}} +$$

$$\frac{7 a \operatorname{Sec}[c + dx]^3 \sqrt{a + a \sin[c + dx]}}{30 d} + \frac{\operatorname{Sec}[c + dx]^5 (a + a \sin[c + dx])^{3/2}}{5 d}$$

Result (type 3, 288 leaves):

$$\frac{1}{240 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^5}$$

$$\left(30 \sin \left[\frac{1}{2} (c + d x) \right] - 15 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) + (105 + 105 i) (-1)^{3/4} \right.$$

$$\left. \operatorname{ArcTanh} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left(-1 + \tan \left[\frac{1}{4} (c + d x) \right] \right) \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + \right.$$

$$\frac{24 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^5} + \frac{40 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} +$$

$$\left. \frac{90 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2}{\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right]} \right) (a (1 + \sin [c + d x]))^{3/2}$$

Problem 127: Result more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^5 (a + a \sin [c + d x])^{5/2} dx$$

Optimal (type 3, 73 leaves, 3 steps):

$$\frac{8 (a + a \sin [c + d x])^{11/2}}{11 a^3 d} - \frac{8 (a + a \sin [c + d x])^{13/2}}{13 a^4 d} + \frac{2 (a + a \sin [c + d x])^{15/2}}{15 a^5 d}$$

Result (type 3, 865 leaves):

$$\begin{aligned}
 & \frac{45 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{64 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} - \frac{65 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{192 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} \\
 & \frac{\operatorname{Cos}\left[\frac{5}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{320 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} - \frac{5 \operatorname{Cos}\left[\frac{7}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{64 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} \\
 & \frac{5 \operatorname{Cos}\left[\frac{9}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{192 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} - \frac{5 \operatorname{Cos}\left[\frac{11}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{704 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} \\
 & \frac{5 \operatorname{Cos}\left[\frac{13}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{832 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} + \frac{\operatorname{Cos}\left[\frac{15}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{960 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} + \\
 & \frac{45 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{64 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} + \frac{65 (a(1+\operatorname{Sin}[c+dx]))^{5/2} \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right]}{192 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} - \\
 & \frac{(a(1+\operatorname{Sin}[c+dx]))^{5/2} \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]}{320 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} + \frac{5 (a(1+\operatorname{Sin}[c+dx]))^{5/2} \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right]}{64 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} - \\
 & \frac{5 (a(1+\operatorname{Sin}[c+dx]))^{5/2} \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right]}{192 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} + \frac{5 (a(1+\operatorname{Sin}[c+dx]))^{5/2} \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right]}{704 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} - \\
 & \frac{5 (a(1+\operatorname{Sin}[c+dx]))^{5/2} \operatorname{Sin}\left[\frac{13}{2}(c+dx)\right]}{832 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} - \frac{(a(1+\operatorname{Sin}[c+dx]))^{5/2} \operatorname{Sin}\left[\frac{15}{2}(c+dx)\right]}{960 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}
 \end{aligned}$$

Problem 128: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c+dx]^4 (a+a \operatorname{Sin}[c+dx])^{5/2} dx$$

Optimal (type 3, 159 leaves, 5 steps):

$$\begin{aligned}
 & -\frac{4096 a^5 \operatorname{Cos}[c+dx]^5}{15015 d (a+a \operatorname{Sin}[c+dx])^{5/2}} - \frac{1024 a^4 \operatorname{Cos}[c+dx]^5}{3003 d (a+a \operatorname{Sin}[c+dx])^{3/2}} - \frac{128 a^3 \operatorname{Cos}[c+dx]^5}{429 d \sqrt{a+a \operatorname{Sin}[c+dx]}} \\
 & \frac{32 a^2 \operatorname{Cos}[c+dx]^5 \sqrt{a+a \operatorname{Sin}[c+dx]}}{143 d} - \frac{2 a \operatorname{Cos}[c+dx]^5 (a+a \operatorname{Sin}[c+dx])^{3/2}}{13 d}
 \end{aligned}$$

Result (type 3, 757 leaves):

$$\begin{aligned}
 & - \frac{9 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{8d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} + \frac{3 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{32d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} - \\
 & \frac{29 \operatorname{Cos}\left[\frac{5}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{160d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} - \frac{5 \operatorname{Cos}\left[\frac{7}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{112d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} - \\
 & \frac{\operatorname{Cos}\left[\frac{9}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{48d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} - \frac{5 \operatorname{Cos}\left[\frac{11}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{352d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} + \\
 & \frac{\operatorname{Cos}\left[\frac{13}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{416d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} + \frac{9 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{5/2}}{8d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} + \\
 & \frac{3(a(1+\operatorname{Sin}[c+dx]))^{5/2} \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right]}{32d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} + \frac{29(a(1+\operatorname{Sin}[c+dx]))^{5/2} \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]}{160d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} - \\
 & \frac{5(a(1+\operatorname{Sin}[c+dx]))^{5/2} \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right]}{112d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} + \frac{(a(1+\operatorname{Sin}[c+dx]))^{5/2} \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right]}{48d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} - \\
 & \frac{5(a(1+\operatorname{Sin}[c+dx]))^{5/2} \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right]}{352d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5} - \frac{(a(1+\operatorname{Sin}[c+dx]))^{5/2} \operatorname{Sin}\left[\frac{13}{2}(c+dx)\right]}{416d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}
 \end{aligned}$$

Problem 132: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Sec}[c+dx] (a+a \operatorname{Sin}[c+dx])^{5/2} dx$$

Optimal (type 3, 86 leaves, 5 steps):

$$\frac{4\sqrt{2} a^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \operatorname{Sin}[c+dx]}}{\sqrt{2}\sqrt{a}}\right]}{d} - \frac{4a^2 \sqrt{a+a \operatorname{Sin}[c+dx]}}{d} - \frac{2a(a+a \operatorname{Sin}[c+dx])^{3/2}}{3d}$$

Result (type 3, 126 leaves):

$$\begin{aligned}
 & - \left(\left((a(1+\operatorname{Sin}[c+dx]))^{5/2} \left((24+24i) (-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]\right)\right] \right) + \right. \right. \\
 & \quad \left. \left. 15 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] + 15 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] \right) \right) / \\
 & \quad \left(3d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \right)^5 \right)
 \end{aligned}$$

Problem 134: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Sec}[c+dx]^3 (a+a \operatorname{Sin}[c+dx])^{5/2} dx$$

Optimal (type 3, 69 leaves, 4 steps):

$$-\frac{a^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin [c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{\sqrt{2} d} + \frac{a \operatorname{Sec}[c+d x]^2 (a+a \sin [c+d x])^{3/2}}{d}$$

Result (type 3, 138 leaves):

$$-\left(\left(a^2 \left(-\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)+(1+i)(-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2}+\frac{i}{2}\right)(-1)^{1/4}\left(1+\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]\right)\right](-1+\operatorname{Sin}[c+d x])\right)\sqrt{a(1+\operatorname{Sin}[c+d x])}\right) / \left(d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)\right)$$

Problem 135: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+d x]^4 (a+a \sin [c+d x])^{5/2} dx$$

Optimal (type 3, 30 leaves, 1 step):

$$\frac{2 a \operatorname{Sec}[c+d x]^3 (a+a \sin [c+d x])^{3/2}}{3 d}$$

Result (type 3, 69 leaves):

$$\left(2(a(1+\operatorname{Sin}[c+d x]))^{5/2}\right) / \left(3 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^3\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^5\right)$$

Problem 136: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Sec}[c+d x]^5 (a+a \sin [c+d x])^{5/2} dx$$

Optimal (type 3, 103 leaves, 5 steps):

$$\frac{3 a^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin [c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{16 \sqrt{2} d} + \frac{3 a \operatorname{Sec}[c+d x]^2 (a+a \sin [c+d x])^{3/2}}{16 d} + \frac{\operatorname{Sec}[c+d x]^4 (a+a \sin [c+d x])^{5/2}}{4 d}$$

Result (type 3, 174 leaves):

$$\left(a^2 \sqrt{a (1 + \sin [c + d x])} \left(11 \cos \left[\frac{1}{2} (c + d x) \right] + 3 \cos \left[\frac{3}{2} (c + d x) \right] + \right. \right. \\ \left. \left. 11 \sin \left[\frac{1}{2} (c + d x) \right] + (3 + 3 i) (-1)^{1/4} \operatorname{ArcTan} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \left(1 + \tan \left[\frac{1}{4} (c + d x) \right] \right) \right] \right) \right. \\ \left. (-3 + \cos [2 (c + d x)] + 4 \sin [c + d x]) - 3 \sin \left[\frac{3}{2} (c + d x) \right] \right) \Big/ \\ \left(32 d \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) \right)$$

Problem 137: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec [c + d x]^6 (a + a \sin [c + d x])^{5/2} dx$$

Optimal (type 3, 139 leaves, 5 steps):

$$-\frac{a^{5/2} \operatorname{ArcTanh} \left[\frac{\sqrt{a} \cos [c + d x]}{\sqrt{2} \sqrt{a + a \sin [c + d x]}} \right]}{4 \sqrt{2} d} + \frac{a^2 \sec [c + d x] \sqrt{a + a \sin [c + d x]}}{4 d} + \\ \frac{a \sec [c + d x]^3 (a + a \sin [c + d x])^{3/2}}{6 d} + \frac{\sec [c + d x]^5 (a + a \sin [c + d x])^{5/2}}{5 d}$$

Result (type 3, 129 leaves):

$$\left(\left((15 + 15 i) (-1)^{3/4} \operatorname{ArcTanh} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left(-1 + \tan \left[\frac{1}{4} (c + d x) \right] \right) \right] \right) + \right. \\ \left. \frac{89 - 15 \cos [2 (c + d x)] - 80 \sin [c + d x]}{2 \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^5} \right) (a (1 + \sin [c + d x]))^{5/2} \Big/ \\ \left(60 d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^5 \right)$$

Problem 138: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec [c + d x]^7 (a + a \sin [c + d x])^{5/2} dx$$

Optimal (type 3, 159 leaves, 7 steps):

$$\frac{35 a^{5/2} \operatorname{ArcTanh} \left[\frac{\sqrt{a + a \sin [c + d x]}}{\sqrt{2} \sqrt{a}} \right]}{128 \sqrt{2} d} - \frac{35 a^3}{128 d \sqrt{a + a \sin [c + d x]}} + \frac{35 a^2 \sec [c + d x]^2 \sqrt{a + a \sin [c + d x]}}{192 d} + \\ \frac{7 a \sec [c + d x]^4 (a + a \sin [c + d x])^{3/2}}{48 d} + \frac{\sec [c + d x]^6 (a + a \sin [c + d x])^{5/2}}{6 d}$$

Result (type 3, 176 leaves):

$$\frac{1}{d} \left(\frac{1}{3072} + \frac{i}{3072} \right) a^2 \operatorname{Sec}[c + dx]^6 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4$$

$$\sqrt{a(1 + \sin[c + dx])} \left(-840 (-1)^{1/4} \operatorname{ArcTan}\left[\frac{1}{2} + \frac{i}{2}\right] (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4}(c + dx)\right]\right) \right)$$

$$\left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^6 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right) +$$

$$(1 - i) (490 \cos[2(c + dx)] + 791 \sin[c + dx] - 15(10 + 7 \sin[3(c + dx)]))$$

Problem 139: Result more than twice size of optimal antiderivative.

$$\int \cos[c + dx]^7 (a + a \sin[c + dx])^{7/2} dx$$

Optimal (type 3, 97 leaves, 3 steps):

$$\frac{16 (a + a \sin[c + dx])^{15/2}}{15 a^4 d} - \frac{24 (a + a \sin[c + dx])^{17/2}}{17 a^5 d} +$$

$$\frac{12 (a + a \sin[c + dx])^{19/2}}{19 a^6 d} - \frac{2 (a + a \sin[c + dx])^{21/2}}{21 a^7 d}$$

Result (type 3, 1189 leaves):

$$\begin{aligned}
 & \frac{91 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{128 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{91 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{256 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{7 \operatorname{Cos}\left[\frac{5}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{1280 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{43 \operatorname{Cos}\left[\frac{7}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{448 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{7 \operatorname{Cos}\left[\frac{9}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{192 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{7 \operatorname{Cos}\left[\frac{11}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{512 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{7 \operatorname{Cos}\left[\frac{13}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{512 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{7 \operatorname{Cos}\left[\frac{15}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{3840 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{7 \operatorname{Cos}\left[\frac{17}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{4352 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{7 \operatorname{Cos}\left[\frac{19}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{9728 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{\operatorname{Cos}\left[\frac{21}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{10752 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{91 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{128 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{91 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right]}{256 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{7 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]}{1280 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{43 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right]}{448 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{7 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right]}{192 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{7 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right]}{512 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{7 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{13}{2}(c+dx)\right]}{512 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{7 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{15}{2}(c+dx)\right]}{3840 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{7 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{17}{2}(c+dx)\right]}{4352 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{7 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{19}{2}(c+dx)\right]}{9728 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{(a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{21}{2}(c+dx)\right]}{10752 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7}
 \end{aligned}$$

Problem 140: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c+dx]^6 (a+a \operatorname{Sin}[c+dx])^{7/2} dx$$

Optimal (type 3, 223 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{131072 a^7 \operatorname{Cos}[c+dx]^7}{969969 d (a+a \operatorname{Sin}[c+dx])^{7/2}} - \frac{32768 a^6 \operatorname{Cos}[c+dx]^7}{138567 d (a+a \operatorname{Sin}[c+dx])^{5/2}} - \frac{12288 a^5 \operatorname{Cos}[c+dx]^7}{46189 d (a+a \operatorname{Sin}[c+dx])^{3/2}} \\
 & - \frac{1024 a^4 \operatorname{Cos}[c+dx]^7}{4199 d \sqrt{a+a \operatorname{Sin}[c+dx]}} - \frac{64 a^3 \operatorname{Cos}[c+dx]^7 \sqrt{a+a \operatorname{Sin}[c+dx]}}{323 d} \\
 & - \frac{48 a^2 \operatorname{Cos}[c+dx]^7 (a+a \operatorname{Sin}[c+dx])^{3/2}}{323 d} - \frac{2 a \operatorname{Cos}[c+dx]^7 (a+a \operatorname{Sin}[c+dx])^{5/2}}{19 d}
 \end{aligned}$$

Result (type 3, 1081 leaves):

$$\begin{aligned}
 & - \frac{143 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{128 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{13 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{128 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & - \frac{13 \operatorname{Cos}\left[\frac{5}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{64 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{23 \operatorname{Cos}\left[\frac{7}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{448 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & - \frac{7 \operatorname{Cos}\left[\frac{9}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{192 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{19 \operatorname{Cos}\left[\frac{11}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{704 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & - \frac{7 \operatorname{Cos}\left[\frac{13}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{3328 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{\operatorname{Cos}\left[\frac{15}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{256 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & - \frac{7 \operatorname{Cos}\left[\frac{17}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{4352 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{\operatorname{Cos}\left[\frac{19}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{4864 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & - \frac{143 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{128 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{13 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right]}{128 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & - \frac{13 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]}{64 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{23 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right]}{448 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & - \frac{7 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right]}{192 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{19 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right]}{704 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & - \frac{7 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{13}{2}(c+dx)\right]}{3328 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{(a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{15}{2}(c+dx)\right]}{256 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & - \frac{7 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{17}{2}(c+dx)\right]}{4352 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{(a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{19}{2}(c+dx)\right]}{4864 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7}
 \end{aligned}$$

Problem 141: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c+dx]^5 (a+a \operatorname{Sin}[c+dx])^{7/2} dx$$

Optimal (type 3, 73 leaves, 3 steps):

$$\frac{8 (a + a \sin[c + d x])^{13/2}}{13 a^3 d} - \frac{8 (a + a \sin[c + d x])^{15/2}}{15 a^4 d} + \frac{2 (a + a \sin[c + d x])^{17/2}}{17 a^5 d}$$

Result (type 3, 865 leaves):

$$\begin{aligned} & \frac{55 \cos\left[\frac{1}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{64 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{11 \cos\left[\frac{3}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{24 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \\ & \frac{\cos\left[\frac{5}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{20 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{3 \cos\left[\frac{7}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{32 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \\ & \frac{5 \cos\left[\frac{9}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{96 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{\cos\left[\frac{13}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{104 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} + \\ & \frac{7 \cos\left[\frac{15}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{1920 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{\cos\left[\frac{17}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{2176 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} + \\ & \frac{55 \sin\left[\frac{1}{2}(c+dx)\right] (a(1+\sin[c+dx]))^{7/2}}{64 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{11 (a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{3}{2}(c+dx)\right]}{24 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \\ & \frac{(a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{5}{2}(c+dx)\right]}{20 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{3 (a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{7}{2}(c+dx)\right]}{32 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \\ & \frac{5 (a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{9}{2}(c+dx)\right]}{96 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{(a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{13}{2}(c+dx)\right]}{104 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} - \\ & \frac{7 (a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{15}{2}(c+dx)\right]}{1920 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{(a(1+\sin[c+dx]))^{7/2} \sin\left[\frac{17}{2}(c+dx)\right]}{2176 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^7} \end{aligned}$$

Problem 142: Result more than twice size of optimal antiderivative.

$$\int \cos[c + d x]^4 (a + a \sin[c + d x])^{7/2} dx$$

Optimal (type 3, 191 leaves, 6 steps):

$$\begin{aligned} & - \frac{16384 a^6 \cos[c + d x]^5}{45045 d (a + a \sin[c + d x])^{5/2}} - \frac{4096 a^5 \cos[c + d x]^5}{9009 d (a + a \sin[c + d x])^{3/2}} - \\ & \frac{512 a^4 \cos[c + d x]^5}{1287 d \sqrt{a + a \sin[c + d x]}} - \frac{128 a^3 \cos[c + d x]^5 \sqrt{a + a \sin[c + d x]}}{429 d} - \\ & \frac{8 a^2 \cos[c + d x]^5 (a + a \sin[c + d x])^{3/2}}{39 d} - \frac{2 a \cos[c + d x]^5 (a + a \sin[c + d x])^{5/2}}{15 d} \end{aligned}$$

Result (type 3, 865 leaves):

$$\begin{aligned}
 & - \frac{99 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{64 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{11 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{192 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \\
 & \frac{77 \operatorname{Cos}\left[\frac{5}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{320 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{43 \operatorname{Cos}\left[\frac{7}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{448 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \\
 & \frac{7 \operatorname{Cos}\left[\frac{9}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{576 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{17 \operatorname{Cos}\left[\frac{11}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{704 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \\
 & \frac{7 \operatorname{Cos}\left[\frac{13}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{832 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{\operatorname{Cos}\left[\frac{15}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{960 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \\
 & \frac{99 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{64 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{11 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right]}{192 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \\
 & \frac{77 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]}{43 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right]} + \frac{320 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7}{448 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \\
 & \frac{7 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right]}{17 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right]} - \frac{576 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7}{704 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \\
 & \frac{7 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{13}{2}(c+dx)\right]}{832 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{(a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{15}{2}(c+dx)\right]}{960 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7}
 \end{aligned}$$

Problem 143: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c+dx]^3 (a+a \operatorname{Sin}[c+dx])^{7/2} dx$$

Optimal (type 3, 49 leaves, 3 steps):

$$\frac{4 (a+a \operatorname{Sin}[c+dx])^{11/2}}{11 a^2 d} - \frac{2 (a+a \operatorname{Sin}[c+dx])^{13/2}}{13 a^3 d}$$

Result (type 3, 757 leaves):

$$\begin{aligned}
 & \frac{9 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{8 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{21 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{32 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{5 \operatorname{Cos}\left[\frac{5}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{32 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{\operatorname{Cos}\left[\frac{7}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{\operatorname{Cos}\left[\frac{9}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{7 \operatorname{Cos}\left[\frac{11}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{352 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{\operatorname{Cos}\left[\frac{13}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{416 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{9 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{8 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{21 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right]}{32 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{5 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]}{32 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{(a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right]}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{(a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right]}{16 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & \frac{7 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right]}{352 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{(a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{13}{2}(c+dx)\right]}{416 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7}
 \end{aligned}$$

Problem 144: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c+dx]^2 (a+a \operatorname{Sin}[c+dx])^{7/2} dx$$

Optimal (type 3, 159 leaves, 5 steps):

$$\begin{aligned}
 & -\frac{4096 a^5 \operatorname{Cos}[c+dx]^3}{3465 d (a+a \operatorname{Sin}[c+dx])^{3/2}} - \\
 & \frac{1024 a^4 \operatorname{Cos}[c+dx]^3}{1155 d \sqrt{a+a \operatorname{Sin}[c+dx]}} - \frac{128 a^3 \operatorname{Cos}[c+dx]^3 \sqrt{a+a \operatorname{Sin}[c+dx]}}{231 d} \\
 & \frac{32 a^2 \operatorname{Cos}[c+dx]^3 (a+a \operatorname{Sin}[c+dx])^{3/2}}{99 d} - \frac{2 a \operatorname{Cos}[c+dx]^3 (a+a \operatorname{Sin}[c+dx])^{5/2}}{11 d}
 \end{aligned}$$

Result (type 3, 649 leaves):

$$\begin{aligned}
 & - \frac{21 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{8d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{\operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{8d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} \\
 & - \frac{21 \operatorname{Cos}\left[\frac{5}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{80d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{19 \operatorname{Cos}\left[\frac{7}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{112d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \\
 & + \frac{7 \operatorname{Cos}\left[\frac{9}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{144d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{\operatorname{Cos}\left[\frac{11}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{176d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \\
 & - \frac{21 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] (a(1+\operatorname{Sin}[c+dx]))^{7/2}}{8d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{(a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right]}{8d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \\
 & - \frac{21 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]}{80d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \frac{19 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right]}{112d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} - \\
 & + \frac{7 (a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right]}{144d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7} + \frac{(a(1+\operatorname{Sin}[c+dx]))^{7/2} \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right]}{176d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7}
 \end{aligned}$$

Problem 146: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Sec}[c+dx] (a+a \operatorname{Sin}[c+dx])^{7/2} dx$$

Optimal (type 3, 110 leaves, 6 steps):

$$\frac{8 \sqrt{2} a^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \operatorname{Sin}[c+dx]}}{\sqrt{2} \sqrt{a}}\right]}{d} - \frac{8 a^3 \sqrt{a+a \operatorname{Sin}[c+dx]}}{d} - \frac{4 a^2 (a+a \operatorname{Sin}[c+dx])^{3/2}}{3 d} - \frac{2 a (a+a \operatorname{Sin}[c+dx])^{5/2}}{5 d}$$

Result (type 3, 165 leaves):

$$\begin{aligned}
 & - \left(\left(a^3 (1+\operatorname{Sin}[c+dx])^3 \sqrt{a(1+\operatorname{Sin}[c+dx])} \right. \right. \\
 & \quad \left. \left((480+480i) (-1)^{1/4} \operatorname{ArcTan}\left[\frac{1}{2} + \frac{i}{2}\right] (-1)^{1/4} \left(1 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]\right) \right) + \right. \\
 & \quad \left. 330 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] - 35 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] - 3 \operatorname{Cos}\left[\frac{5}{2}(c+dx)\right] + 330 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] + \right. \\
 & \quad \left. 35 \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right] - 3 \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right] \right) \left. \right) / \left(30d \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^7 \right)
 \end{aligned}$$

Problem 148: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Sec}[c+dx]^3 (a+a \operatorname{Sin}[c+dx])^{7/2} dx$$

Optimal (type 3, 91 leaves, 5 steps):

$$-\frac{3\sqrt{2}a^{7/2}\operatorname{ArcTanh}\left[\frac{\sqrt{a+a\sin[c+dx]}}{\sqrt{2}\sqrt{a}}\right]}{d} + \frac{3a^3\sqrt{a+a\sin[c+dx]}}{d} + \frac{a\sec[c+dx]^2(a+a\sin[c+dx])^{5/2}}{d}$$

Result (type 3, 159 leaves):

$$\left(a^3\sqrt{a(1+\sin[c+dx])}\left(3\cos\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{3}{2}(c+dx)\right] + 3\sin\left[\frac{1}{2}(c+dx)\right] - (6+6i)(-1)^{1/4}\operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right)(-1)^{1/4}\left(1 + \tan\left[\frac{1}{4}(c+dx)\right]\right)\right](-1 + \sin[c+dx]) - \sin\left[\frac{3}{2}(c+dx)\right]\right)\right) / \left(d\left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^2\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)\right)$$

Problem 150: Result unnecessarily involves imaginary or complex numbers.

$$\int \sec[c+dx]^5 (a+a\sin[c+dx])^{7/2} dx$$

Optimal (type 3, 106 leaves, 5 steps):

$$-\frac{a^{7/2}\operatorname{ArcTanh}\left[\frac{\sqrt{a+a\sin[c+dx]}}{\sqrt{2}\sqrt{a}}\right]}{8\sqrt{2}d} - \frac{a^2\sec[c+dx]^2(a+a\sin[c+dx])^{3/2}}{8d} + \frac{a\sec[c+dx]^4(a+a\sin[c+dx])^{5/2}}{2d}$$

Result (type 3, 172 leaves):

$$-\left(\left(a^3\sqrt{a(1+\sin[c+dx])}\left(-7\cos\left[\frac{1}{2}(c+dx)\right] + \cos\left[\frac{3}{2}(c+dx)\right] - 7\sin\left[\frac{1}{2}(c+dx)\right] + (1+i)(-1)^{1/4}\operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right)(-1)^{1/4}\left(1 + \tan\left[\frac{1}{4}(c+dx)\right]\right)\right]\right)\right)\left(-3 + \cos[2(c+dx)] + 4\sin[c+dx] - \sin\left[\frac{3}{2}(c+dx)\right]\right)\right) / \left(16d\left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^4\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)\right)$$

Problem 151: Result more than twice size of optimal antiderivative.

$$\int \sec[c+dx]^6 (a+a\sin[c+dx])^{7/2} dx$$

Optimal (type 3, 30 leaves, 1 step):

$$\frac{2 a \operatorname{Sec}[c+d x]^5 (a+a \operatorname{Sin}[c+d x])^{5/2}}{5 d}$$

Result (type 3, 69 leaves):

$$\left(2 (a (1+\operatorname{Sin}[c+d x]))^{7/2}\right) / \left(5 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^5 \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^7\right)$$

Problem 152: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Sec}[c+d x]^7 (a+a \operatorname{Sin}[c+d x])^{7/2} dx$$

Optimal (type 3, 135 leaves, 6 steps):

$$\frac{5 a^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{a+a \operatorname{Sin}[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{64 \sqrt{2} d} + \frac{5 a^2 \operatorname{Sec}[c+d x]^2 (a+a \operatorname{Sin}[c+d x])^{3/2}}{64 d} + \frac{5 a \operatorname{Sec}[c+d x]^4 (a+a \operatorname{Sin}[c+d x])^{5/2}}{48 d} + \frac{\operatorname{Sec}[c+d x]^6 (a+a \operatorname{Sin}[c+d x])^{7/2}}{6 d}$$

Result (type 3, 205 leaves):

$$\left(a^3 \sqrt{a (1+\operatorname{Sin}[c+d x])}\right) \left(198 \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+85 \operatorname{Cos}\left[\frac{3}{2}(c+d x)\right]-15 \operatorname{Cos}\left[\frac{5}{2}(c+d x)\right]-\left(60+60 i\right)(-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2}+\frac{i}{2}\right)(-1)^{1/4}\left(1+\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]\right)\right]\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^6+198 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]-85 \operatorname{Sin}\left[\frac{3}{2}(c+d x)\right]-15 \operatorname{Sin}\left[\frac{5}{2}(c+d x)\right]\right) / \left(768 d \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^6 \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)\right)$$

Problem 153: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Sec}[c+d x]^8 (a+a \operatorname{Sin}[c+d x])^{7/2} dx$$

Optimal (type 3, 171 leaves, 6 steps):

$$\begin{aligned}
 & - \frac{a^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{2} \sqrt{a+a \sin[c+dx]}}\right]}{8 \sqrt{2} d} + \\
 & \frac{a^3 \sec[c+dx] \sqrt{a+a \sin[c+dx]}}{8 d} + \frac{a^2 \sec[c+dx]^3 (a+a \sin[c+dx])^{3/2}}{12 d} + \\
 & \frac{a \sec[c+dx]^5 (a+a \sin[c+dx])^{5/2}}{10 d} + \frac{\sec[c+dx]^7 (a+a \sin[c+dx])^{7/2}}{7 d}
 \end{aligned}$$

Result (type 3, 139 leaves):

$$\begin{aligned}
 & \left((a (1 + \sin[c + dx]))^{7/2} \right. \\
 & \left. \left((105 + 105 i) (-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \tan\left[\frac{1}{4}(c + dx)\right]\right)\right] \right) + \right. \\
 & \left. (2286 - 770 \cos[2(c + dx)] - 2471 \sin[c + dx] + 105 \sin[3(c + dx)]) \right) / \\
 & \left(4 \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^7 \right) / \\
 & \left(840 d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^7 \right)
 \end{aligned}$$

Problem 154: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^9 (a + a \sin[c + dx])^{7/2} dx$$

Optimal (type 3, 191 leaves, 8 steps):

$$\begin{aligned}
 & \frac{315 a^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin[c+dx]}}{\sqrt{2} \sqrt{a}}\right]}{2048 \sqrt{2} d} - \frac{315 a^4}{2048 d \sqrt{a+a \sin[c+dx]}} + \\
 & \frac{105 a^3 \sec[c+dx]^2 \sqrt{a+a \sin[c+dx]}}{1024 d} + \frac{21 a^2 \sec[c+dx]^4 (a+a \sin[c+dx])^{3/2}}{256 d} + \\
 & \frac{3 a \sec[c+dx]^6 (a+a \sin[c+dx])^{5/2}}{32 d} + \frac{\sec[c+dx]^8 (a+a \sin[c+dx])^{7/2}}{8 d}
 \end{aligned}$$

Result (type 3, 735 leaves):

$$\begin{aligned}
& - \frac{(a(1 + \sin[c + dx]))^{7/2}}{16 d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^8} - \\
& \left(\left(\frac{315}{2048} + \frac{315 i}{2048} \right) (-1)^{1/4} \operatorname{ArcTan}\left[\frac{1}{2} + \frac{i}{2}\right] (-1)^{1/4} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right] \right. \\
& \quad \left. \left(\cos\left[\frac{1}{4}(c + dx)\right] + \sin\left[\frac{1}{4}(c + dx)\right] \right) \right) (a(1 + \sin[c + dx]))^{7/2} \Big/ \\
& \left(d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^7 \right) + (a(1 + \sin[c + dx]))^{7/2} \Big/ \\
& \left(16 d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^7 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^7 \right) + \\
& \left(5 (a(1 + \sin[c + dx]))^{7/2} \right) \Big/ \\
& \left(64 d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^5 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^7 \right) + \\
& \left(41 (a(1 + \sin[c + dx]))^{7/2} \right) \Big/ \\
& \left(512 d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^3 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^7 \right) + \\
& \left(187 (a(1 + \sin[c + dx]))^{7/2} \right) \Big/ \\
& \left(2048 d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right) \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^7 \right) + \\
& \left(\sin\left[\frac{1}{2}(c + dx)\right] (a(1 + \sin[c + dx]))^{7/2} \right) \Big/ \\
& \left(8 d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^8 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^7 \right) + \\
& \left(5 \sin\left[\frac{1}{2}(c + dx)\right] (a(1 + \sin[c + dx]))^{7/2} \right) \Big/ \\
& \left(32 d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^6 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^7 \right) + \\
& \left(41 \sin\left[\frac{1}{2}(c + dx)\right] (a(1 + \sin[c + dx]))^{7/2} \right) \Big/ \\
& \left(256 d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^4 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^7 \right) + \\
& \left(187 \sin\left[\frac{1}{2}(c + dx)\right] (a(1 + \sin[c + dx]))^{7/2} \right) \Big/ \\
& \left(1024 d \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^2 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^7 \right)
\end{aligned}$$

Problem 155: Result unnecessarily involves imaginary or complex numbers.

$$\int \operatorname{Sec}[c + dx]^{10} (a + a \sin[c + dx])^{7/2} dx$$

Optimal (type 3, 233 leaves, 8 steps):

$$\begin{aligned}
 & - \frac{11 a^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}}\right]}{64 \sqrt{2} d} - \frac{11 a^5 \cos [c+d x]}{64 d (a+a \sin [c+d x])^{3/2}} + \frac{11 a^4 \sec [c+d x]}{48 d \sqrt{a+a \sin [c+d x]}} + \\
 & \frac{11 a^3 \sec [c+d x]^3 \sqrt{a+a \sin [c+d x]}}{120 d} + \frac{11 a^2 \sec [c+d x]^5 (a+a \sin [c+d x])^{3/2}}{140 d} + \\
 & \frac{11 a \sec [c+d x]^7 (a+a \sin [c+d x])^{5/2}}{126 d} + \frac{\sec [c+d x]^9 (a+a \sin [c+d x])^{7/2}}{9 d}
 \end{aligned}$$

Result (type 3, 388 leaves):

$$\begin{aligned}
 & \frac{1}{20160 d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^9} \\
 & \left(630 \sin \left[\frac{1}{2}(c+d x)\right] - 315 \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right) + (3465 + 3465 i) (-1)^{3/4} \right. \\
 & \quad \left. \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \tan \left[\frac{1}{4}(c+d x)\right]\right)\right] \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2 + \right. \\
 & \quad \frac{1120 \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right)^9} + \frac{1440 \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right)^7} + \\
 & \quad \frac{1512 \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right)^5} + \frac{1680 \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2}{\left(\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]\right)^3} + \\
 & \quad \left. \frac{3150 \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2}{\cos \left[\frac{1}{2}(c+d x)\right] - \sin \left[\frac{1}{2}(c+d x)\right]} \right) (a(1 + \sin [c+d x]))^{7/2}
 \end{aligned}$$

Problem 161: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^2}{\sqrt{a+a \sin [c+d x]}} dx$$

Optimal (type 3, 30 leaves, 1 step):

$$- \frac{2 a \cos [c+d x]^3}{3 d (a+a \sin [c+d x])^{3/2}}$$

Result (type 3, 67 leaves):

$$\begin{aligned}
 & - \left(\left(2 \left(\cos \left[\frac{1}{2}(c+d x) \right] - \sin \left[\frac{1}{2}(c+d x) \right] \right) \right)^3 \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right) \right) / \\
 & \quad \left(3 d \sqrt{a(1 + \sin [c+d x])} \right)
 \end{aligned}$$

Problem 163: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Sec}[c + d x]}{\sqrt{a + a \text{Sin}[c + d x]}} dx$$

Optimal (type 3, 60 leaves, 4 steps):

$$\frac{\text{ArcTanh}\left[\frac{\sqrt{a+a \text{Sin}[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{\sqrt{2} \sqrt{a} d} - \frac{1}{d \sqrt{a + a \text{Sin}[c + d x]}}$$

Result (type 3, 76 leaves):

$$\left(-1 - (1 + i) (-1)^{1/4} \text{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \text{Tan}\left[\frac{1}{4}(c + d x)\right]\right)\right] \right) \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right] \right) / \left(d \sqrt{a(1 + \text{Sin}[c + d x])} \right)$$

Problem 164: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Sec}[c + d x]^2}{\sqrt{a + a \text{Sin}[c + d x]}} dx$$

Optimal (type 3, 102 leaves, 4 steps):

$$-\frac{3 \text{ArcTanh}\left[\frac{\sqrt{a} \text{Cos}[c+d x]}{\sqrt{2} \sqrt{a+a \text{Sin}[c+d x]}}\right]}{4 \sqrt{2} \sqrt{a} d} - \frac{3 a \text{Cos}[c + d x]}{4 d (a + a \text{Sin}[c + d x])^{3/2}} + \frac{\text{Sec}[c + d x]}{d \sqrt{a + a \text{Sin}[c + d x]}}$$

Result (type 3, 118 leaves):

$$-\left(\left(\text{Sec}[c + d x] \left(-1 - (3 + 3 i) (-1)^{3/4} \text{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \text{Tan}\left[\frac{1}{4}(c + d x)\right]\right)\right] \right) \right) \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] - \text{Sin}\left[\frac{1}{2}(c + d x)\right] \right) \left(\text{Cos}\left[\frac{1}{2}(c + d x)\right] + \text{Sin}\left[\frac{1}{2}(c + d x)\right] \right)^2 - 3 \text{Sin}[c + d x] \right) / \left(4 d \sqrt{a(1 + \text{Sin}[c + d x])} \right)$$

Problem 165: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\text{Sec}[c + d x]^3}{\sqrt{a + a \text{Sin}[c + d x]}} dx$$

Optimal (type 3, 116 leaves, 6 steps):

$$\frac{5 \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin [c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{8 \sqrt{2} \sqrt{a} d} - \frac{5 a}{12 d (a+a \sin [c+d x])^{3/2}} - \frac{5}{8 d \sqrt{a+a \sin [c+d x]}} + \frac{\operatorname{Sec}[c+d x]^2}{2 d \sqrt{a+a \sin [c+d x]}}$$

Result (type 3, 108 leaves):

$$\left((-30 - 30 i) (-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]\right)\right] \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right) - \operatorname{Sec}[c+d x]^2 (11 + 15 \cos[2(c+d x)] - 20 \sin[c+d x]) \right) / \left(48 d \sqrt{a(1 + \sin[c+d x])}\right)$$

Problem 166: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Sec}[c+d x]^4}{\sqrt{a+a \sin [c+d x]}} dx$$

Optimal (type 3, 162 leaves, 6 steps):

$$-\frac{35 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}}\right]}{64 \sqrt{2} \sqrt{a} d} - \frac{35 a \cos [c+d x]}{64 d (a+a \sin [c+d x])^{3/2}} - \frac{7 a \operatorname{Sec}[c+d x]}{24 d (a+a \sin [c+d x])^{3/2}} + \frac{35 \operatorname{Sec}[c+d x]}{48 d \sqrt{a+a \sin [c+d x]}} + \frac{\operatorname{Sec}[c+d x]^3}{3 d \sqrt{a+a \sin [c+d x]}}$$

Result (type 3, 117 leaves):

$$\left((420 + 420 i) (-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]\right)\right] \left(\cos\left[\frac{1}{2}(c+d x)\right] + \sin\left[\frac{1}{2}(c+d x)\right]\right) + \operatorname{Sec}[c+d x]^3 (102 + 70 \cos[2(c+d x)] + 329 \sin[c+d x] + 105 \sin[3(c+d x)]) \right) / \left(768 d \sqrt{a(1 + \sin[c+d x])}\right)$$

Problem 167: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Sec}[c+d x]^5}{\sqrt{a+a \sin [c+d x]}} dx$$

Optimal (type 3, 175 leaves, 8 steps):

$$\frac{63 \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \sin [c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{128 \sqrt{2} \sqrt{a} d}-\frac{21 a}{64 d(a+a \sin [c+d x])^{3 / 2}}-\frac{9 a \operatorname{Sec}[c+d x]^2}{40 d(a+a \sin [c+d x])^{3 / 2}}-\frac{63}{128 d \sqrt{a+a \sin [c+d x]}}+\frac{63 \operatorname{Sec}[c+d x]^2}{160 d \sqrt{a+a \sin [c+d x]}}+\frac{\operatorname{Sec}[c+d x]^4}{4 d \sqrt{a+a \sin [c+d x]}}$$

Result (type 3, 130 leaves):

$$\left(\left(-315-315 i\right)\left(-1\right)^{1 / 4} \operatorname{ArcTan}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(-1\right)^{1 / 4}\left(1+\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]\right)\right]\right)\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)-\frac{1}{8} \operatorname{Sec}[c+d x]^4\left(649+1092 \operatorname{Cos}[2(c+d x)]+315 \operatorname{Cos}[4(c+d x)]-1572 \operatorname{Sin}[c+d x]-420 \operatorname{Sin}[3(c+d x)]\right)\left(640 d \sqrt{a(1+\operatorname{Sin}[c+d x])}\right) /$$

Problem 168: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Sec}[c+d x]^6}{\sqrt{a+a \sin [c+d x]}} d x$$

Optimal (type 3, 221 leaves, 8 steps):

$$-\frac{231 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \operatorname{Cos}[c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}}\right]}{512 \sqrt{2} \sqrt{a} d}-\frac{231 a \operatorname{Cos}[c+d x]}{512 d(a+a \sin [c+d x])^{3 / 2}}-\frac{77 a \operatorname{Sec}[c+d x]}{320 d(a+a \sin [c+d x])^{3 / 2}}-\frac{11 a \operatorname{Sec}[c+d x]^3}{60 d(a+a \sin [c+d x])^{3 / 2}}+\frac{77 \operatorname{Sec}[c+d x]}{128 d \sqrt{a+a \sin [c+d x]}}+\frac{11 \operatorname{Sec}[c+d x]^3}{40 d \sqrt{a+a \sin [c+d x]}}+\frac{\operatorname{Sec}[c+d x]^5}{5 d \sqrt{a+a \sin [c+d x]}}$$

Result (type 3, 140 leaves):

$$\left(\left(3465+3465 i\right)\left(-1\right)^{3 / 4} \operatorname{ArcTanh}\left[\left(\frac{1}{2}+\frac{i}{2}\right)\left(-1\right)^{3 / 4}\left(-1+\operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]\right)\right]\right)\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)+\frac{1}{16} \operatorname{Sec}[c+d x]^5\left(11090+11352 \operatorname{Cos}[2(c+d x)]+2310 \operatorname{Cos}[4(c+d x)]+36850 \operatorname{Sin}[c+d x]+17787 \operatorname{Sin}[3(c+d x)]+3465 \operatorname{Sin}[5(c+d x)]\right)\left(7680 d \sqrt{a(1+\operatorname{Sin}[c+d x])}\right) /$$

Problem 172: Result more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Cos}[c+d x]^4}{(a+a \sin [c+d x])^{3 / 2}} d x$$

Optimal (type 3, 30 leaves, 1 step):

$$-\frac{2 a \operatorname{Cos}[c+d x]^5}{5 d (a+a \operatorname{Sin}[c+d x])^{5/2}}$$

Result (type 3, 69 leaves):

$$-\left(\left(2 \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) \right)^5 \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^3 \right) / \left(5 d (a (1 + \operatorname{Sin}[c+d x]))^{3/2} \right)$$

Problem 174: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Cos}[c+d x]^2}{(a+a \operatorname{Sin}[c+d x])^{3/2}} dx$$

Optimal (type 3, 76 leaves, 3 steps):

$$-\frac{2 \sqrt{2} \operatorname{ArcTanh}\left[\frac{\sqrt{a} \operatorname{Cos}[c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sin}[c+d x]}}\right]}{a^{3/2} d} + \frac{2 \operatorname{Cos}[c+d x]}{a d \sqrt{a+a \operatorname{Sin}[c+d x]}}$$

Result (type 3, 100 leaves):

$$\left(2 \left((2+2i) (-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]\right)\right] + \operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^3 \right) / \left(d (a (1 + \operatorname{Sin}[c+d x]))^{3/2} \right)$$

Problem 176: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Sec}[c+d x]}{(a+a \operatorname{Sin}[c+d x])^{3/2}} dx$$

Optimal (type 3, 89 leaves, 5 steps):

$$\frac{\operatorname{ArcTanh}\left[\frac{\sqrt{a+a \operatorname{Sin}[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{2 \sqrt{2} a^{3/2} d} - \frac{1}{3 d (a+a \operatorname{Sin}[c+d x])^{3/2}} - \frac{1}{2 a d \sqrt{a+a \operatorname{Sin}[c+d x]}}$$

Result (type 3, 106 leaves):

$$\left(-2 - 3 \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^2 - (3+3i) (-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]\right)\right] \right) \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^3 / \left(6 d (a (1 + \operatorname{Sin}[c+d x]))^{3/2} \right)$$

Problem 177: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Sec}[c + d x]^2}{(a + a \operatorname{Sin}[c + d x])^{3/2}} dx$$

Optimal (type 3, 134 leaves, 5 steps):

$$\frac{15 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \operatorname{Cos}[c+d x]}{\sqrt{2} \sqrt{a+a \operatorname{Sin}[c+d x]}}\right]}{32 \sqrt{2} a^{3/2} d} - \frac{15 \operatorname{Cos}[c+d x]}{32 d (a+a \operatorname{Sin}[c+d x])^{3/2}} - \frac{\operatorname{Sec}[c+d x]}{4 d (a+a \operatorname{Sin}[c+d x])^{3/2}} + \frac{5 \operatorname{Sec}[c+d x]}{8 a d \sqrt{a+a \operatorname{Sin}[c+d x]}}$$

Result (type 3, 224 leaves):

$$\left(-4 + \frac{8 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]}{\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]} + 14 \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right) - 7 \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^2 + (15 + 15 i) (-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]\right)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^3 + \frac{8 \left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right] \right)^3}{\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]} \right) / \left(32 d (a (1 + \operatorname{Sin}[c+d x]))^{3/2} \right)$$

Problem 178: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Sec}[c + d x]^3}{(a + a \operatorname{Sin}[c + d x])^{3/2}} dx$$

Optimal (type 3, 150 leaves, 7 steps):

$$\frac{7 \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \operatorname{Sin}[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{16 \sqrt{2} a^{3/2} d} - \frac{7}{24 d (a+a \operatorname{Sin}[c+d x])^{3/2}} - \frac{\operatorname{Sec}[c+d x]^2}{5 d (a+a \operatorname{Sin}[c+d x])^{3/2}} - \frac{7}{16 a d \sqrt{a+a \operatorname{Sin}[c+d x]}} + \frac{7 \operatorname{Sec}[c+d x]^2}{20 a d \sqrt{a+a \operatorname{Sin}[c+d x]}}$$

Result (type 3, 241 leaves):

$$\left(-40 - \frac{24}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^2} - 90 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 - \right. \\ \left. (105 + 105i) (-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \tan\left[\frac{1}{4}(c+dx)\right]\right)\right] \right) \\ \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 + \frac{15 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}{\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]} + \\ \left. \frac{30 \sin\left[\frac{1}{2}(c+dx)\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}{\left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^2} \right) / \left(240 d (a (1 + \sin[c+dx]))^{3/2} \right)$$

Problem 179: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\sec[c+dx]^4}{(a+a\sin[c+dx])^{3/2}} dx$$

Optimal (type 3, 195 leaves, 7 steps):

$$-\frac{105 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{2} \sqrt{a+a\sin[c+dx]}}\right]}{256 \sqrt{2} a^{3/2} d} - \frac{105 \cos[c+dx]}{256 d (a+a\sin[c+dx])^{3/2}} - \frac{7 \sec[c+dx]}{32 d (a+a\sin[c+dx])^{3/2}} - \\ \frac{\sec[c+dx]^3}{6 d (a+a\sin[c+dx])^{3/2}} + \frac{35 \sec[c+dx]}{64 a d \sqrt{a+a\sin[c+dx]}} + \frac{\sec[c+dx]^3}{4 a d \sqrt{a+a\sin[c+dx]}}$$

Result (type 3, 334 leaves):

$$\frac{1}{768 d (a (1 + \sin[c+dx]))^{3/2}} \left(-68 + \frac{64 \sin\left[\frac{1}{2}(c+dx)\right]}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3} - \right. \\ \left. \frac{32}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^2} + \frac{136 \sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]} + \right. \\ \left. 246 \sin\left[\frac{1}{2}(c+dx)\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) - \right. \\ \left. 123 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 + (315 + 315i) (-1)^{3/4} \right. \\ \left. \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \tan\left[\frac{1}{4}(c+dx)\right]\right)\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 + \right. \\ \left. \frac{32 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}{\left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^3} + \frac{192 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}{\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]} \right)$$

Problem 180: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Sec}[c + d x]^5}{(a + a \operatorname{Sin}[c + d x])^{3/2}} dx$$

Optimal (type 3, 211 leaves, 9 steps):

$$\frac{99 \operatorname{ArcTanh}\left[\frac{\sqrt{a+a \operatorname{Sin}[c+d x]}}{\sqrt{2} \sqrt{a}}\right]}{256 \sqrt{2} a^{3/2} d} - \frac{33}{128 d (a + a \operatorname{Sin}[c + d x])^{3/2}} - \frac{99 \operatorname{Sec}[c + d x]^2}{560 d (a + a \operatorname{Sin}[c + d x])^{3/2}} - \frac{\operatorname{Sec}[c + d x]^4}{7 d (a + a \operatorname{Sin}[c + d x])^{3/2}} - \frac{99}{256 a d \sqrt{a + a \operatorname{Sin}[c + d x]}} + \frac{99 \operatorname{Sec}[c + d x]^2}{320 a d \sqrt{a + a \operatorname{Sin}[c + d x]}} + \frac{11 \operatorname{Sec}[c + d x]^4}{56 a d \sqrt{a + a \operatorname{Sin}[c + d x]}}$$

Result (type 3, 376 leaves):

$$\frac{1}{8960 d (a (1 + \operatorname{Sin}[c + d x]))^{3/2}} \left(-1120 - \frac{320}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} - \frac{672}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} - 2800 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2 - (3465 + 3465 i) (-1)^{1/4} \operatorname{ArcTan}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{1/4} \left(1 + \operatorname{Tan}\left[\frac{1}{4}(c + d x)\right]\right)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^3 + \frac{140 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^3}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^3} + \frac{665 \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^3}{\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]} + \frac{280 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^3}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} + \frac{1330 \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^3}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} \right)$$

Problem 181: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Sec}[c + d x]^6}{(a + a \operatorname{Sin}[c + d x])^{3/2}} dx$$

Optimal (type 3, 256 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{3003 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{2} \sqrt{a+a \sin[c+dx]}}\right]}{8192 \sqrt{2} a^{3/2} d} - \frac{3003 \cos[c+dx]}{8192 d (a+a \sin[c+dx])^{3/2}} - \\
 & \frac{1001 \sec[c+dx]}{5120 d (a+a \sin[c+dx])^{3/2}} - \frac{143 \sec[c+dx]^3}{960 d (a+a \sin[c+dx])^{3/2}} - \frac{\sec[c+dx]^5}{8 d (a+a \sin[c+dx])^{3/2}} + \\
 & \frac{1001 \sec[c+dx]}{2048 a d \sqrt{a+a \sin[c+dx]}} + \frac{143 \sec[c+dx]^3}{640 a d \sqrt{a+a \sin[c+dx]}} + \frac{13 \sec[c+dx]^5}{80 a d \sqrt{a+a \sin[c+dx]}}
 \end{aligned}$$

Result (type 3, 444 leaves):

$$\begin{aligned}
 & \frac{1}{122880 d (a(1+\sin[c+dx]))^{3/2}} \\
 & \left(-8860 + \frac{3840 \sin\left[\frac{1}{2}(c+dx)\right]}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^5} - \frac{1920}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^4} + \right. \\
 & \frac{9920 \sin\left[\frac{1}{2}(c+dx)\right]}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{4960}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + \\
 & \frac{17720 \sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]} + 32490 \sin\left[\frac{1}{2}(c+dx)\right] \\
 & \left. \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) - 16245 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 + \right. \\
 & \left. (45045 + 45045 i) (-1)^{3/4} \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \tan\left[\frac{1}{4}(c+dx)\right]\right)\right] \right) \\
 & \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 + \frac{1536 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}{\left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^5} + \\
 & \left. \frac{6400 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}{\left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right)^3} + \frac{28800 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3}{\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]} \right)
 \end{aligned}$$

Problem 182: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx]^{10}}{(a+a \sin[c+dx])^{5/2}} dx$$

Optimal (type 3, 95 leaves, 3 steps):

$$- \frac{64 a^3 \cos[c+dx]^{11}}{2145 d (a+a \sin[c+dx])^{11/2}} - \frac{16 a^2 \cos[c+dx]^{11}}{195 d (a+a \sin[c+dx])^{9/2}} - \frac{2 a \cos[c+dx]^{11}}{15 d (a+a \sin[c+dx])^{7/2}}$$

Result (type 3, 865 leaves):

$$\begin{aligned}
& - \frac{45 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{64 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{65 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{192 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{\operatorname{Cos}\left[\frac{5}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{320 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{5 \operatorname{Cos}\left[\frac{7}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{64 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{5 \operatorname{Cos}\left[\frac{9}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{192 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{5 \operatorname{Cos}\left[\frac{11}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{704 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{5 \operatorname{Cos}\left[\frac{13}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{832 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} - \\
& \frac{\operatorname{Cos}\left[\frac{15}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{960 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{45 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{64 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{65 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5 \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right]}{192 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} - \\
& \frac{\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5 \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]}{320 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{5 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5 \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right]}{64 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} - \\
& \frac{5 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5 \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right]}{192 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{5 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5 \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right]}{704 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} - \\
& \frac{5 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5 \operatorname{Sin}\left[\frac{13}{2}(c+dx)\right]}{832 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} -
\end{aligned}$$

$$\frac{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^5 \sin\left[\frac{15}{2}(c+dx)\right]}{960 d \left(a \left(1 + \sin[c+dx]\right)\right)^{5/2}}$$

Problem 183: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos[c+dx]^9}{(a+a\sin[c+dx])^{5/2}} dx$$

Optimal (type 3, 121 leaves, 3 steps):

$$\frac{32 (a+a\sin[c+dx])^{5/2}}{5 a^5 d} - \frac{64 (a+a\sin[c+dx])^{7/2}}{7 a^6 d} + \frac{16 (a+a\sin[c+dx])^{9/2}}{3 a^7 d} - \frac{16 (a+a\sin[c+dx])^{11/2}}{11 a^8 d} + \frac{2 (a+a\sin[c+dx])^{13/2}}{13 a^9 d}$$

Result (type 3, 757 leaves):

$$\begin{aligned}
& \frac{9 \operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{8 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} - \\
& \frac{3 \operatorname{Cos}\left[\frac{3}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{32 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{29 \operatorname{Cos}\left[\frac{5}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{160 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{5 \operatorname{Cos}\left[\frac{7}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{112 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{\operatorname{Cos}\left[\frac{9}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{48 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{5 \operatorname{Cos}\left[\frac{11}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{352 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} - \\
& \frac{\operatorname{Cos}\left[\frac{13}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{416 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{9 \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right] \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5}{8 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{3 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5 \operatorname{Sin}\left[\frac{3}{2}(c+dx)\right]}{32 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{29 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5 \operatorname{Sin}\left[\frac{5}{2}(c+dx)\right]}{160 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} - \\
& \frac{5 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5 \operatorname{Sin}\left[\frac{7}{2}(c+dx)\right]}{112 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} + \\
& \frac{\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5 \operatorname{Sin}\left[\frac{9}{2}(c+dx)\right]}{48 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} - \\
& \frac{5 \left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5 \operatorname{Sin}\left[\frac{11}{2}(c+dx)\right]}{352 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}} - \\
& \frac{\left(\operatorname{Cos}\left[\frac{1}{2}(c+dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c+dx)\right]\right)^5 \operatorname{Sin}\left[\frac{13}{2}(c+dx)\right]}{416 d (a (1 + \operatorname{Sin}[c+dx]))^{5/2}}
\end{aligned}$$

Problem 186: Result more than twice size of optimal antiderivative.

$$\int \frac{\cos [c+d x]^6}{(a+a \sin [c+d x])^{5/2}} d x$$

Optimal (type 3, 30 leaves, 1 step):

$$-\frac{2 a \cos [c+d x]^7}{7 d (a+a \sin [c+d x])^{7/2}}$$

Result (type 3, 69 leaves):

$$-\left(\left(2 \left(\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right) \right)^7 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^5 \right) / \left(7 d (a (1 + \sin [c+d x]))^{5/2} \right)$$

Problem 188: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [c+d x]^4}{(a+a \sin [c+d x])^{5/2}} d x$$

Optimal (type 3, 108 leaves, 4 steps):

$$-\frac{4 \sqrt{2} \operatorname{ArcTanh} \left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}} \right]}{a^{5/2} d} + \frac{2 \cos [c+d x]^3}{3 a d (a+a \sin [c+d x])^{3/2}} + \frac{4 \cos [c+d x]}{a^2 d \sqrt{a+a \sin [c+d x]}}$$

Result (type 3, 128 leaves):

$$\left(\left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right) \right)^5 \left((24+24 i) (-1)^{3/4} \operatorname{ArcTanh} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left(-1 + \tan \left[\frac{1}{4} (c+d x) \right] \right) \right] + 15 \cos \left[\frac{1}{2} (c+d x) \right] - \cos \left[\frac{3}{2} (c+d x) \right] - 15 \sin \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{3}{2} (c+d x) \right] \right) / \left(3 d (a (1 + \sin [c+d x]))^{5/2} \right)$$

Problem 190: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\cos [c+d x]^2}{(a+a \sin [c+d x])^{5/2}} d x$$

Optimal (type 3, 75 leaves, 3 steps):

$$\frac{\operatorname{ArcTanh} \left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}} \right]}{\sqrt{2} a^{5/2} d} - \frac{\cos [c+d x]}{a d (a+a \sin [c+d x])^{3/2}}$$

Result (type 3, 108 leaves):

$$- \left(\left(\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 \right. \right. \\ \left. \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] + (1 + i) (-1)^{3/4} \operatorname{ArcTanh} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \right. \right. \right. \\ \left. \left. \left. \left(-1 + \tan \left[\frac{1}{4} (c + d x) \right] \right) \right) (1 + \sin [c + d x]) \right) \right) \right) / \left(d (a (1 + \sin [c + d x]))^{5/2} \right)$$

Problem 192: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Sec}[c + d x]}{(a + a \sin [c + d x])^{5/2}} dx$$

Optimal (type 3, 113 leaves, 6 steps):

$$\frac{\operatorname{ArcTanh} \left[\frac{\sqrt{a+a \sin [c+d x]}}{\sqrt{2} \sqrt{a}} \right]}{4 \sqrt{2} a^{5/2} d} - \frac{1}{5 d (a + a \sin [c + d x])^{5/2}} - \\ \frac{1}{6 a d (a + a \sin [c + d x])^{3/2}} - \frac{1}{4 a^2 d \sqrt{a + a \sin [c + d x]}}$$

Result (type 3, 131 leaves):

$$\left(-12 - 10 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 - 15 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 - \right. \\ \left. (15 + 15 i) (-1)^{1/4} \operatorname{ArcTan} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \left(1 + \tan \left[\frac{1}{4} (c + d x) \right] \right) \right] \right) \\ \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^5 \right) / \left(60 d (a (1 + \sin [c + d x]))^{5/2} \right)$$

Problem 193: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Sec}[c + d x]^2}{(a + a \sin [c + d x])^{5/2}} dx$$

Optimal (type 3, 167 leaves, 6 steps):

$$\frac{35 \operatorname{ArcTanh} \left[\frac{\sqrt{a} \cos [c+d x]}{\sqrt{2} \sqrt{a+a \sin [c+d x]}} \right]}{128 \sqrt{2} a^{5/2} d} - \frac{\operatorname{Sec}[c + d x]}{6 d (a + a \sin [c + d x])^{5/2}} - \\ \frac{35 \cos [c + d x]}{128 a d (a + a \sin [c + d x])^{3/2}} - \frac{7 \operatorname{Sec}[c + d x]}{48 a d (a + a \sin [c + d x])^{3/2}} + \frac{35 \operatorname{Sec}[c + d x]}{96 a^2 d \sqrt{a + a \sin [c + d x]}}$$

Result (type 3, 284 leaves):

$$\frac{1}{384 d (a (1 + \sin [c + d x]))^{5/2}} \left(-32 + \frac{64 \sin \left[\frac{1}{2} (c + d x) \right]}{\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right]} + \right.$$

$$88 \sin \left[\frac{1}{2} (c + d x) \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) -$$

$$44 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 + 114 \sin \left[\frac{1}{2} (c + d x) \right]$$

$$\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 - 57 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 +$$

$$(105 + 105 i) (-1)^{3/4} \operatorname{ArcTanh} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{3/4} \left(-1 + \tan \left[\frac{1}{4} (c + d x) \right] \right) \right]$$

$$\left. \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^5 + \frac{48 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^5}{\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right]} \right)$$

Problem 194: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\sec [c + d x]^3}{(a + a \sin [c + d x])^{5/2}} dx$$

Optimal (type 3, 185 leaves, 8 steps):

$$\frac{9 \operatorname{ArcTanh} \left[\frac{\sqrt{a + a \sin [c + d x]}}{\sqrt{2} \sqrt{a}} \right]}{32 \sqrt{2} a^{5/2} d} - \frac{\sec [c + d x]^2}{7 d (a + a \sin [c + d x])^{5/2}} - \frac{3}{16 a d (a + a \sin [c + d x])^{3/2}}$$

$$\frac{9 \sec [c + d x]^2}{70 a d (a + a \sin [c + d x])^{3/2}} - \frac{9}{32 a^2 d \sqrt{a + a \sin [c + d x]}} + \frac{9 \sec [c + d x]^2}{40 a^2 d \sqrt{a + a \sin [c + d x]}}$$

Result (type 3, 266 leaves):

$$\frac{1}{1120 d (a (1 + \sin [c + d x]))^{5/2}} \left(-112 - \frac{80}{\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} - \right.$$

$$140 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 - 280 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 -$$

$$(315 + 315 i) (-1)^{1/4} \operatorname{ArcTan} \left[\left(\frac{1}{2} + \frac{i}{2} \right) (-1)^{1/4} \left(1 + \tan \left[\frac{1}{4} (c + d x) \right] \right) \right]$$

$$\left. \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^5 + \frac{35 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^5}{\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right]} + \right.$$

$$\left. \frac{70 \sin \left[\frac{1}{2} (c + d x) \right] \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^5}{\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2} \right)$$

Problem 195: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\operatorname{Sec}[c+dx]^4}{(a+a\sin[c+dx])^{5/2}} dx$$

Optimal (type 3, 233 leaves, 8 steps):

$$\begin{aligned} & \frac{1155 \operatorname{ArcTanh}\left[\frac{\sqrt{a} \cos[c+dx]}{\sqrt{2} \sqrt{a+a\sin[c+dx]}}\right]}{4096 \sqrt{2} a^{5/2} d} - \frac{\operatorname{Sec}[c+dx]^3}{8 d (a+a\sin[c+dx])^{5/2}} - \\ & \frac{1155 \cos[c+dx]}{4096 a d (a+a\sin[c+dx])^{3/2}} - \frac{77 \operatorname{Sec}[c+dx]}{512 a d (a+a\sin[c+dx])^{3/2}} - \\ & \frac{11 \operatorname{Sec}[c+dx]^3}{96 a d (a+a\sin[c+dx])^{3/2}} + \frac{385 \operatorname{Sec}[c+dx]}{1024 a^2 d \sqrt{a+a\sin[c+dx]}} + \frac{11 \operatorname{Sec}[c+dx]^3}{64 a^2 d \sqrt{a+a\sin[c+dx]}} \end{aligned}$$

Result (type 3, 394 leaves):

$$\begin{aligned} & \frac{1}{12288 d (a(1+\sin[c+dx]))^{5/2}} \\ & \left(-736 + \frac{768 \sin\left[\frac{1}{2}(c+dx)\right]}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} - \frac{384}{\left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2} + \right. \\ & \frac{1472 \sin\left[\frac{1}{2}(c+dx)\right]}{\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]} + 2072 \sin\left[\frac{1}{2}(c+dx)\right] \\ & \left. \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right) - 1036 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^2 + \right. \\ & 3090 \sin\left[\frac{1}{2}(c+dx)\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^3 - \\ & 1545 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^4 + (3465 + 3465 i) (-1)^{3/4} \\ & \left. \operatorname{ArcTanh}\left[\left(\frac{1}{2} + \frac{i}{2}\right) (-1)^{3/4} \left(-1 + \tan\left[\frac{1}{4}(c+dx)\right]\right)\right] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^5 + \right. \\ & \left. \frac{256 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^5}{\left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]\right)^3} + \frac{1920 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right]\right)^5}{\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right]} \right) \end{aligned}$$

Problem 197: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (e \cos[c+dx])^{5/2} (a+a\sin[c+dx]) dx$$

Optimal (type 4, 95 leaves, 4 steps):

$$-\frac{2 a (e \cos [c+d x])^{7/2}}{7 d e} + \frac{6 a e^2 \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5 d \sqrt{\cos [c+d x]}} + \frac{2 a e (e \cos [c+d x])^{3/2} \sin [c+d x]}{5 d}$$

Result (type 5, 264 leaves):

$$\frac{1}{560 d \sqrt{e \cos [c+d x]}} a e^3 \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \left(-154 \cos [d x] - 182 \cos [2 c+d x] + 14 \cos [2 c+3 d x] - 14 \cos [4 c+3 d x] - 30 \sin [c] + 168 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] (\cos [d x] - i \sin [d x]) \sqrt{1 + \cos [2(c+d x)] + i \sin [2(c+d x)]} + 56 \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] (\cos [d x] + i \sin [d x]) \sqrt{1 + \cos [2(c+d x)] + i \sin [2(c+d x)]} + 20 \sin [c+2 d x] - 20 \sin [3 c+2 d x] + 5 \sin [3 c+4 d x] - 5 \sin [5 c+4 d x] \right)$$

Problem 199: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sqrt{e \cos [c+d x]} (a + a \sin [c+d x]) dx$$

Optimal (type 4, 63 leaves, 3 steps):

$$-\frac{2 a (e \cos [c+d x])^{3/2}}{3 d e} + \frac{2 a \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{d \sqrt{\cos [c+d x]}}$$

Result (type 5, 260 leaves):

$$\frac{1}{6 d \left((1 + e^{2 i d x}) \cos [c] + i (-1 + e^{2 i d x}) \sin [c] \right)} a \sqrt{e \cos [c+d x]} \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] (\cos [d x] + i \sin [d x]) \left(-6 \cos [d x] - 6 \cos [2 c+d x] - 2 \sin [c] + 6 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] (\cos [d x] - i \sin [d x]) \sqrt{1 + \cos [2(c+d x)] + i \sin [2(c+d x)]} + 2 \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2 i d x} (\cos [c] + i \sin [c])^2\right] (\cos [d x] + i \sin [d x]) \sqrt{1 + \cos [2(c+d x)] + i \sin [2(c+d x)]} + \sin [c+2 d x] - \sin [3 c+2 d x] \right)$$

Problem 201: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{a + a \sin[c + dx]}{(e \cos[c + dx])^{3/2}} dx$$

Optimal (type 4, 91 leaves, 4 steps):

$$\frac{2a}{de \sqrt{e \cos[c + dx]}} - \frac{2a \sqrt{e \cos[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{de^2 \sqrt{\cos[c + dx]}} + \frac{2a \sin[c + dx]}{de \sqrt{e \cos[c + dx]}}$$

Result (type 5, 188 leaves):

$$\begin{aligned} & -\frac{1}{6de \sqrt{e \cos[c + dx]}} a \operatorname{Csc}\left[\frac{c}{2}\right] \operatorname{Sec}\left[\frac{c}{2}\right] \\ & \left(-6(\cos[dx] + \sin[c]) + 3 \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i dx} (\cos[c] + i \sin[c])^2\right] \right. \\ & \quad \left. (\cos[dx] - i \sin[dx]) \sqrt{1 + \cos[2(c + dx)] + i \sin[2(c + dx)]} + \right. \\ & \quad \left. \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{3}{4}, \frac{7}{4}, -e^{2i dx} (\cos[c] + i \sin[c])^2\right] \right. \\ & \quad \left. (\cos[dx] + i \sin[dx]) \sqrt{1 + \cos[2(c + dx)] + i \sin[2(c + dx)]} \right) \end{aligned}$$

Problem 203: Result unnecessarily involves higher level functions.

$$\int \frac{a + a \sin[c + dx]}{(e \cos[c + dx])^{7/2}} dx$$

Optimal (type 4, 126 leaves, 5 steps):

$$\begin{aligned} & \frac{2a}{5de (e \cos[c + dx])^{5/2}} - \frac{6a \sqrt{e \cos[c + dx]} \operatorname{EllipticE}\left[\frac{1}{2}(c + dx), 2\right]}{5de^4 \sqrt{\cos[c + dx]}} + \\ & \frac{2a \sin[c + dx]}{5de (e \cos[c + dx])^{5/2}} + \frac{6a \sin[c + dx]}{5de^3 \sqrt{e \cos[c + dx]}} \end{aligned}$$

Result (type 5, 160 leaves):

$$\begin{aligned} & \left(2a \sqrt{e \cos[c + dx]} (\cos[c + dx] - i \sin[c + dx]) \left(3i + \cos[c + dx] + 3i \sqrt{1 + e^{2i(c + dx)}} \right. \right. \\ & \quad \left. \left. \operatorname{Hypergeometric2F1}\left[-\frac{1}{4}, \frac{1}{2}, \frac{3}{4}, -e^{2i(c + dx)}\right] (-1 + \sin[c + dx]) - 2i \sin[c + dx] \right) \right) / \\ & \left(5de^4 \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^3 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right) \right) \end{aligned}$$

Problem 210: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[c + dx])^2}{(e \cos[c + dx])^{5/2}} dx$$

Optimal (type 4, 89 leaves, 4 steps):

$$-\frac{2 a^2 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3 d e^2 \sqrt{e \cos [c+d x]}}+\frac{4 a^4 \sqrt{e \cos [c+d x]}}{3 d e^3\left(a^2-a^2 \sin [c+d x]\right)}$$

Result (type 4, 1198 leaves):

$$\frac{\cos [c+d x]^3\left(-\frac{2}{3}+\frac{4}{3\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^2}\right)\left(a+a \sin [c+d x]\right)^2}{d\left(e \cos [c+d x]\right)^{5 / 2}\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^4}+$$

$$\left(2 \cos [c+d x]^2\left(-\frac{\cos \left[\frac{1}{2}(c+d x)\right] \sqrt{\cos [c+d x]}}{3\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)}-\frac{\sqrt{\cos [c+d x]} \sin \left[\frac{1}{2}(c+d x)\right]}{3\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)}\right)\left(a+a \sin [c+d x]\right)^2\right.$$

$$\left.\left(\cos [c+d x]-2 \sqrt{2} \cos \left[\frac{1}{4}(c+d x)\right]\right)^2 \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}}\right.$$

$$\left.\left.\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}\right)\right) /$$

$$\left(3 d\left(e \cos [c+d x]\right)^{5 / 2}\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^4\right.$$

$$\left.\left(\left(\sin [c+d x]\left(\cos [c+d x]-2 \sqrt{2} \cos \left[\frac{1}{4}(c+d x)\right]\right)^2 \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}}\right.\right.\right.$$

$$\left.\left.\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}\right)\right) / \left(3 \cos [c+d x]^{3 / 2}\right)+$$

$$\frac{1}{3 \sqrt{\cos [c+d x]}} 2\left(-\sin [c+d x]+\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}}\right)$$

$$\begin{aligned}
 & \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\text{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \text{Tan}\left[\frac{1}{4}(c+dx)\right]\right) / \\
 & \left(\sqrt{2} \sqrt{3-2\sqrt{2} - \text{Tan}\left[\frac{1}{4}(c+dx)\right]^2} + \sqrt{2} \text{Cos}\left[\frac{1}{4}(c+dx)\right] \right. \\
 & \left. \sqrt{\frac{-1+\sqrt{2} - (-2+\sqrt{2}) \text{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\text{Cos}\left[\frac{1}{2}(c+dx)\right]}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\text{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], \right. \right. \\
 & \left. \left. 17-12\sqrt{2}\right] \text{Sin}\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2} - \text{Tan}\left[\frac{1}{4}(c+dx)\right]^2} - \right. \\
 & \left. \left(\sqrt{2} \text{Cos}\left[\frac{1}{4}(c+dx)\right]^2 \text{EllipticF}\left[\text{ArcSin}\left[\frac{\text{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right. \right. \\
 & \left. \left. \left(\frac{(-2+\sqrt{2}) \text{Sin}\left[\frac{1}{2}(c+dx)\right]}{2(1+\text{Cos}\left[\frac{1}{2}(c+dx)\right])} + \left((-1+\sqrt{2} - (-2+\sqrt{2}) \text{Cos}\left[\frac{1}{2}(c+dx)\right]) \right. \right. \right. \right. \\
 & \left. \left. \left. \text{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) / \left(2 \left(1 + \text{Cos}\left[\frac{1}{2}(c+dx)\right] \right)^2 \right) \right) \\
 & \left. \sqrt{3-2\sqrt{2} - \text{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) / \left(\sqrt{\frac{-1+\sqrt{2} - (-2+\sqrt{2}) \text{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\text{Cos}\left[\frac{1}{2}(c+dx)\right]}} \right) - \\
 & \left(\sqrt{\frac{-1+\sqrt{2} - (-2+\sqrt{2}) \text{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\text{Cos}\left[\frac{1}{2}(c+dx)\right]}} \sqrt{3-2\sqrt{2} - \text{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) / \\
 & \left(\sqrt{2(3-2\sqrt{2})} \sqrt{1 - \frac{\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \sqrt{1 - \frac{(17-12\sqrt{2}) \text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \right) \right) \right)
 \end{aligned}$$

Problem 212: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \text{Sin}[c + dx])^2}{(e \text{Cos}[c + dx])^{9/2}} dx$$

Optimal (type 4, 114 leaves, 4 steps):

$$\frac{2 a^2 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{7 d e^4 \sqrt{e \cos [c+d x]}} + \frac{2 a^2 \sin [c+d x]}{7 d e^3 (e \cos [c+d x])^{3/2}} + \frac{4 (a^2 + a^2 \sin [c+d x])}{7 d e (e \cos [c+d x])^{7/2}}$$

Result (type 4, 1227 leaves):

$$\left(\cos [c+d x]^5 \right. \\ \left. \left(\frac{2}{7} + \frac{2}{7 \left(\cos \left[\frac{1}{2}(c+d x) \right] - \sin \left[\frac{1}{2}(c+d x) \right] \right)^4} + \frac{2}{7 \left(\cos \left[\frac{1}{2}(c+d x) \right] - \sin \left[\frac{1}{2}(c+d x) \right] \right)^2} \right) \right. \\ \left. (a + a \sin [c+d x])^2 \right) / \left(d (e \cos [c+d x])^{9/2} \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^4 \right) - \\ \left(2 \cos [c+d x]^4 \left(\frac{\cos \left[\frac{1}{2}(c+d x) \right] \sqrt{\cos [c+d x]}}{7 \left(\cos \left[\frac{1}{2}(c+d x) \right] - \sin \left[\frac{1}{2}(c+d x) \right] \right)} + \frac{\sqrt{\cos [c+d x]} \sin \left[\frac{1}{2}(c+d x) \right]}{7 \left(\cos \left[\frac{1}{2}(c+d x) \right] - \sin \left[\frac{1}{2}(c+d x) \right] \right)} \right) \right. \\ \left. (a + a \sin [c+d x])^2 \right. \\ \left. \left(\cos [c+d x] - 2 \sqrt{2} \cos \left[\frac{1}{4}(c+d x) \right] \right)^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2}(c+d x) \right]}{1 + \cos \left[\frac{1}{2}(c+d x) \right]}} \right. \\ \left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x) \right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4}(c+d x) \right]^2} \right] \right) \right) / \\ \left(7 d (e \cos [c+d x])^{9/2} \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^4 \right. \\ \left. \left(- \left(\left(\sin [c+d x] \left(\cos [c+d x] - 2 \sqrt{2} \cos \left[\frac{1}{4}(c+d x) \right] \right)^2 \right. \right. \right. \right. \\ \left. \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2}(c+d x) \right]}{1 + \cos \left[\frac{1}{2}(c+d x) \right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x) \right]}{\sqrt{3 - 2 \sqrt{2}}}\right], \right. \right. \right. \\ \left. \left. \left. 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4}(c+d x) \right]^2} \right) \right) \right) / (7 \cos [c+d x]^{3/2}) \right) -$$

$$\begin{aligned}
& \frac{1}{7\sqrt{\cos[c+dx]}} 2 \left(-\sin[c+dx] + \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \right. \right. \\
& \quad \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \tan\left[\frac{1}{4}(c+dx)\right] \right) \right) / \\
& \quad \left(\sqrt{2} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} + \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] \right) \\
& \quad \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], \right. \\
& \quad \left. 17-12\sqrt{2}\right] \sin\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} - \\
& \quad \left(\sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right]^2 \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right. \\
& \quad \left. \left(\frac{(-2+\sqrt{2})\sin\left[\frac{1}{2}(c+dx)\right]}{2(1+\cos\left[\frac{1}{2}(c+dx)\right])} + \left((-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]) \right. \right. \right. \\
& \quad \left. \left. \left. \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \left(2(1+\cos\left[\frac{1}{2}(c+dx)\right])^2 \right) \right) \\
& \quad \left. \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \right) - \\
& \quad \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \\
& \quad \left(\sqrt{2(3-2\sqrt{2})} \sqrt{1-\frac{\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \sqrt{1-\frac{(17-12\sqrt{2})\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \right) \right) \right)
\end{aligned}$$

Problem 222: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[c + d x])^3}{(e \cos[c + d x])^{9/2}} dx$$

Optimal (type 4, 127 leaves, 5 steps):

$$-\frac{2 a^3 \sqrt{\cos[c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 d e^4 \sqrt{e \cos[c + d x]}} + \frac{4 a^5 \sqrt{e \cos[c + d x]}}{7 d e^5 (a - a \sin[c + d x])^2} - \frac{2 a^6 \sqrt{e \cos[c + d x]}}{21 d e^5 (a^3 - a^3 \sin[c + d x])}$$

Result (type 4, 1227 leaves):

$$\left(\cos[c + d x]^5 \left(-\frac{2}{21} + \frac{4}{7 \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right)^4} - \frac{2}{21 \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right)^2} \right) (a + a \sin[c + d x])^3 \right) / \left(d (e \cos[c + d x])^{9/2} \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^6 \right) + \left(2 \cos[c + d x]^4 \left(-\frac{\cos\left[\frac{1}{2}(c + d x)\right] \sqrt{\cos[c + d x]}}{21 \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right)} - \frac{\sqrt{\cos[c + d x]} \sin\left[\frac{1}{2}(c + d x)\right]}{21 \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right)} \right) (a + a \sin[c + d x])^3 \right) \left(\cos[c + d x] - 2 \sqrt{2} \cos\left[\frac{1}{4}(c + d x)\right]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + d x)\right]}{1 + \cos\left[\frac{1}{2}(c + d x)\right]}} \right) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2} - \tan\left[\frac{1}{4}(c + d x)\right]^2} \right) / \left(21 d (e \cos[c + d x])^{9/2} \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^6 \right) \left(\sin[c + d x] \left(\cos[c + d x] - 2 \sqrt{2} \cos\left[\frac{1}{4}(c + d x)\right]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + d x)\right]}{1 + \cos\left[\frac{1}{2}(c + d x)\right]}} \right) \right)$$

$$\begin{aligned}
& \text{EllipticF}\left[\text{ArcSin}\left[\frac{\text{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \\
& \left. \sqrt{3-2\sqrt{2}-\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}\right) \Big/ (21 \text{Cos}[c+dx]^{3/2}) + \\
& \frac{1}{21\sqrt{\text{Cos}[c+dx]}} 2 \left(-\text{Sin}[c+dx] + \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\text{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\text{Cos}\left[\frac{1}{2}(c+dx)\right]}} \right. \right. \\
& \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\text{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \text{Tan}\left[\frac{1}{4}(c+dx)\right] \right) \Big/ \right. \\
& \left. \left(\sqrt{2} \sqrt{3-2\sqrt{2}-\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2} + \sqrt{2} \text{Cos}\left[\frac{1}{4}(c+dx)\right] \right) \right. \\
& \left. \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\text{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\text{Cos}\left[\frac{1}{2}(c+dx)\right]}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\text{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], \right. \right. \\
& \left. \left. 17-12\sqrt{2}\right] \text{Sin}\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2}-\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2} - \right. \\
& \left. \left(\sqrt{2} \text{Cos}\left[\frac{1}{4}(c+dx)\right]^2 \text{EllipticF}\left[\text{ArcSin}\left[\frac{\text{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right. \right. \\
& \left. \left. \left(\frac{(-2+\sqrt{2})\text{Sin}\left[\frac{1}{2}(c+dx)\right]}{2(1+\text{Cos}\left[\frac{1}{2}(c+dx)\right])} + \left((-1+\sqrt{2}-(-2+\sqrt{2})\text{Cos}\left[\frac{1}{2}(c+dx)\right]) \right. \right. \right. \right. \\
& \left. \left. \left. \text{Sin}\left[\frac{1}{2}(c+dx)\right] \right) \right) \Big/ \left(2(1+\text{Cos}\left[\frac{1}{2}(c+dx)\right])^2 \right) \right) \Big/ \\
& \left. \sqrt{3-2\sqrt{2}-\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) \Big/ \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\text{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\text{Cos}\left[\frac{1}{2}(c+dx)\right]}} \right) - \\
& \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\text{Cos}\left[\frac{1}{2}(c+dx)\right]}{1+\text{Cos}\left[\frac{1}{2}(c+dx)\right]}} \sqrt{3-2\sqrt{2}-\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) \Big/
\end{aligned}$$

$$\left(\sqrt{2(3-2\sqrt{2})} \sqrt{1 - \frac{\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \sqrt{1 - \frac{(17-12\sqrt{2})\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \right) \right)$$

Problem 230: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[c + dx])^4}{(e \cos[c + dx])^{9/2}} dx$$

Optimal (type 4, 127 leaves, 5 steps):

$$\frac{10 a^4 \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{21 d e^4 \sqrt{e \cos[c + dx]}} + \frac{4 a^7 (e \cos[c + dx])^{5/2}}{7 d e^7 (a - a \sin[c + dx])^3} - \frac{20 a^8 \sqrt{e \cos[c + dx]}}{21 d e^5 (a^4 - a^4 \sin[c + dx])}$$

Result (type 4, 1227 leaves):

$$\left(\cos[c + dx]^5 \left(\frac{10}{21} + \frac{8}{7 \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^4} - \frac{32}{21 \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)^2} \right) (a + a \sin[c + dx])^4 \right) / \left(d (e \cos[c + dx])^{9/2} \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)^8 \right) - \left(10 \cos[c + dx]^4 \left(\frac{5 \cos\left[\frac{1}{2}(c + dx)\right] \sqrt{\cos[c + dx]}}{21 \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)} + \frac{5 \sqrt{\cos[c + dx]} \sin\left[\frac{1}{2}(c + dx)\right]}{21 \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right)} \right) (a + a \sin[c + dx])^4 \right) \left(\cos[c + dx] - 2\sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right] \right)^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) /$$

$$\begin{aligned}
& \left(21 d (e \cos [c + d x])^{9/2} \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^8 \right. \\
& \left. - \left(\left(5 \sin [c + d x] \left(\cos [c + d x] - 2 \sqrt{2} \cos \left[\frac{1}{4} (c + d x) \right] \right)^2 \right. \right. \right. \\
& \left. \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2} (c + d x) \right]}{1 + \cos \left[\frac{1}{2} (c + d x) \right]}} \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right] \right], \right. \right. \\
& \left. \left. 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} \right) \right) / (21 \cos [c + d x]^{3/2}) - \\
& \frac{1}{21 \sqrt{\cos [c + d x]}} 10 \left(-\sin [c + d x] + \left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2} (c + d x) \right]}{1 + \cos \left[\frac{1}{2} (c + d x) \right]}} \right. \right. \\
& \left. \left. \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right] \right], 17 - 12 \sqrt{2} \right] \tan \left[\frac{1}{4} (c + d x) \right] \right) \right) / \\
& \left(\sqrt{2} \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} + \sqrt{2} \cos \left[\frac{1}{4} (c + d x) \right] \right. \\
& \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2} (c + d x) \right]}{1 + \cos \left[\frac{1}{2} (c + d x) \right]}} \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right] \right], \right. \\
& \left. 17 - 12 \sqrt{2} \right] \sin \left[\frac{1}{4} (c + d x) \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} - \\
& \left(\sqrt{2} \cos \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right] \right], 17 - 12 \sqrt{2} \right] \\
& \left(\frac{(-2 + \sqrt{2}) \sin \left[\frac{1}{2} (c + d x) \right]}{2 \left(1 + \cos \left[\frac{1}{2} (c + d x) \right] \right)} + \left((-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2} (c + d x) \right] \right) \right. \\
& \left. \left. \sin \left[\frac{1}{2} (c + d x) \right] \right) \right) / \left(2 \left(1 + \cos \left[\frac{1}{2} (c + d x) \right] \right)^2 \right)
\end{aligned}$$

$$\left(\sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) / \left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right) -$$

$$\left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) /$$

$$\left(\sqrt{2(3 - 2\sqrt{2})} \sqrt{1 - \frac{\tan\left[\frac{1}{4}(c + dx)\right]^2}{3 - 2\sqrt{2}}} \sqrt{1 - \frac{(17 - 12\sqrt{2}) \tan\left[\frac{1}{4}(c + dx)\right]^2}{3 - 2\sqrt{2}}} \right) \right)$$

Problem 232: Result more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[c + dx])^4}{(e \cos[c + dx])^{13/2}} dx$$

Optimal (type 4, 169 leaves, 6 steps):

$$-\frac{2a^4 \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{77de^6 \sqrt{e \cos[c + dx]}} + \frac{4a^7 \sqrt{e \cos[c + dx]}}{11de^7 (a - a \sin[c + dx])^3} -$$

$$\frac{2a^8 \sqrt{e \cos[c + dx]}}{77de^7 (a^2 - a^2 \sin[c + dx])^2} - \frac{2a^8 \sqrt{e \cos[c + dx]}}{77de^7 (a^4 - a^4 \sin[c + dx])}$$

Result (type 4, 1256 leaves):

$$\left(\cos[c + dx]^7 \right.$$

$$\left(-\frac{2}{77} + \frac{4}{11 \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^6} - \frac{2}{77 \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^4} - \right.$$

$$\left. \frac{2}{77 \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)^2} \right) (a + a \sin[c + dx])^4 /$$

$$\left(d (e \cos[c + dx])^{13/2} \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^8 \right) +$$

$$\left(2 \cos[c + dx]^6 \left(-\frac{\cos\left[\frac{1}{2}(c + dx)\right] \sqrt{\cos[c + dx]}}{77 \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)} - \right.$$

$$\left. \frac{\sqrt{\cos[c + dx]} \sin\left[\frac{1}{2}(c + dx)\right]}{77 \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right)} \right) (a + a \sin[c + dx])^4$$

$$\left(\left(\cos [c+d x]-2 \sqrt{2} \cos \left[\frac{1}{4}(c+d x)\right]\right)^2 \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}} \right. \\ \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}\right)\right) /$$

$$\left(77 d (e \cos [c+d x])^{13 / 2} \left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^8 \right. \\ \left. \left(\left(\sin [c+d x] \left(\cos [c+d x]-2 \sqrt{2} \cos \left[\frac{1}{4}(c+d x)\right]\right)^2 \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}} \right. \right. \right. \\ \left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \right. \right. \right. \\ \left. \left. \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}\right)\right) / (77 \cos [c+d x]^{3 / 2}) + \right. \\ \left. \frac{1}{77 \sqrt{\cos [c+d x]}} 2 \left(-\sin [c+d x]+\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}} \right. \right. \\ \left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \tan \left[\frac{1}{4}(c+d x)\right]\right)\right) / \\ \left(\sqrt{2} \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}+\sqrt{2} \cos \left[\frac{1}{4}(c+d x)\right] \right. \\ \left. \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x)\right]}{1+\cos \left[\frac{1}{2}(c+d x)\right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], \right. \right. \\ \left. \left. 17-12 \sqrt{2}\right] \sin \left[\frac{1}{4}(c+d x)\right] \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}- \right. \\ \left. \left(\sqrt{2} \cos \left[\frac{1}{4}(c+d x)\right]\right)^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \right)$$

$$\left(\frac{(-2 + \sqrt{2}) \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]}{2 \left(1 + \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]\right)} + \left((-1 + \sqrt{2} - (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]) \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \right) / \left(2 \left(1 + \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]\right)^2 \right) \right) \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} / \left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]}{1 + \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]}} \right) - \left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]}{1 + \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]}} \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \right) / \left(\sqrt{2(3 - 2\sqrt{2})} \sqrt{1 - \frac{\operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{3 - 2\sqrt{2}}} \sqrt{1 - \frac{(17 - 12\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{3 - 2\sqrt{2}}} \right) \right)$$

Problem 237: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \operatorname{Cos}[c + dx])^{3/2}}{a + a \operatorname{Sin}[c + dx]} dx$$

Optimal (type 4, 66 leaves, 3 steps):

$$\frac{2 e \sqrt{e \operatorname{Cos}[c + dx]}}{a d} + \frac{2 e^2 \sqrt{\operatorname{Cos}[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{a d \sqrt{e \operatorname{Cos}[c + dx]}}$$

Result (type 4, 1089 leaves):

$$\left(2 (e \operatorname{Cos}[c + dx])^{3/2} \operatorname{Sec}[c + dx]^2 \left(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \right)^2 \right. \\ \left(\frac{\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] \sqrt{\operatorname{Cos}[c + dx]}}{\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]} - \frac{\sqrt{\operatorname{Cos}[c + dx]} \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]}{\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right]} \right) \\ \left(\operatorname{Cos}[c + dx] + 2\sqrt{2} \operatorname{Cos}\left[\frac{1}{4}(c + dx)\right]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]}{1 + \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right]}} \right. \\ \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \right) \right) /$$

$$\begin{aligned}
& \left(d (a + a \sin [c + d x]) \left(\frac{1}{\cos [c + d x]^{3/2}} \sin [c + d x] \right. \right. \\
& \left. \left(\cos [c + d x] + 2 \sqrt{2} \cos \left[\frac{1}{4} (c + d x) \right]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2} (c + d x) \right]}{1 + \cos \left[\frac{1}{2} (c + d x) \right]}} \right. \right. \\
& \left. \left. \text{EllipticF} \left[\text{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} \right) \right) + \\
& \frac{1}{\sqrt{\cos [c + d x]}} 2 \left(-\sin [c + d x] - \left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2} (c + d x) \right]}{1 + \cos \left[\frac{1}{2} (c + d x) \right]}} \right. \right. \\
& \left. \left. \text{EllipticF} \left[\text{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \tan \left[\frac{1}{4} (c + d x) \right] \right) \right) / \\
& \left(\sqrt{2} \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} - \sqrt{2} \cos \left[\frac{1}{4} (c + d x) \right] \right) \\
& \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2} (c + d x) \right]}{1 + \cos \left[\frac{1}{2} (c + d x) \right]}} \text{EllipticF} \left[\text{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], \right. \\
& \left. 17 - 12 \sqrt{2} \right] \sin \left[\frac{1}{4} (c + d x) \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} + \\
& \left(\sqrt{2} \cos \left[\frac{1}{4} (c + d x) \right]^2 \text{EllipticF} \left[\text{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right. \\
& \left. \left(\frac{(-2 + \sqrt{2}) \sin \left[\frac{1}{2} (c + d x) \right]}{2 (1 + \cos \left[\frac{1}{2} (c + d x) \right])} + \left((-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2} (c + d x) \right]) \right. \right. \right. \\
& \left. \left. \sin \left[\frac{1}{2} (c + d x) \right] \right) \right) / \left(2 (1 + \cos \left[\frac{1}{2} (c + d x) \right])^2 \right) \right) \\
& \left. \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} \right) / \left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2} (c + d x) \right]}{1 + \cos \left[\frac{1}{2} (c + d x) \right]}} \right) +
\end{aligned}$$

$$\left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]}{1 + \cos\left[\frac{1}{2}(c+dx)\right]}} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \left(\sqrt{2(3 - 2\sqrt{2})} \sqrt{1 - \frac{\tan\left[\frac{1}{4}(c+dx)\right]^2}{3 - 2\sqrt{2}}} \sqrt{1 - \frac{(17 - 12\sqrt{2}) \tan\left[\frac{1}{4}(c+dx)\right]^2}{3 - 2\sqrt{2}}} \right) \right)$$

Problem 239: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{e \cos[c+dx]} (a + a \sin[c+dx])} dx$$

Optimal (type 4, 78 leaves, 3 steps):

$$\frac{2 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{3 a d \sqrt{e \cos[c+dx]}} - \frac{2 \sqrt{e \cos[c+dx]}}{3 d e (a + a \sin[c+dx])}$$

Result (type 4, 1182 leaves):

$$\left(\cos[c+dx] \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 \left(-\frac{2}{3} - \frac{2}{3 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^2} \right) \right) / \left(d \sqrt{e \cos[c+dx]} (a + a \sin[c+dx]) \right) + \left(2 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 \left(\frac{\cos\left[\frac{1}{2}(c+dx)\right] \sqrt{\cos[c+dx]}}{3 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)} - \frac{\sqrt{\cos[c+dx]} \sin\left[\frac{1}{2}(c+dx)\right]}{3 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)} \right) \right) \left(\cos[c+dx] + 2\sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]}{1 + \cos\left[\frac{1}{2}(c+dx)\right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \right) \right) / \left(3 d \sqrt{e \cos[c+dx]} (a + a \sin[c+dx]) \left(\left(\sin[c+dx] \left(\cos[c+dx] + 2\sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right]^2 \right) \right) \right) \right)$$

$$\begin{aligned}
& \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], \right. \\
& \left. 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \Bigg) / (3 \cos[c + dx]^{3/2}) + \\
& \frac{1}{3\sqrt{\cos[c + dx]}} 2 \left(-\sin[c + dx] - \left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right. \right. \\
& \left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \tan\left[\frac{1}{4}(c + dx)\right] \right) / \right. \\
& \left. \left(\sqrt{2} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} - \sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right] \right) \right. \\
& \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], \right. \right. \\
& \left. \left. 17 - 12\sqrt{2}\right] \sin\left[\frac{1}{4}(c + dx)\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} + \right. \\
& \left. \left(\sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right. \right. \\
& \left. \left. \left(\frac{(-2 + \sqrt{2}) \sin\left[\frac{1}{2}(c + dx)\right]}{2(1 + \cos\left[\frac{1}{2}(c + dx)\right])} + \left((-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]) \right. \right. \right. \right. \\
& \left. \left. \left. \sin\left[\frac{1}{2}(c + dx)\right] \right) / \left(2(1 + \cos\left[\frac{1}{2}(c + dx)\right])^2 \right) \right) \right. \\
& \left. \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) / \left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right) + \\
& \left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) /
\end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. \left. \left. 17 - 12\sqrt{2} \right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \right) \right) \right) \left/ (3 \cos[c+dx]^{3/2}) \right. - \\
& \frac{1}{3\sqrt{\cos[c+dx]}} 2 \left(-\sin[c+dx] - \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]}{1 + \cos\left[\frac{1}{2}(c+dx)\right]}} \right. \\
& \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \tan\left[\frac{1}{4}(c+dx)\right] \right) \left/ \right. \\
& \left(\sqrt{2} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} - \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] \right. \\
& \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]}{1 + \cos\left[\frac{1}{2}(c+dx)\right]}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], \right. \right. \\
& \left. \left. 17 - 12\sqrt{2}\right] \sin\left[\frac{1}{4}(c+dx)\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} + \right. \\
& \left. \left(\sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right]^2 \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right. \right. \\
& \left. \left. \left(\frac{(-2 + \sqrt{2}) \sin\left[\frac{1}{2}(c+dx)\right]}{2(1 + \cos\left[\frac{1}{2}(c+dx)\right])} + \left((-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]) \right. \right. \right. \right. \\
& \left. \left. \left. \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) \left/ \left(2 \left(1 + \cos\left[\frac{1}{2}(c+dx)\right] \right)^2 \right) \right) \right) \\
& \left. \left. \left. \left. \left. \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \right) \right) \right) \left/ \left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]}{1 + \cos\left[\frac{1}{2}(c+dx)\right]}} \right) \right. \right. + \\
& \left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c+dx)\right]}{1 + \cos\left[\frac{1}{2}(c+dx)\right]}} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \right) \left/ \right. \\
& \left(\sqrt{2(3 - 2\sqrt{2})} \sqrt{1 - \frac{\tan\left[\frac{1}{4}(c+dx)\right]^2}{3 - 2\sqrt{2}}} \sqrt{1 - \frac{(17 - 12\sqrt{2}) \tan\left[\frac{1}{4}(c+dx)\right]^2}{3 - 2\sqrt{2}}} \right) \right) \right) \right) \right)
\end{aligned}$$

Problem 249: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{e \cos [c+d x]} (a+a \sin [c+d x])^2} dx$$

Optimal (type 4, 116 leaves, 4 steps):

$$\frac{2 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{7 a^2 d \sqrt{e \cos [c+d x]}} - \frac{2 \sqrt{e \cos [c+d x]}}{7 d e (a+a \sin [c+d x])^2} - \frac{2 \sqrt{e \cos [c+d x]}}{7 d e (a^2+a^2 \sin [c+d x])}$$

Result (type 4, 1209 leaves):

$$\left(\cos [c+d x] \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^4 \right. \\ \left. \left(-\frac{2}{7} - \frac{2}{7 \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^4} - \frac{2}{7 \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^2} \right) \right) / \\ \left(d \sqrt{e \cos [c+d x]} (a+a \sin [c+d x])^2 \right) + \left(2 \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^4 \right. \\ \left. \left(\frac{\cos \left[\frac{1}{2}(c+d x) \right] \sqrt{\cos [c+d x]}}{7 \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)} - \frac{\sqrt{\cos [c+d x]} \sin \left[\frac{1}{2}(c+d x) \right]}{7 \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)} \right) \right) \\ \left(\cos [c+d x] + 2 \sqrt{2} \cos \left[\frac{1}{4}(c+d x) \right] \right)^2 \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x) \right]}{1+\cos \left[\frac{1}{2}(c+d x) \right]}} \\ \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x) \right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x) \right]^2} \right) / \\ \left(7 d \sqrt{e \cos [c+d x]} (a+a \sin [c+d x])^2 \left(\left(\sin [c+d x] \left(\cos [c+d x] + 2 \sqrt{2} \cos \left[\frac{1}{4}(c+d x) \right] \right)^2 \right. \right. \right. \\ \left. \left. \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x) \right]}{1+\cos \left[\frac{1}{2}(c+d x) \right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x) \right]}{\sqrt{3-2 \sqrt{2}}}\right], \right. \right. \right. \\ \left. \left. \left. 17-12 \sqrt{2}\right] \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x) \right]^2} \right) \right) / \left(7 \cos [c+d x]^{3/2} \right) +$$

$$\begin{aligned}
& \frac{1}{7\sqrt{\cos[c+dx]}} 2 \left(-\sin[c+dx] - \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \right. \right. \\
& \quad \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \tan\left[\frac{1}{4}(c+dx)\right]\right) \right) / \\
& \left(\sqrt{2} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} - \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] \right. \\
& \quad \left. \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], \right. \right. \\
& \quad \left. \left. 17-12\sqrt{2}\right] \sin\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} + \right. \\
& \quad \left. \left(\sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right]^2 \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right. \right. \\
& \quad \left. \left. \left(\frac{(-2+\sqrt{2})\sin\left[\frac{1}{2}(c+dx)\right]}{2(1+\cos\left[\frac{1}{2}(c+dx)\right])} + \left((-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]) \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) / \left(2(1+\cos\left[\frac{1}{2}(c+dx)\right])^2 \right) \right) \right) \\
& \quad \left. \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \right) + \\
& \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \\
& \left(\sqrt{2(3-2\sqrt{2})} \sqrt{1-\frac{\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \sqrt{1-\frac{(17-12\sqrt{2})\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \right) \right) \right)
\end{aligned}$$

Problem 259: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{3/2}}{(a + a \sin [c + d x])^3} dx$$

Optimal (type 4, 118 leaves, 4 steps):

$$\frac{2 e^2 \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 a^3 d \sqrt{e \cos [c + d x]}} - \frac{4 e \sqrt{e \cos [c + d x]}}{7 a d (a + a \sin [c + d x])^2} + \frac{2 e \sqrt{e \cos [c + d x]}}{21 d (a^3 + a^3 \sin [c + d x])}$$

Result (type 4, 1217 leaves):

$$\left((e \cos [c + d x])^{3/2} \operatorname{Sec}[c + d x] \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)^6 \right. \\ \left. \left(\frac{2}{21} - \frac{4}{7 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)^4} + \frac{2}{21 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)^2} \right) \right) / \\ (d (a + a \sin [c + d x])^3) - \\ \left(2 (e \cos [c + d x])^{3/2} \operatorname{Sec}[c + d x]^2 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)^6 \right. \\ \left(- \frac{\cos \left[\frac{1}{2}(c + d x) \right] \sqrt{\cos [c + d x]}}{21 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)} + \frac{\sqrt{\cos [c + d x]} \sin \left[\frac{1}{2}(c + d x) \right]}{21 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)} \right) \\ \left(\cos [c + d x] + 2 \sqrt{2} \cos \left[\frac{1}{4}(c + d x) \right] \right)^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2}(c + d x) \right]}{1 + \cos \left[\frac{1}{2}(c + d x) \right]}} \\ \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4}(c + d x) \right]^2} \right) \right) / \\ \left(21 d (a + a \sin [c + d x])^3 \left(\left(\left(\sin [c + d x] \left(\cos [c + d x] + 2 \sqrt{2} \cos \left[\frac{1}{4}(c + d x) \right] \right)^2 \right. \right. \right. \right. \right. \\ \left. \left. \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2}(c + d x) \right]}{1 + \cos \left[\frac{1}{2}(c + d x) \right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], \right. \right. \right. \right. \\ \left. \left. \left. 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4}(c + d x) \right]^2} \right) \right) \right) / (21 \cos [c + d x]^{3/2}) \right) -$$

$$\begin{aligned}
& \frac{1}{21 \sqrt{\cos[c+dx]}} \left(-\sin[c+dx] - \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \right. \right. \\
& \quad \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \tan\left[\frac{1}{4}(c+dx)\right] \right) \right) / \\
& \left(\sqrt{2} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} - \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] \right. \\
& \quad \left. \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], \right. \right. \\
& \quad \left. \left. 17-12\sqrt{2}\right] \sin\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} + \right. \\
& \quad \left. \left(\sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right]^2 \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right. \right. \\
& \quad \left. \left. \left(\frac{(-2+\sqrt{2})\sin\left[\frac{1}{2}(c+dx)\right]}{2(1+\cos\left[\frac{1}{2}(c+dx)\right])} + \left((-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]) \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \left(2(1+\cos\left[\frac{1}{2}(c+dx)\right])^2 \right) \right) \\
& \quad \left. \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \right) + \\
& \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \\
& \left(\sqrt{2(3-2\sqrt{2})} \sqrt{1-\frac{\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \sqrt{1-\frac{(17-12\sqrt{2})\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \right) \right) \right)
\end{aligned}$$

Problem 261: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{e \cos[c+dx]} (a+a \sin[c+dx])^3} dx$$

Optimal (type 4, 153 leaves, 5 steps):

$$\frac{10 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{77 a^3 d \sqrt{e \cos [c+d x]}} - \frac{2 \sqrt{e \cos [c+d x]}}{11 d e (a+a \sin [c+d x])^3} - \frac{10 \sqrt{e \cos [c+d x]}}{77 a d e (a+a \sin [c+d x])^2} - \frac{10 \sqrt{e \cos [c+d x]}}{77 d e (a^3+a^3 \sin [c+d x])}$$

Result (type 4, 1236 leaves):

$$\left(\cos [c+d x] \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^6 \right. \\ \left(-\frac{10}{77} - \frac{2}{11 \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^6} - \frac{10}{77 \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^4} - \frac{10}{77 \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^2} \right) \Bigg/ \\ \left(d \sqrt{e \cos [c+d x]} (a+a \sin [c+d x])^3 \right) + \left(10 \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^6 \right. \\ \left. \left(\frac{5 \cos \left[\frac{1}{2}(c+d x) \right] \sqrt{\cos [c+d x]}}{77 \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)} - \frac{5 \sqrt{\cos [c+d x]} \sin \left[\frac{1}{2}(c+d x) \right]}{77 \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)} \right) \right. \\ \left. \left(\cos [c+d x] + 2 \sqrt{2} \cos \left[\frac{1}{4}(c+d x) \right] \right)^2 \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x) \right]}{1+\cos \left[\frac{1}{2}(c+d x) \right]}} \right. \\ \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x) \right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x) \right]^2} \right) \Bigg/ \\ \left(77 d \sqrt{e \cos [c+d x]} (a+a \sin [c+d x])^3 \right) \left(\left(5 \sin [c+d x] \left(\cos [c+d x] + 2 \sqrt{2} \cos \left[\frac{1}{4}(c+d x) \right] \right)^2 \right. \right. \\ \left. \left. \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2}) \cos \left[\frac{1}{2}(c+d x) \right]}{1+\cos \left[\frac{1}{2}(c+d x) \right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x) \right]}{\sqrt{3-2 \sqrt{2}}}\right], \right. \right. \right. \\ \left. \left. \left. 17-12 \sqrt{2}\right] \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x) \right]^2} \right) \right) \Bigg/ (77 \cos [c+d x]^{3/2}) +$$

$$\begin{aligned}
& \frac{1}{77 \sqrt{\cos[c+dx]}} \left(-\sin[c+dx] - \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \right. \right. \\
& \quad \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \tan\left[\frac{1}{4}(c+dx)\right]\right) \right) / \\
& \left(\sqrt{2} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} - \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] \right. \\
& \quad \left. \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], \right. \right. \\
& \quad \left. \left. 17-12\sqrt{2}\right] \sin\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} + \right. \\
& \quad \left. \left(\sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right]^2 \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right. \right. \\
& \quad \left. \left. \left(\frac{(-2+\sqrt{2})\sin\left[\frac{1}{2}(c+dx)\right]}{2(1+\cos\left[\frac{1}{2}(c+dx)\right])} + \left((-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]) \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \left(2(1+\cos\left[\frac{1}{2}(c+dx)\right])^2 \right) \right) \\
& \quad \left. \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \right) + \\
& \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \\
& \left(\sqrt{2(3-2\sqrt{2})} \sqrt{1-\frac{\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \sqrt{1-\frac{(17-12\sqrt{2})\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \right) \right) \right)
\end{aligned}$$

Problem 267: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{7/2}}{(a + a \sin [c + d x])^4} dx$$

Optimal (type 4, 120 leaves, 4 steps):

$$\frac{10 e^4 \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{21 a^4 d \sqrt{e \cos [c + d x]}} + \frac{4 e (e \cos [c + d x])^{5/2}}{7 a d (a + a \sin [c + d x])^3} + \frac{20 e^3 \sqrt{e \cos [c + d x]}}{21 d (a^4 + a^4 \sin [c + d x])}$$

Result (type 4, 1219 leaves):

$$\left((e \cos [c + d x])^{7/2} \operatorname{Sec}[c + d x]^3 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)^8 \right. \\ \left. \left(-\frac{10}{21} - \frac{8}{7 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)^4} + \frac{32}{21 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)^2} \right) \right) / \\ (d (a + a \sin [c + d x])^4) + \\ \left(10 (e \cos [c + d x])^{7/2} \operatorname{Sec}[c + d x]^4 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)^8 \right. \\ \left(\frac{5 \cos \left[\frac{1}{2}(c + d x) \right] \sqrt{\cos [c + d x]}}{21 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)} - \frac{5 \sqrt{\cos [c + d x]} \sin \left[\frac{1}{2}(c + d x) \right]}{21 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)} \right) \\ \left(\cos [c + d x] + 2 \sqrt{2} \cos \left[\frac{1}{4}(c + d x) \right] \right)^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2}(c + d x) \right]}{1 + \cos \left[\frac{1}{2}(c + d x) \right]}} \\ \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4}(c + d x) \right]^2} \right) \right) / \\ \left(21 d (a + a \sin [c + d x])^4 \left(\left(5 \sin [c + d x] \left(\cos [c + d x] + 2 \sqrt{2} \cos \left[\frac{1}{4}(c + d x) \right] \right)^2 \right. \right. \right. \\ \left. \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2}(c + d x) \right]}{1 + \cos \left[\frac{1}{2}(c + d x) \right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], \right. \right. \right. \\ \left. \left. \left. 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4}(c + d x) \right]^2} \right) \right) \right) / (21 \cos [c + d x]^{3/2}) +$$

$$\begin{aligned}
& \frac{1}{21 \sqrt{\cos[c+dx]}} \left(-\sin[c+dx] - \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \right. \right. \\
& \quad \left. \left. \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \tan\left[\frac{1}{4}(c+dx)\right]\right) \right) / \\
& \left(\sqrt{2} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} - \sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right] \right. \\
& \quad \left. \sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], \right. \right. \\
& \quad \left. \left. 17-12\sqrt{2}\right] \sin\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} + \right. \\
& \quad \left. \left(\sqrt{2} \cos\left[\frac{1}{4}(c+dx)\right]^2 \text{EllipticF}\left[\text{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right. \right. \\
& \quad \left. \left. \left(\frac{(-2+\sqrt{2})\sin\left[\frac{1}{2}(c+dx)\right]}{2(1+\cos\left[\frac{1}{2}(c+dx)\right])} + \left((-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]) \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sin\left[\frac{1}{2}(c+dx)\right] \right) \right) \right) / \left(2(1+\cos\left[\frac{1}{2}(c+dx)\right])^2 \right) \right) \\
& \quad \left. \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \right) + \\
& \left(\sqrt{\frac{-1+\sqrt{2}-(-2+\sqrt{2})\cos\left[\frac{1}{2}(c+dx)\right]}{1+\cos\left[\frac{1}{2}(c+dx)\right]}} \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \\
& \left(\sqrt{2(3-2\sqrt{2})} \sqrt{1-\frac{\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \sqrt{1-\frac{(17-12\sqrt{2})\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \right) \right) \right)
\end{aligned}$$

Problem 269: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{3/2}}{(a + a \sin [c + d x])^4} dx$$

Optimal (type 4, 154 leaves, 5 steps):

$$\frac{2 e^2 \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c + d x), 2\right]}{77 a^4 d \sqrt{e \cos [c + d x]}} - \frac{4 e \sqrt{e \cos [c + d x]}}{11 a d (a + a \sin [c + d x])^3} + \frac{2 e \sqrt{e \cos [c + d x]}}{77 d (a^2 + a^2 \sin [c + d x])^2} + \frac{2 e \sqrt{e \cos [c + d x]}}{77 d (a^4 + a^4 \sin [c + d x])}$$

Result (type 4, 1244 leaves):

$$\left((e \cos [c + d x])^{3/2} \sec [c + d x] \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)^8 \right. \\ \left. \left(\frac{2}{77} - \frac{4}{11 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)^6} + \frac{2}{77 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)^4} + \frac{2}{77 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)^2} \right) \right) / (d (a + a \sin [c + d x])^4) - \\ \left(2 (e \cos [c + d x])^{3/2} \sec [c + d x]^2 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)^8 \right. \\ \left(- \frac{\cos \left[\frac{1}{2}(c + d x) \right] \sqrt{\cos [c + d x]}}{77 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)} + \frac{\sqrt{\cos [c + d x]} \sin \left[\frac{1}{2}(c + d x) \right]}{77 \left(\cos \left[\frac{1}{2}(c + d x) \right] + \sin \left[\frac{1}{2}(c + d x) \right] \right)} \right) \\ \left(\cos [c + d x] + 2 \sqrt{2} \cos \left[\frac{1}{4}(c + d x) \right] \right)^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2}(c + d x) \right]}{1 + \cos \left[\frac{1}{2}(c + d x) \right]}} \\ \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4}(c + d x) \right]^2} \right) \right) / \\ \left(77 d (a + a \sin [c + d x])^4 \left(- \left(\left(\sin [c + d x] \left(\cos [c + d x] + 2 \sqrt{2} \cos \left[\frac{1}{4}(c + d x) \right] \right)^2 \right. \right. \right. \right. \right. \\ \left. \left. \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos \left[\frac{1}{2}(c + d x) \right]}{1 + \cos \left[\frac{1}{2}(c + d x) \right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], \right. \right. \right. \right. \right. \right.$$

Problem 271: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{e \cos[c + dx]} (a + a \sin[c + dx])^4} dx$$

Optimal (type 4, 191 leaves, 6 steps):

$$\frac{2 \sqrt{\cos[c + dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c + dx), 2\right]}{33 a^4 d \sqrt{e \cos[c + dx]}} - \frac{2 \sqrt{e \cos[c + dx]}}{15 d e (a + a \sin[c + dx])^4} - \frac{14 \sqrt{e \cos[c + dx]}}{165 a d e (a + a \sin[c + dx])^3} - \frac{2 \sqrt{e \cos[c + dx]}}{33 d e (a^2 + a^2 \sin[c + dx])^2} - \frac{2 \sqrt{e \cos[c + dx]}}{33 d e (a^4 + a^4 \sin[c + dx])}$$

Result (type 4, 1263 leaves):

$$\left(\cos[c + dx] \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^8 \left(-\frac{2}{33} - \frac{2}{15 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^8} - \frac{14}{165 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^6} - \frac{2}{33 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^4} - \frac{2}{33 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^2} \right) \right) /$$

$$\left(d \sqrt{e \cos[c + dx]} (a + a \sin[c + dx])^4 \right) + \left(2 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^8 \left(\frac{\cos\left[\frac{1}{2}(c + dx)\right] \sqrt{\cos[c + dx]}}{33 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)} - \frac{\sqrt{\cos[c + dx]} \sin\left[\frac{1}{2}(c + dx)\right]}{33 \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)} \right) \right)$$

$$\left(\cos[c + dx] + 2 \sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right] \right)^2 \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) /$$

$$\left(33 d \sqrt{e \cos[c + dx]} (a + a \sin[c + dx])^4 \left(\left(\sin[c + dx] \left(\cos[c + dx] + 2 \sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right] \right)^2 \right) \right) \right)$$

$$\begin{aligned}
& \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], \right. \\
& \left. 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \Bigg) / (33 \cos[c + dx]^{3/2}) + \\
& \frac{1}{33\sqrt{\cos[c + dx]}} 2 \left(-\sin[c + dx] - \left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right. \right. \\
& \left. \left. \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \tan\left[\frac{1}{4}(c + dx)\right] \right) / \right. \\
& \left. \left(\sqrt{2} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} - \sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right] \right) \right. \\
& \left. \sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], \right. \right. \\
& \left. \left. 17 - 12\sqrt{2}\right] \sin\left[\frac{1}{4}(c + dx)\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} + \right. \\
& \left. \left(\sqrt{2} \cos\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right. \right. \\
& \left. \left. \left(\frac{(-2 + \sqrt{2}) \sin\left[\frac{1}{2}(c + dx)\right]}{2(1 + \cos\left[\frac{1}{2}(c + dx)\right])} + \left((-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]) \right. \right. \right. \right. \\
& \left. \left. \left. \sin\left[\frac{1}{2}(c + dx)\right] \right) / \left(2(1 + \cos\left[\frac{1}{2}(c + dx)\right])^2 \right) \right) \right. \\
& \left. \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) / \left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \right) + \\
& \left(\sqrt{\frac{-1 + \sqrt{2} - (-2 + \sqrt{2}) \cos\left[\frac{1}{2}(c + dx)\right]}{1 + \cos\left[\frac{1}{2}(c + dx)\right]}} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) /
\end{aligned}$$

$$\left(\sqrt{2(3-2\sqrt{2})} \sqrt{1 - \frac{\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \sqrt{1 - \frac{(17-12\sqrt{2})\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \right) \Bigg) \Bigg) \Bigg)$$

Problem 273: Result unnecessarily involves imaginary or complex numbers.

$$\int (e \cos[c+dx])^{3/2} \sqrt{a+a \sin[c+dx]} dx$$

Optimal (type 3, 236 leaves, 8 steps):

$$\begin{aligned} & -\frac{a(e \cos[c+dx])^{5/2}}{2de\sqrt{a+a \sin[c+dx]}} + \frac{3e\sqrt{e \cos[c+dx]}\sqrt{a+a \sin[c+dx]}}{4d} - \\ & \frac{3e^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c+dx]}}{\sqrt{e}}\right] \sqrt{1+\cos[c+dx]}\sqrt{a+a \sin[c+dx]}}{4d(1+\cos[c+dx]+\sin[c+dx])} + \\ & \left(\frac{3e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c+dx]}{\sqrt{e \cos[c+dx]}\sqrt{1+\cos[c+dx]}}\right] \sqrt{1+\cos[c+dx]}\sqrt{a+a \sin[c+dx]}}{4d(1+\cos[c+dx]+\sin[c+dx])} \right) / \end{aligned}$$

Result (type 3, 269 leaves):

$$\begin{aligned} & -\left(\left(i e^{-i(c+dx)} \sqrt{e \cos[c+dx]} \left(-i \sqrt{1+e^{2i(c+dx)}} - 2e^{i(c+dx)} \sqrt{1+e^{2i(c+dx)}} + \right. \right. \right. \\ & \quad \left. \left. \left. 2ie^{2i(c+dx)} \sqrt{1+e^{2i(c+dx)}} + e^{3i(c+dx)} \sqrt{1+e^{2i(c+dx)}} - 3de^{2i(c+dx)} x + \right. \right. \right. \\ & \quad \left. \left. \left. 3e^{2i(c+dx)} \operatorname{ArcSinh}\left[e^{i(c+dx)}\right] - 3ie^{2i(c+dx)} \operatorname{Log}\left[1+\sqrt{1+e^{2i(c+dx)}}\right] \right) \right) \right) \\ & \sqrt{a(1+\sin[c+dx])} \Bigg) / \left(4d(i+e^{i(c+dx)}) \sqrt{1+e^{2i(c+dx)}} \right) \end{aligned}$$

Problem 274: Result unnecessarily involves imaginary or complex numbers.

$$\int \sqrt{e \cos[c+dx]} \sqrt{a+a \sin[c+dx]} dx$$

Optimal (type 3, 194 leaves, 7 steps):

$$\begin{aligned} & -\frac{a(e \cos[c+dx])^{3/2}}{de\sqrt{a+a \sin[c+dx]}} + \frac{\sqrt{e} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c+dx]}}{\sqrt{e}}\right] \sqrt{1+\cos[c+dx]}\sqrt{a+a \sin[c+dx]}}{d(1+\cos[c+dx]+\sin[c+dx])} + \\ & \left(\frac{\sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c+dx]}{\sqrt{e \cos[c+dx]}\sqrt{1+\cos[c+dx]}}\right] \sqrt{1+\cos[c+dx]}\sqrt{a+a \sin[c+dx]}}{d(1+\cos[c+dx]+\sin[c+dx])} \right) / \end{aligned}$$

Result (type 3, 195 leaves):

$$- \left(\left(i \sqrt{e \cos[c+dx]} \left(-i \sqrt{1+e^{2i(c+dx)}} + e^{i(c+dx)} \sqrt{1+e^{2i(c+dx)}} + \right. \right. \right. \\ \left. \left. \left. i d e^{i(c+dx)} x + i e^{i(c+dx)} \operatorname{ArcSinh}\left[e^{i(c+dx)}\right] - e^{i(c+dx)} \operatorname{Log}\left[1+\sqrt{1+e^{2i(c+dx)}}\right]\right) \right) \\ \left. \sqrt{a(1+\sin[c+dx])} \right) / \left(d \left(i + e^{i(c+dx)} \right) \sqrt{1+e^{2i(c+dx)}} \right)$$

Problem 275: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{\sqrt{a+a \sin[c+dx]}}{\sqrt{e \cos[c+dx]}} dx$$

Optimal (type 3, 161 leaves, 6 steps):

$$- \frac{2 \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c+dx]}}{\sqrt{e}}\right] \sqrt{1+\cos[c+dx]} \sqrt{a+a \sin[c+dx]}}{d \sqrt{e} (1+\cos[c+dx]+\sin[c+dx])} + \\ \left(\frac{2 \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c+dx]}{\sqrt{e \cos[c+dx]} \sqrt{1+\cos[c+dx]}}\right] \sqrt{1+\cos[c+dx]} \sqrt{a+a \sin[c+dx]}}{d \sqrt{e} (1+\cos[c+dx]+\sin[c+dx])} \right) /$$

Result (type 3, 108 leaves):

$$\left(\sqrt{1+e^{2i(c+dx)}} \left(dx - \operatorname{ArcSinh}\left[e^{i(c+dx)}\right] + i \operatorname{Log}\left[1+\sqrt{1+e^{2i(c+dx)}}\right] \right) \sqrt{a(1+\sin[c+dx])} \right) / \\ \left(d \left(1 - i e^{i(c+dx)} \right) \sqrt{e \cos[c+dx]} \right)$$

Problem 280: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (e \cos[c+dx])^{5/2} (a+a \sin[c+dx])^{3/2} dx$$

Optimal (type 3, 319 leaves, 10 steps):

$$- \frac{15 a^3 (e \cos[c+dx])^{7/2}}{32 d e (a+a \sin[c+dx])^{3/2}} + \frac{15 a^2 e (e \cos[c+dx])^{3/2}}{64 d \sqrt{a+a \sin[c+dx]}} - \\ \frac{3 a^2 (e \cos[c+dx])^{7/2}}{8 d e \sqrt{a+a \sin[c+dx]}} - \frac{a (e \cos[c+dx])^{7/2} \sqrt{a+a \sin[c+dx]}}{4 d e} + \\ \frac{45 a e^{5/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c+dx]}}{\sqrt{e}}\right] \sqrt{1+\cos[c+dx]} \sqrt{a+a \sin[c+dx]}}{64 d (1+\cos[c+dx]+\sin[c+dx])} + \\ \left(\frac{45 a e^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c+dx]}{\sqrt{e \cos[c+dx]} \sqrt{1+\cos[c+dx]}}\right] \sqrt{1+\cos[c+dx]} \sqrt{a+a \sin[c+dx]}}{64 d (1+\cos[c+dx]+\sin[c+dx])} \right) /$$

Result (type 4, 2816 leaves):

$$\begin{aligned}
 & \left((e \cos [c + d x])^{5/2} \sec [c + d x]^2 (a (1 + \sin [c + d x]))^{3/2} \right. \\
 & \quad \left(-\frac{3}{4} \cos \left[\frac{1}{2} (c + d x) \right] + \frac{3}{64} \cos \left[\frac{3}{2} (c + d x) \right] - \frac{1}{8} \cos \left[\frac{5}{2} (c + d x) \right] - \frac{1}{32} \cos \left[\frac{7}{2} (c + d x) \right] + \right. \\
 & \quad \left. \frac{3}{4} \sin \left[\frac{1}{2} (c + d x) \right] + \frac{3}{64} \sin \left[\frac{3}{2} (c + d x) \right] + \frac{1}{8} \sin \left[\frac{5}{2} (c + d x) \right] - \frac{1}{32} \sin \left[\frac{7}{2} (c + d x) \right] \right) / \\
 & \left(d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 \right) + \left(45 \sqrt{3 - 2 \sqrt{2}} (e \cos [c + d x])^{5/2} \right. \\
 & \quad \sec [c + d x]^2 (a (1 + \sin [c + d x]))^{3/2} \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} \left(1 + \tan \left[\frac{1}{4} (c + d x) \right] \right)^2 \right) \\
 & \quad \sqrt{\frac{-3 + 2 \sqrt{2} + \tan \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan \left[\frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \tan \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
 & \quad \sqrt{1 - 3 \tan \left[\frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \tan \left[\frac{1}{4} (c + d x) \right]^2} \\
 & \quad \left(2 - 2 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \sqrt{2} \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} \right) \\
 & \quad \left(4 \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} \right. \\
 & \quad \left. \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} + \right. \\
 & \quad \left. 8 \operatorname{EllipticPi} \left[-3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right. \\
 & \quad \left. \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[\frac{1}{4} (c + d x) \right]^2} \right. \\
 & \quad \left. \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} + \sqrt{2} \left(\operatorname{Log} \left[1 + \tan \left[\frac{1}{4} (c + d x) \right] \right]^2 - \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[2 - 2 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \sqrt{2} \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} \right] \right) \right)
 \end{aligned}$$

$$\left(1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4 \right) \Bigg) \Bigg) /$$

$$\left(128 d \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^4 \left(4 \sec\left[\frac{1}{4}(c+dx)\right]^2 - \right. \right.$$

$$3\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 - 52 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 +$$

$$39\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 + 200 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 -$$

$$150\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 - 200 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 +$$

$$150\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 + 52 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^8 -$$

$$39\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^8 - 4 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^{10} +$$

$$3\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^{10} + 2\sqrt{2(3-2\sqrt{2})} \sec\left[\frac{1}{4}(c+dx)\right]^2$$

$$\tan\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2} + \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}}$$

$$\sqrt{\frac{-3+2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c+dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}}$$

$$\sqrt{1-3 \tan\left[\frac{1}{4}(c+dx)\right]^2 + 2\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2} - 12\sqrt{2(3-2\sqrt{2})} \sec\left[\frac{1}{4}(c+dx)\right]^2$$

$$\tan\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2} + \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}}$$

$$\sqrt{\frac{-3+2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c+dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}}$$

$$\sqrt{1-3 \tan\left[\frac{1}{4}(c+dx)\right]^2 + 2\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2} + 2\sqrt{2(3-2\sqrt{2})} \sec\left[\frac{1}{4}(c+dx)\right]^2$$

$$\tan\left[\frac{1}{4}(c+dx)\right]^5 \sqrt{3-2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2} + \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}}$$

$$\begin{aligned}
 & \sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 - 12\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3 + 2\sqrt{2}}} \\
 & \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 -} \\
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 4\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 32\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 84 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 56\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 32\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 4\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 4\sqrt{3 - 2\sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \\
 & \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3 + 2\sqrt{2}}}
 \end{aligned}$$

$$\sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}}$$

$$\sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}$$

$$\sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4 - 4\sqrt{3 - 2\sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2}$$

$$\operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^3 \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}}$$

$$\sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}}$$

$$\sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}$$

$$\sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} \right)$$

Problem 281: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (e \operatorname{Cos}[c + dx])^{3/2} (a + a \operatorname{Sin}[c + dx])^{3/2} dx$$

Optimal (type 3, 278 leaves, 9 steps):

$$\frac{7 a^2 (e \operatorname{Cos}[c + dx])^{5/2}}{12 d e \sqrt{a + a \operatorname{Sin}[c + dx]}} + \frac{7 a e \sqrt{e \operatorname{Cos}[c + dx]} \sqrt{a + a \operatorname{Sin}[c + dx]}}{8 d}$$

$$\frac{a (e \operatorname{Cos}[c + dx])^{5/2} \sqrt{a + a \operatorname{Sin}[c + dx]}}{3 d e}$$

$$\frac{7 a e^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \operatorname{Cos}[c + dx]}}{\sqrt{e}}\right] \sqrt{1 + \operatorname{Cos}[c + dx]} \sqrt{a + a \operatorname{Sin}[c + dx]}}{8 d (1 + \operatorname{Cos}[c + dx] + \operatorname{Sin}[c + dx])} +$$

$$\left(\frac{7 a e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \operatorname{Sin}[c + dx]}{\sqrt{e \operatorname{Cos}[c + dx]} \sqrt{1 + \operatorname{Cos}[c + dx]}}\right] \sqrt{1 + \operatorname{Cos}[c + dx]} \sqrt{a + a \operatorname{Sin}[c + dx]}}{8 d (1 + \operatorname{Cos}[c + dx] + \operatorname{Sin}[c + dx])} \right) /$$

Result (type 4, 2810 leaves):

$$\begin{aligned}
 & \left((e \cos [c + d x])^{3/2} \sec [c + d x] (a (1 + \sin [c + d x]))^{3/2} \left(\frac{5}{12} \cos \left[\frac{1}{2} (c + d x) \right] - \frac{3}{8} \cos \left[\frac{3}{2} (c + d x) \right] - \right. \right. \\
 & \quad \left. \left. \frac{1}{12} \cos \left[\frac{5}{2} (c + d x) \right] + \frac{5}{12} \sin \left[\frac{1}{2} (c + d x) \right] + \frac{3}{8} \sin \left[\frac{3}{2} (c + d x) \right] - \frac{1}{12} \sin \left[\frac{5}{2} (c + d x) \right] \right) \right) / \\
 & \left(d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 - \left(7 \sqrt{3 - 2 \sqrt{2}} (e \cos [c + d x])^{3/2} \sec [c + d x] \right. \right. \\
 & \quad \left. \left. (a (1 + \sin [c + d x]))^{3/2} \sqrt{3 - 2 \sqrt{2}} - \tan \left[\frac{1}{4} (c + d x) \right]^2 \left(1 + \tan \left[\frac{1}{4} (c + d x) \right]^2 \right) \right. \right. \\
 & \quad \left. \sqrt{\frac{-3 + 2 \sqrt{2} + \tan \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan \left[\frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \tan \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right. \\
 & \quad \left. \sqrt{1 - 3 \tan \left[\frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \tan \left[\frac{1}{4} (c + d x) \right]^2} \right. \\
 & \quad \left. \left(2 - 2 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \sqrt{2} \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} \right) \right. \\
 & \quad \left. \left(4 \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2}} - \tan \left[\frac{1}{4} (c + d x) \right]^2 \right. \right. \\
 & \quad \left. \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} + \right. \\
 & \quad \left. 8 \operatorname{EllipticPi} \left[-3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right. \\
 & \quad \left. \sqrt{3 - 2 \sqrt{2}} - \tan \left[\frac{1}{4} (c + d x) \right]^2 \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[\frac{1}{4} (c + d x) \right]^2} \right. \\
 & \quad \left. \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} - \sqrt{2} \left(\log \left[1 + \tan \left[\frac{1}{4} (c + d x) \right]^2 \right] - \right. \right. \\
 & \quad \left. \left. \log \left[2 - 2 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \sqrt{2} \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} \right] \right) \right. \\
 & \quad \left. \left. \left(1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4 \right) \right) \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(16 d \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 \right. \\
 & \left(-4 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 + 3 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 + 52 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 - \right. \\
 & 39 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 - 200 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^4 + \\
 & 150 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^4 + 200 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^6 - \\
 & 150 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^6 - 52 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^8 + \\
 & 39 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^8 + 4 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^{10} - \\
 & 3 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^{10} + 2 \sqrt{2 (3 - 2 \sqrt{2})} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \\
 & \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right] \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
 & \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
 & \sqrt{1 - 3 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2 (3 - 2 \sqrt{2})} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2} \\
 & \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^3 \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
 & \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
 & \sqrt{1 - 3 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2 (3 - 2 \sqrt{2})} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2} \\
 & \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^5 \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
 & \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 +} \\
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 4\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 32\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 84 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 56\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 32\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 4\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 4\sqrt{3-2\sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \\
 & \sqrt{3-2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2} + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 - 12\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}}
 \end{aligned}$$

$$\begin{aligned} & \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \\ & \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4 - 4\sqrt{3 - 2\sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2} \\ & \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^3 \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\ & \sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\ & \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \\ & \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} \end{aligned}$$

Problem 282: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sqrt{e \cos [c + dx]} (a + a \sin [c + dx])^{3/2} dx$$

Optimal (type 3, 243 leaves, 8 steps):

$$\begin{aligned} & \frac{5 a^2 (e \cos [c + dx])^{3/2}}{4 d e \sqrt{a + a \sin [c + dx]}} - \frac{a (e \cos [c + dx])^{3/2} \sqrt{a + a \sin [c + dx]}}{2 d e} + \\ & \frac{5 a \sqrt{e} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos [c + dx]}}{\sqrt{e}}\right] \sqrt{1 + \cos [c + dx]} \sqrt{a + a \sin [c + dx]}}{4 d (1 + \cos [c + dx] + \sin [c + dx])} + \\ & \left(\frac{5 a \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin [c + dx]}{\sqrt{e \cos [c + dx]} \sqrt{1 + \cos [c + dx]}}\right] \sqrt{1 + \cos [c + dx]} \sqrt{a + a \sin [c + dx]}}{4 d (1 + \cos [c + dx] + \sin [c + dx])} \right) / \end{aligned}$$

Result (type 4, 2322 leaves):

$$\begin{aligned} & \left(\sqrt{e \cos [c + dx]} (a (1 + \sin [c + dx]))^{3/2} \right. \\ & \left. \left(-\frac{3}{2} \cos \left[\frac{1}{2}(c + dx) \right] - \frac{1}{4} \cos \left[\frac{3}{2}(c + dx) \right] + \frac{3}{2} \sin \left[\frac{1}{2}(c + dx) \right] - \frac{1}{4} \sin \left[\frac{3}{2}(c + dx) \right] \right) \right) / \\ & \left(d \left(\cos \left[\frac{1}{2}(c + dx) \right] + \sin \left[\frac{1}{2}(c + dx) \right] \right)^3 \right) - \end{aligned}$$

$$\begin{aligned}
 & \left(25 \cos \left[\frac{1}{4} (c + d x) \right]^2 \sqrt{e \cos [c + d x]} (a (1 + \sin [c + d x]))^{3/2} \left(\sqrt{2} \left(\log \left[\sec \left[\frac{1}{4} (c + d x) \right]^2 \right] - \right. \right. \right. \\
 & \quad \left. \left. \left. \log \left[2 + \sqrt{2} \sqrt{\cos [c + d x] \sec \left[\frac{1}{4} (c + d x) \right]^4 - 2 \tan \left[\frac{1}{4} (c + d x) \right]^2} \right] \right) \right. \right. \\
 & \quad \left. \sqrt{\cos [c + d x] \sec \left[\frac{1}{4} (c + d x) \right]^4} + 4 \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right. \\
 & \quad \left. \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[\frac{1}{4} (c + d x) \right]^2} + \right. \\
 & \quad \left. 8 \operatorname{EllipticPi} \left[-3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right. \\
 & \quad \left. \left. \left. \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[\frac{1}{4} (c + d x) \right]^2} \right) \right) \right) / \\
 & \left(64 d \sqrt{\cos [c + d x]} \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^4 \right. \\
 & \left(\frac{1}{16 \sqrt{\cos [c + d x]}} 5 \cos \left[\frac{1}{4} (c + d x) \right] \sin \left[\frac{1}{4} (c + d x) \right] \left(\sqrt{2} \left(\log \left[\sec \left[\frac{1}{4} (c + d x) \right]^2 \right] - \right. \right. \right. \\
 & \quad \left. \left. \left. \log \left[2 + \sqrt{2} \sqrt{\cos [c + d x] \sec \left[\frac{1}{4} (c + d x) \right]^4 - 2 \tan \left[\frac{1}{4} (c + d x) \right]^2} \right] \right) \right) \right. \\
 & \quad \left. \sqrt{\cos [c + d x] \sec \left[\frac{1}{4} (c + d x) \right]^4} + 4 \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], \right. \right. \\
 & \quad \left. \left. 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[\frac{1}{4} (c + d x) \right]^2} + \right. \\
 & \quad \left. 8 \operatorname{EllipticPi} \left[-3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right. \\
 & \quad \left. \left. \left. \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[\frac{1}{4} (c + d x) \right]^2} \right) \right) - \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{16 \cos [c+d x]^{3/2}} 5 \cos \left[\frac{1}{4}(c+d x)\right]^2 \sin [c+d x] \left(\sqrt{2} \left(\log \left[\sec \left[\frac{1}{4}(c+d x)\right]^2\right] - \right. \right. \\
 & \quad \left. \left. \log \left[2+\sqrt{2} \sqrt{\cos [c+d x] \sec \left[\frac{1}{4}(c+d x)\right]^4 - 2 \tan \left[\frac{1}{4}(c+d x)\right]^2} \right] \right) \right. \\
 & \quad \left. \sqrt{\cos [c+d x] \sec \left[\frac{1}{4}(c+d x)\right]^4} + 4 \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}} \right], \right. \right. \\
 & \quad \left. \left. 17-12 \sqrt{2} \right] \sqrt{3-2 \sqrt{2} - \tan \left[\frac{1}{4}(c+d x)\right]^2} \sqrt{1+(-3+2 \sqrt{2}) \tan \left[\frac{1}{4}(c+d x)\right]^2} + \right. \\
 & \quad \left. 8 \operatorname{EllipticPi} \left[-3+2 \sqrt{2}, -\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}} \right], 17-12 \sqrt{2} \right] \right. \\
 & \quad \left. \sqrt{3-2 \sqrt{2} - \tan \left[\frac{1}{4}(c+d x)\right]^2} \sqrt{1+(-3+2 \sqrt{2}) \tan \left[\frac{1}{4}(c+d x)\right]^2} \right) - \\
 & \frac{1}{8 \sqrt{\cos [c+d x]}} 5 \cos \left[\frac{1}{4}(c+d x)\right]^2 \left(\left(\left(\log \left[\sec \left[\frac{1}{4}(c+d x)\right]^2\right] - \log \left[\right. \right. \right. \right. \\
 & \quad \left. \left. \left. 2+\sqrt{2} \sqrt{\cos [c+d x] \sec \left[\frac{1}{4}(c+d x)\right]^4 - 2 \tan \left[\frac{1}{4}(c+d x)\right]^2} \right] \right) \right) \right. \\
 & \quad \left. \left(-\sec \left[\frac{1}{4}(c+d x)\right]^4 \sin [c+d x] + \cos [c+d x] \sec \left[\frac{1}{4}(c+d x)\right]^4 \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{4}(c+d x)\right] \right) \right) / \left(\sqrt{2} \sqrt{\cos [c+d x] \sec \left[\frac{1}{4}(c+d x)\right]^4} + \right. \\
 & \quad \left. \left((-3+2 \sqrt{2}) \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}} \right], 17-12 \sqrt{2} \right] \right. \right. \\
 & \quad \left. \left. \sec \left[\frac{1}{4}(c+d x)\right]^2 \tan \left[\frac{1}{4}(c+d x)\right] \sqrt{3-2 \sqrt{2} - \tan \left[\frac{1}{4}(c+d x)\right]^2} \right) / \right. \\
 & \quad \left. \left(\sqrt{1+(-3+2 \sqrt{2}) \tan \left[\frac{1}{4}(c+d x)\right]^2} \right) + \left(2(-3+2 \sqrt{2}) \operatorname{EllipticPi} \left[-3+2 \sqrt{2}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\text{ArcSin}\left[\frac{\text{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\left]\text{Sec}\left[\frac{1}{4}(c+dx)\right]^2\text{Tan}\left[\frac{1}{4}(c+dx)\right]\right. \\
 & \left.\sqrt{3-2\sqrt{2}-\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}\right]/\left(\sqrt{1+(-3+2\sqrt{2})\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}\right)- \\
 & \left(\text{EllipticF}\left[\text{ArcSin}\left[\frac{\text{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\text{Sec}\left[\frac{1}{4}(c+dx)\right]^2\text{Tan}\left[\frac{1}{4}(c+dx)\right]\right) \\
 & \left.\sqrt{1+(-3+2\sqrt{2})\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}\right)/\left(\sqrt{3-2\sqrt{2}-\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}\right)- \\
 & \left(2\text{EllipticPi}\left[-3+2\sqrt{2}, -\text{ArcSin}\left[\frac{\text{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right]\right) \\
 & \text{Sec}\left[\frac{1}{4}(c+dx)\right]^2\text{Tan}\left[\frac{1}{4}(c+dx)\right]\sqrt{1+(-3+2\sqrt{2})\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}/ \\
 & \left(\sqrt{3-2\sqrt{2}-\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}\right)+\left(\text{Sec}\left[\frac{1}{4}(c+dx)\right]^2\right) \\
 & \left.\sqrt{3-2\sqrt{2}-\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}\sqrt{1+(-3+2\sqrt{2})\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}\right)/ \\
 & \left(\sqrt{3-2\sqrt{2}}\sqrt{1-\frac{\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}}\sqrt{1-\frac{(17-12\sqrt{2})\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}}\right)- \\
 & \left(2\text{Sec}\left[\frac{1}{4}(c+dx)\right]^2\sqrt{3-2\sqrt{2}-\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}\right) \\
 & \left.\sqrt{1+(-3+2\sqrt{2})\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}\right)/\left(\sqrt{3-2\sqrt{2}}\sqrt{1-\frac{\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}}\right) \\
 & \left.\sqrt{1-\frac{(17-12\sqrt{2})\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}}\left(1-\frac{(-3+2\sqrt{2})\text{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}\right)\right)+
 \end{aligned}$$

$$\sqrt{2} \sqrt{\cos [c+d x] \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^4} \left(\frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}(c+d x)\right] - \left(-\operatorname{Sec}\left[\frac{1}{4}(c+d x)\right] \right)^2 \operatorname{Tan}\left[\frac{1}{4}(c+d x)\right] + \left(-\operatorname{Sec}\left[\frac{1}{4}(c+d x)\right] \right)^4 \sin [c+d x] + \cos [c+d x] \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^4 \operatorname{Tan}\left[\frac{1}{4}(c+d x)\right] \right) / \left(\sqrt{2} \sqrt{\cos [c+d x] \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^4} \right) / \left(2 + \sqrt{2} \sqrt{\cos [c+d x] \operatorname{Sec}\left[\frac{1}{4}(c+d x)\right]^4} - 2 \operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]^2 \right)$$

Problem 283: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin [c+d x])^{3/2}}{\sqrt{e \cos [c+d x]}} dx$$

Optimal (type 3, 198 leaves, 7 steps):

$$\frac{a \sqrt{e \cos [c+d x]} \sqrt{a + a \sin [c+d x]}}{d e} + \frac{3 a \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos [c+d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos [c+d x]} \sqrt{a + a \sin [c+d x]}}{d \sqrt{e} (1 + \cos [c+d x] + \sin [c+d x])} + \frac{\left(3 a \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin [c+d x]}{\sqrt{e \cos [c+d x]} \sqrt{1 + \cos [c+d x]}}\right] \sqrt{1 + \cos [c+d x]} \sqrt{a + a \sin [c+d x]} \right)}{d \sqrt{e} (1 + \cos [c+d x] + \sin [c+d x])}$$

Result (type 4, 2750 leaves):

$$\left(\cos [c+d x] \left(-\cos \left[\frac{1}{2}(c+d x) \right] - \sin \left[\frac{1}{2}(c+d x) \right] \right) (a (1 + \sin [c+d x]))^{3/2} \right) / \left(d \sqrt{e \cos [c+d x]} \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^3 \right) - \left(3 \sqrt{3 - 2 \sqrt{2}} \cos [c+d x] (a (1 + \sin [c+d x]))^{3/2} \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]^2} \right) \left(1 + \operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]^2 \right) \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan}\left[\frac{1}{4}(c+d x)\right]^2}{-3 + 2 \sqrt{2}}}$$

$$\begin{aligned}
 & \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c+dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3 + 2\sqrt{2}}} \\
 & \sqrt{1 - 3 \tan\left[\frac{1}{4}(c+dx)\right]^2 + 2\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \left(2 - 2 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} \right) \\
 & \left(4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \right. \\
 & \quad \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & \quad \left. 8 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right. \\
 & \quad \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \quad \left. \sqrt{1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} - \sqrt{2} \left(\operatorname{Log}\left[1 + \tan\left[\frac{1}{4}(c+dx)\right]^2\right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[2 - 2 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4}\right] \right) \right) \\
 & \quad \left. \left(1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4 \right) \right) \Bigg) / \\
 & \left(2 d \sqrt{e \cos[c+dx]} \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right) \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right) \right)^3 \\
 & \left(-4 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 + 3\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 + 52 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 - \right. \\
 & \quad \left. 39\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 - 200 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 150 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 + 200 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 - \\
 & 150 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 - 52 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 + \\
 & 39 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 + 4 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^{10} - \\
 & 3 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^{10} + 2 \sqrt{2(3-2\sqrt{2})} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2(3-2\sqrt{2})}\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2(3-2\sqrt{2})}\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^5 \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+} \\
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} -
 \end{aligned}$$

$$\begin{aligned}
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 32 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 84 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 56 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 32 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \\
 & \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}-4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}}
 \end{aligned}$$

$$\sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}}$$

$$\sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}$$

$$\sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4}$$

Problem 284: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \operatorname{Sin}[c + dx])^{3/2}}{(e \operatorname{Cos}[c + dx])^{3/2}} dx$$

Optimal (type 3, 210 leaves, 7 steps):

$$\frac{4 a \sqrt{a + a \operatorname{Sin}[c + dx]} - \frac{2 a^2 \operatorname{ArcSinh}\left[\frac{\sqrt{e \operatorname{Cos}[c + dx]}}{\sqrt{e}}\right] \sqrt{1 + \operatorname{Cos}[c + dx]} \sqrt{a + a \operatorname{Sin}[c + dx]}}{d e^{3/2} (a + a \operatorname{Cos}[c + dx] + a \operatorname{Sin}[c + dx])}}{\left(\frac{2 a^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} \operatorname{Sin}[c + dx]}{\sqrt{e \operatorname{Cos}[c + dx]} \sqrt{1 + \operatorname{Cos}[c + dx]}}\right] \sqrt{1 + \operatorname{Cos}[c + dx]} \sqrt{a + a \operatorname{Sin}[c + dx]}}{d e^{3/2} (a + a \operatorname{Cos}[c + dx] + a \operatorname{Sin}[c + dx])} \right) /}$$

Result (type 4, 2727 leaves):

$$\left(4 \operatorname{Cos}[c + dx]^2 (a (1 + \operatorname{Sin}[c + dx]))^{3/2} \right) / \left(d (e \operatorname{Cos}[c + dx])^{3/2} \right)$$

$$\left(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \right) \left(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \right)^3 -$$

$$\left(\sqrt{3 - 2\sqrt{2}} \operatorname{Cos}[c + dx]^2 (a (1 + \operatorname{Sin}[c + dx]))^{3/2} \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \right.$$

$$\left. \left(1 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 \right) \sqrt{\frac{-3 + 2\sqrt{2} + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \right.$$

$$\left. \sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \right.$$

$$\left. \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \right)$$

$$\left(\begin{aligned} &2 - 2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} \\ &4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \\ &\sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} + \\ &8 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \\ &\sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2} \\ &\sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4} + \sqrt{2} \left(\operatorname{Log}\left[1 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2\right] - \right. \\ &\left. \operatorname{Log}\left[2 - 2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \sqrt{2} \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4}\right] \right) \\ &\left(1 - 6 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4\right) \Big) / \end{aligned} \right)$$

$$\left(d \left(e \operatorname{Cos}[c + d x] \right)^{3/2} \left(\operatorname{Cos}\left[\frac{1}{2} (c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2} (c + d x)\right] \right)^4 \right)$$

$$\left(\begin{aligned} &4 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 - 3\sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 - 52 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + \\ &39\sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^2 + 200 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4 - \\ &150\sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^4 - 200 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^6 + \\ &150\sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^6 + 52 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^8 - \\ &39\sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^8 - 4 \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^{10} + \\ &3\sqrt{2} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \operatorname{Tan}\left[\frac{1}{4} (c + d x)\right]^{10} + 2\sqrt{2(3 - 2\sqrt{2})} \operatorname{Sec}\left[\frac{1}{4} (c + d x)\right]^2 \end{aligned} \right)$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2(3-2\sqrt{2})}\sec\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \tan\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2(3-2\sqrt{2})}\sec\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \tan\left[\frac{1}{4}(c+dx)\right]^5 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2} - \\
 & 6\sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 4\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 48\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 32\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} -
 \end{aligned}$$

$$\begin{aligned}
 & 84 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 56 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 32 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \\
 & \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}-4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}
 \end{aligned}$$

$$\sqrt{1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4}$$

Problem 289: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (e \cos [c + dx])^{3/2} (a + a \sin [c + dx])^{5/2} dx$$

Optimal (type 3, 323 leaves, 10 steps):

$$\begin{aligned} & -\frac{77 a^3 (e \cos [c + dx])^{5/2}}{96 d e \sqrt{a + a \sin [c + dx]}} + \frac{77 a^2 e \sqrt{e \cos [c + dx]} \sqrt{a + a \sin [c + dx]}}{64 d} - \\ & \frac{11 a^2 (e \cos [c + dx])^{5/2} \sqrt{a + a \sin [c + dx]}}{24 d e} - \\ & \frac{77 a^2 e^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos [c + dx]}}{\sqrt{e}}\right] \sqrt{1 + \cos [c + dx]} \sqrt{a + a \sin [c + dx]}}{64 d (1 + \cos [c + dx] + \sin [c + dx])} + \\ & \left(\frac{77 a^2 e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin [c + dx]}{\sqrt{e \cos [c + dx]} \sqrt{1 + \cos [c + dx]}}\right] \sqrt{1 + \cos [c + dx]} \sqrt{a + a \sin [c + dx]}}{64 d (1 + \cos [c + dx] + \sin [c + dx])} - \frac{a (e \cos [c + dx])^{5/2} (a + a \sin [c + dx])^{3/2}}{4 d e} \right) / \end{aligned}$$

Result (type 4, 2838 leaves):

$$\begin{aligned} & \left((e \cos [c + dx])^{3/2} \operatorname{Sec}[c + dx] (a (1 + \sin [c + dx]))^{5/2} \right. \\ & \left. \left(\frac{5}{12} \cos\left[\frac{1}{2}(c + dx)\right] - \frac{35}{64} \cos\left[\frac{3}{2}(c + dx)\right] - \frac{5}{24} \cos\left[\frac{5}{2}(c + dx)\right] + \frac{1}{32} \cos\left[\frac{7}{2}(c + dx)\right] + \right. \right. \\ & \left. \left. \frac{5}{12} \sin\left[\frac{1}{2}(c + dx)\right] + \frac{35}{64} \sin\left[\frac{3}{2}(c + dx)\right] - \frac{5}{24} \sin\left[\frac{5}{2}(c + dx)\right] - \frac{1}{32} \sin\left[\frac{7}{2}(c + dx)\right] \right) \right) / \\ & \left(d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^5 \right) - \left(77 \sqrt{3 - 2\sqrt{2}} (e \cos [c + dx])^{3/2} \right. \\ & \operatorname{Sec}[c + dx] (a (1 + \sin [c + dx]))^{5/2} \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \left(1 + \tan\left[\frac{1}{4}(c + dx)\right]^2 \right) \\ & \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\ & \left. \sqrt{1 - 3 \tan\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) \end{aligned}$$

$$\begin{aligned}
 & \left(2 - 2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right] \right)^2 + \sqrt{2} \sqrt{1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^4} \right) \\
 & \left(4 \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \right. \right. \\
 & \quad \sqrt{1 + (-3 + 2 \sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^4} + \\
 & \quad \left. 8 \operatorname{EllipticPi} \left[-3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[\frac{\operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right. \right. \\
 & \quad \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \\
 & \quad \left. \sqrt{1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^4} - \sqrt{2} \left(\operatorname{Log} \left[1 + \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[2 - 2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 + \sqrt{2} \sqrt{1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^4} \right] \right) \right) \right) \\
 & \left. \left(1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^4 \right) \right) \Bigg) / \\
 & \left(128 d \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right) \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right) \right)^5 \\
 & \left(-4 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 + 3 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 + 52 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 - \right. \\
 & \quad 39 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 - 200 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^4 + \\
 & \quad 150 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^4 + 200 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^6 - \\
 & \quad 150 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^6 - 52 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^8 + \\
 & \quad 39 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^8 + 4 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^{10} - \\
 & \quad \left. 3 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^{10} + 2 \sqrt{2(3 - 2 \sqrt{2})} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2(3-2\sqrt{2})}\sec\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \tan\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2(3-2\sqrt{2})}\sec\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \tan\left[\frac{1}{4}(c+dx)\right]^5 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2+} \\
 & 6\sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 4\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 48\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 32\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4}+
 \end{aligned}$$

$$\begin{aligned}
 & 84 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 56 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 32 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \\
 & \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}-4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}
 \end{aligned}$$

$$\sqrt{1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4}$$

Problem 290: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sqrt{e \cos[c + dx]} (a + a \sin[c + dx])^{5/2} dx$$

Optimal (type 3, 286 leaves, 9 steps):

$$\frac{15 a^3 (e \cos[c + dx])^{3/2} - 3 a^2 (e \cos[c + dx])^{3/2} \sqrt{a + a \sin[c + dx]}}{8 d e \sqrt{a + a \sin[c + dx]}} + \frac{15 a^2 \sqrt{e} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c + dx]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c + dx]} \sqrt{a + a \sin[c + dx]}}{8 d (1 + \cos[c + dx] + \sin[c + dx])} + \left(\frac{15 a^2 \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c + dx]}{\sqrt{e \cos[c + dx]}}\right] \sqrt{1 + \cos[c + dx]} \sqrt{a + a \sin[c + dx]}}{\sqrt{e \cos[c + dx]} \sqrt{1 + \cos[c + dx]}} \right) / (8 d (1 + \cos[c + dx] + \sin[c + dx])) - \frac{a (e \cos[c + dx])^{3/2} (a + a \sin[c + dx])^{3/2}}{3 d e}$$

Result (type 4, 2350 leaves):

$$\left(\sqrt{e \cos[c + dx]} (a (1 + \sin[c + dx]))^{5/2} \left(-\frac{29}{12} \cos\left[\frac{1}{2}(c + dx)\right] - \frac{5}{8} \cos\left[\frac{3}{2}(c + dx)\right] + \frac{1}{12} \cos\left[\frac{5}{2}(c + dx)\right] + \frac{29}{12} \sin\left[\frac{1}{2}(c + dx)\right] - \frac{5}{8} \sin\left[\frac{3}{2}(c + dx)\right] - \frac{1}{12} \sin\left[\frac{5}{2}(c + dx)\right] \right) \right) / \left(d \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^5 \right) - \left(225 \cos\left[\frac{1}{4}(c + dx)\right]^2 \sqrt{e \cos[c + dx]} (a (1 + \sin[c + dx]))^{5/2} \left(\sqrt{2} \left(\log\left[\sec\left[\frac{1}{4}(c + dx)\right]^2\right] - \log\left[2 + \sqrt{2} \sqrt{\cos[c + dx] \sec\left[\frac{1}{4}(c + dx)\right]^4 - 2 \tan\left[\frac{1}{4}(c + dx)\right]^2}\right]} \right) \right) \right) \sqrt{\cos[c + dx] \sec\left[\frac{1}{4}(c + dx)\right]^4} + 4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c + dx)\right]^2} + \right.$$

$$\begin{aligned}
& 8 \operatorname{EllipticPi} \left[-3 + 2\sqrt{2}, -\operatorname{ArcSin} \left[\frac{\operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2\sqrt{2}}} \right], 17 - 12\sqrt{2} \right] \\
& \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \Bigg) / \\
& \left(256 d \sqrt{\operatorname{Cos} [c + d x]} \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right)^6 \right. \\
& \left. \left(\frac{1}{32 \sqrt{\operatorname{Cos} [c + d x]}} 15 \operatorname{Cos} \left[\frac{1}{4} (c + d x) \right] \operatorname{Sin} \left[\frac{1}{4} (c + d x) \right] \left(\sqrt{2} \left(\operatorname{Log} \left[\operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \right] - \right. \right. \right. \right. \right. \\
& \left. \left. \left. \operatorname{Log} \left[2 + \sqrt{2} \sqrt{\operatorname{Cos} [c + d x] \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^4 - 2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \right] \right) \right) \right. \right. \\
& \left. \left. \sqrt{\operatorname{Cos} [c + d x] \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^4} + 4 \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2\sqrt{2}}} \right], \right. \right. \right. \\
& \left. \left. 17 - 12\sqrt{2} \right] \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} + \right. \\
& \left. 8 \operatorname{EllipticPi} \left[-3 + 2\sqrt{2}, -\operatorname{ArcSin} \left[\frac{\operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2\sqrt{2}}} \right], 17 - 12\sqrt{2} \right] \right. \\
& \left. \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \right) - \\
& \frac{1}{32 \operatorname{Cos} [c + d x]^{3/2}} 15 \operatorname{Cos} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Sin} [c + d x] \left(\sqrt{2} \left(\operatorname{Log} \left[\operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \right] - \right. \right. \\
& \left. \left. \operatorname{Log} \left[2 + \sqrt{2} \sqrt{\operatorname{Cos} [c + d x] \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^4 - 2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \right] \right) \right. \\
& \left. \left. \sqrt{\operatorname{Cos} [c + d x] \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^4} + 4 \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2\sqrt{2}}} \right], \right. \right. \right. \\
& \left. \left. 17 - 12\sqrt{2} \right] \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} + \right.
\end{aligned}$$

$$\begin{aligned}
 & 8 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \\
 & \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{1+(-3+2\sqrt{2})\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} - \\
 & \frac{1}{16\sqrt{\operatorname{Cos}[c+dx]}} 15 \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^2 \left(\left(\left(\operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]\right]^2\right) - \operatorname{Log}\left[\right. \right. \right. \\
 & \left. \left. \left. 2+\sqrt{2} \sqrt{\operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^4 - 2\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right] \right) \right. \right. \\
 & \left. \left. \left(-\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^4 \operatorname{Sin}[c+dx] + \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^4 \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \right) \right) / \left(\sqrt{2} \sqrt{\operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^4} + \right. \right. \\
 & \left. \left. \left((-3+2\sqrt{2}) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) / \right. \right. \\
 & \left. \left. \left(\sqrt{1+(-3+2\sqrt{2})\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) + \left(2(-3+2\sqrt{2}) \operatorname{EllipticPi}\left[-3+2\sqrt{2}, \right. \right. \right. \\
 & \left. \left. \left. -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \right. \right. \right. \\
 & \left. \left. \left. \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) / \left(\sqrt{1+(-3+2\sqrt{2})\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) - \right. \right. \\
 & \left. \left. \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1+(-3+2\sqrt{2})\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) / \left(\sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 \operatorname{EllipticPi} \left[-3 + 2\sqrt{2}, -\operatorname{ArcSin} \left[\frac{\operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]}{\sqrt{3 - 2\sqrt{2}}} \right], 17 - 12\sqrt{2} \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right] \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \right) / \\
 & \left(\sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \right) + \left(\operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \right. \\
 & \quad \left. \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \right) / \\
 & \left(\sqrt{3 - 2\sqrt{2}} \sqrt{1 - \frac{\operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{3 - 2\sqrt{2}}} \sqrt{1 - \frac{(17 - 12\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{3 - 2\sqrt{2}}} \right) - \\
 & \left(2 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \right. \\
 & \quad \left. \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \right) / \left(\sqrt{3 - 2\sqrt{2}} \sqrt{1 - \frac{\operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{3 - 2\sqrt{2}}} \right. \\
 & \quad \left. \sqrt{1 - \frac{(17 - 12\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{3 - 2\sqrt{2}}} \left(1 - \frac{(-3 + 2\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{3 - 2\sqrt{2}} \right) \right) + \\
 & \sqrt{2} \sqrt{\operatorname{Cos}[c + dx] \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^4} \left(\frac{1}{2} \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right] - \left(-\operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{4} (c + dx) \right] + \left(-\operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^4 \operatorname{Sin}[c + dx] + \operatorname{Cos}[c + dx] \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^4 \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right] \right) \right) / \left(\sqrt{2} \sqrt{\operatorname{Cos}[c + dx] \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^4} \right) \right) / \\
 & \left(2 + \sqrt{2} \sqrt{\operatorname{Cos}[c + dx] \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^4 - 2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \right) \right) \right) \right)
 \end{aligned}$$

Problem 291: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[c + d x])^{5/2}}{\sqrt{e \cos[c + d x]}} dx$$

Optimal (type 3, 247 leaves, 8 steps):

$$\begin{aligned} & \frac{7 a^2 \sqrt{e \cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{4 d e} - \\ & \frac{21 a^2 \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos [c+d x]}}{\sqrt{e}}\right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{4 d \sqrt{e}\left(1+\cos [c+d x]+\sin [c+d x]\right)} + \\ & \left(\frac{21 a^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin [c+d x]}{\sqrt{e \cos [c+d x]} \sqrt{1+\cos [c+d x]}}\right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{4 d \sqrt{e}\left(1+\cos [c+d x]+\sin [c+d x]\right)} - \frac{a \sqrt{e \cos [c+d x]}(a+a \sin [c+d x])^{3/2}}{2 d e} \right) / \end{aligned}$$

Result (type 4, 2782 leaves):

$$\begin{aligned} & \left(\cos [c+d x] (a(1+\sin [c+d x]))^{5/2} \right. \\ & \quad \left. \left(-\frac{5}{2} \cos \left[\frac{1}{2}(c+d x) \right] + \frac{1}{4} \cos \left[\frac{3}{2}(c+d x) \right] - \frac{5}{2} \sin \left[\frac{1}{2}(c+d x) \right] - \frac{1}{4} \sin \left[\frac{3}{2}(c+d x) \right] \right) \right) / \\ & \left(d \sqrt{e \cos [c+d x]} \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^5 \right) - \\ & \left(21 \sqrt{3-2 \sqrt{2}} \cos [c+d x] (a(1+\sin [c+d x]))^{5/2} \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x) \right]^2} \right. \\ & \quad \left. \left(1 + \tan \left[\frac{1}{4}(c+d x) \right] \right)^2 \sqrt{\frac{-3+2 \sqrt{2}+\tan \left[\frac{1}{4}(c+d x) \right]^2}{-3+2 \sqrt{2}}} \right. \\ & \quad \left. \sqrt{\frac{-3+2 \sqrt{2}+17 \tan \left[\frac{1}{4}(c+d x) \right]^2-12 \sqrt{2} \tan \left[\frac{1}{4}(c+d x) \right]^2}{-3+2 \sqrt{2}}} \right. \\ & \quad \left. \sqrt{1-3 \tan \left[\frac{1}{4}(c+d x) \right]^2+2 \sqrt{2} \tan \left[\frac{1}{4}(c+d x) \right]^2} \right. \\ & \quad \left. \left(2-2 \tan \left[\frac{1}{4}(c+d x) \right]^2+\sqrt{2} \sqrt{1-6 \tan \left[\frac{1}{4}(c+d x) \right]^2+\tan \left[\frac{1}{4}(c+d x) \right]^4} \right) \right. \\ & \quad \left. \left(4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x) \right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x) \right]^2} \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4} + \\
 & 8 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \\
 & \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c + dx)\right]^2} \\
 & \sqrt{1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4} - \sqrt{2} \left(\operatorname{Log}\left[1 + \tan\left[\frac{1}{4}(c + dx)\right]^2\right] - \right. \\
 & \left. \operatorname{Log}\left[2 - 2 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4}\right] \right) \\
 & \left. \left(1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4\right) \right) \Bigg/ \\
 & \left(8 d \sqrt{e \cos[c + dx]} \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right]\right) \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right]\right)\right)^5 \\
 & \left(-4 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 + 3\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 + 52 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^2 - \right. \\
 & 39\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^2 - 200 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^4 + \\
 & 150\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^4 + 200 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^6 - \\
 & 150\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^6 - 52 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^8 + \\
 & 39\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^8 + 4 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^{10} - \\
 & \left. 3\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^{10} + 2\sqrt{2(3 - 2\sqrt{2})} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{4}(c + dx)\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}}\right) \\
 & \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2(3 - 2\sqrt{2})} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2} \\
 & \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^3 \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\
 & \sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\
 & \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2(3 - 2\sqrt{2})} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2} \\
 & \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^5 \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\
 & \sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\
 & \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 +} \\
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} - \\
 & 4\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} - \\
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} + \\
 & 32\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} + \\
 & 84 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} - \\
 & 56\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} -
 \end{aligned}$$

$$\begin{aligned}
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 32 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \\
 & \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}-4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} \right)
 \end{aligned}$$

Problem 292: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin[c + d x])^{5/2}}{(e \cos[c + d x])^{3/2}} dx$$

Optimal (type 3, 239 leaves, 8 steps):

$$\frac{5 a^3 (e \cos [c + d x])^{3/2}}{d e^3 \sqrt{a + a \sin [c + d x]}} - \frac{5 a^2 \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos [c + d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos [c + d x]} \sqrt{a + a \sin [c + d x]}}{d e^{3/2} (1 + \cos [c + d x] + \sin [c + d x])} - \left(\frac{5 a^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin [c + d x]}{\sqrt{e \cos [c + d x]} \sqrt{1 + \cos [c + d x]}}\right] \sqrt{1 + \cos [c + d x]} \sqrt{a + a \sin [c + d x]}}{d e^{3/2} (1 + \cos [c + d x] + \sin [c + d x])} + \frac{4 a (a + a \sin [c + d x])^{3/2}}{d e \sqrt{e \cos [c + d x]}} \right) /$$

Result (type 4, 2753 leaves):

$$\left(\cos [c + d x]^2 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \frac{8}{\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right]} - \sin \left[\frac{1}{2} (c + d x) \right] \right) (a (1 + \sin [c + d x]))^{5/2} \right) / \left(d (e \cos [c + d x])^{3/2} \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^5 \right) - \left(5 \sqrt{3 - 2 \sqrt{2}} \cos [c + d x]^2 (a (1 + \sin [c + d x]))^{5/2} \sqrt{3 - 2 \sqrt{2}} - \tan \left[\frac{1}{4} (c + d x) \right]^2 \right. \\ \left. \left(1 + \tan \left[\frac{1}{4} (c + d x) \right] \right)^2 \sqrt{\frac{-3 + 2 \sqrt{2} + \tan \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right. \\ \left. \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan \left[\frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \tan \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right. \\ \left. \sqrt{1 - 3 \tan \left[\frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \tan \left[\frac{1}{4} (c + d x) \right]^2} \right. \\ \left. \left(2 - 2 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \sqrt{2} \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} \right) \right. \\ \left. \left(4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}}\right], 17 - 12 \sqrt{2}\right] \sqrt{3 - 2 \sqrt{2}} - \tan \left[\frac{1}{4} (c + d x) \right]^2 \right. \right. \\ \left. \left. \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} + \right. \right.$$

$$\begin{aligned}
 & 8 \operatorname{EllipticPi} \left[-3 + 2\sqrt{2}, -\operatorname{ArcSin} \left[\frac{\operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]}{\sqrt{3 - 2\sqrt{2}}} \right], 17 - 12\sqrt{2} \right] \\
 & \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \\
 & \sqrt{1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^4} + \sqrt{2} \left(\operatorname{Log} \left[1 + \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 \right] - \right. \\
 & \left. \operatorname{Log} \left[2 - 2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + \sqrt{2} \sqrt{1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^4} \right] \right) \\
 & \left. \left(1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^4 \right) \right) \Bigg) / \\
 & \left(2d (e \operatorname{Cos} [c + dx])^{3/2} \left(\operatorname{Cos} \left[\frac{1}{2} (c + dx) \right] + \operatorname{Sin} \left[\frac{1}{2} (c + dx) \right] \right)^6 \right. \\
 & \left(4 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 - 3\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 - 52 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + \right. \\
 & 39\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + 200 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^4 - \\
 & 150\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^4 - 200 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^6 + \\
 & 150\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^6 + 52 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^8 - \\
 & 39\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^8 - 4 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^{10} + \\
 & \left. 3\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^{10} + 2\sqrt{2(3 - 2\sqrt{2})} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \right. \\
 & \left. \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right] \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{-3 + 2\sqrt{2}}} \right. \\
 & \left. \sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 - 12\sqrt{2} \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{-3 + 2\sqrt{2}}} \right. \\
 & \left. \sqrt{1 - 3 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + 2\sqrt{2} \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} - 12\sqrt{2(3 - 2\sqrt{2})} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2} + 2\sqrt{2(3-2\sqrt{2})} \sec\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \tan\left[\frac{1}{4}(c+dx)\right]^5 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2} - \\
 & 6\sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 4\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 48\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 32\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 84\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 56\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 48\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 32\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} -
 \end{aligned}$$

$$\begin{aligned}
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \\
 & \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} - 4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \left. \left. \left. \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} \right) \right) \right)
 \end{aligned}$$

Problem 293: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \operatorname{Sin}[c + dx])^{5/2}}{(e \operatorname{Cos}[c + dx])^{5/2}} dx$$

Optimal (type 3, 204 leaves, 7 steps):

$$\frac{2 a^2 \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos [c+d x]}}{\sqrt{e}}\right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{d e^{5 / 2}\left(1+\cos [c+d x]+\sin [c+d x]\right)} -$$

$$\left(2 a^2 \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin [c+d x]}{\sqrt{e \cos [c+d x]} \sqrt{1+\cos [c+d x]}}\right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}\right) /$$

$$\left(d e^{5 / 2}\left(1+\cos [c+d x]+\sin [c+d x]\right)\right)+\frac{4 a\left(a+a \sin [c+d x]\right)^{3 / 2}}{3 d e\left(e \cos [c+d x]\right)^{3 / 2}}$$

Result (type 4, 2795 leaves):

$$\left(\cos [c+d x]^3\left(\frac{4}{3\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)}+\frac{8 \sin \left[\frac{1}{2}(c+d x)\right]}{3\left(\cos \left[\frac{1}{2}(c+d x)\right]-\sin \left[\frac{1}{2}(c+d x)\right]\right)^2}\right)\right.$$

$$\left.\left(a\left(1+\sin [c+d x]\right)\right)^{5 / 2}\right) / \left(d\left(e \cos [c+d x]\right)^{5 / 2}\left(\cos \left[\frac{1}{2}(c+d x)\right]+\sin \left[\frac{1}{2}(c+d x)\right]\right)^5\right)+$$

$$\left(\sqrt{3-2 \sqrt{2}} \cos [c+d x]^3\left(a\left(1+\sin [c+d x]\right)\right)^{5 / 2} \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}\right.$$

$$\left.\left(1+\tan \left[\frac{1}{4}(c+d x)\right]\right)^2\right) \sqrt{\frac{-3+2 \sqrt{2}+\tan \left[\frac{1}{4}(c+d x)\right]^2}{-3+2 \sqrt{2}}}$$

$$\sqrt{\frac{-3+2 \sqrt{2}+17 \tan \left[\frac{1}{4}(c+d x)\right]^2-12 \sqrt{2} \tan \left[\frac{1}{4}(c+d x)\right]^2}{-3+2 \sqrt{2}}}$$

$$\sqrt{1-3 \tan \left[\frac{1}{4}(c+d x)\right]^2+2 \sqrt{2} \tan \left[\frac{1}{4}(c+d x)\right]^2}$$

$$\left(2-2 \tan \left[\frac{1}{4}(c+d x)\right]^2+\sqrt{2} \sqrt{1-6 \tan \left[\frac{1}{4}(c+d x)\right]^2+\tan \left[\frac{1}{4}(c+d x)\right]^4}\right)$$

$$\left(4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}\right.$$

$$\left.\sqrt{1+(-3+2 \sqrt{2}) \tan \left[\frac{1}{4}(c+d x)\right]^2} \sqrt{1-6 \tan \left[\frac{1}{4}(c+d x)\right]^2+\tan \left[\frac{1}{4}(c+d x)\right]^4}+\right.$$

$$\left.8 \operatorname{EllipticPi}\left[-3+2 \sqrt{2},-\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right]\right)$$

$$\begin{aligned}
 & \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c + dx)\right]^2} \\
 & \sqrt{1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4} - \sqrt{2} \left(\log\left[1 + \tan\left[\frac{1}{4}(c + dx)\right]^2\right] - \right. \\
 & \left. \log\left[2 - 2 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4}\right] \right) \\
 & \left. \left(1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4\right) \right) \Bigg/ \\
 & \left(d \left(e \cos[c + dx] \right)^{5/2} \left(\cos\left[\frac{1}{2}(c + dx)\right] - \sin\left[\frac{1}{2}(c + dx)\right] \right) \right) \\
 & \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^5 \\
 & \left(-4 \sec\left[\frac{1}{4}(c + dx)\right]^2 + 3\sqrt{2} \sec\left[\frac{1}{4}(c + dx)\right]^2 + 52 \sec\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^2 - \right. \\
 & 39\sqrt{2} \sec\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^2 - 200 \sec\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^4 + \\
 & 150\sqrt{2} \sec\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^4 + 200 \sec\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^6 - \\
 & 150\sqrt{2} \sec\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^6 - 52 \sec\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^8 + \\
 & 39\sqrt{2} \sec\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^8 + 4 \sec\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^{10} - \\
 & \left. 3\sqrt{2} \sec\left[\frac{1}{4}(c + dx)\right]^2 \tan\left[\frac{1}{4}(c + dx)\right]^{10} + 2\sqrt{2(3 - 2\sqrt{2})} \sec\left[\frac{1}{4}(c + dx)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{4}(c + dx)\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \right. \\
 & \left. \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \right. \\
 & \left. \sqrt{1 - 3 \tan\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \tan\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2(3 - 2\sqrt{2})} \sec\left[\frac{1}{4}(c + dx)\right]^2} \right)^2
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2} + 2\sqrt{2(3-2\sqrt{2})} \sec\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \tan\left[\frac{1}{4}(c+dx)\right]^5 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2} + \\
 & 6\sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 4\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 48\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 32\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 84\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 56\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 48\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 32\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} +
 \end{aligned}$$

$$\begin{aligned}
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \\
 & \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}-4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \left. \left. \left. \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}\right)\right)\right)
 \end{aligned}$$

Problem 294: Result more than twice size of optimal antiderivative.

$$\int \frac{(a+a \operatorname{Sin}[c+dx])^{5/2}}{(e \operatorname{Cos}[c+dx])^{7/2}} dx$$

Optimal (type 3, 36 leaves, 1 step):

$$\frac{2(a+a \operatorname{Sin}[c+dx])^{5/2}}{5 d e(e \operatorname{Cos}[c+dx])^{5/2}}$$

Result (type 3, 87 leaves):

$$\frac{2 a^2 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2 \sqrt{a (1 + \sin [c+d x])}}{5 d e^3 \sqrt{e \cos [c+d x]} \left(\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right)^2}$$

Problem 298: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c+d x])^{5/2}}{\sqrt{a+a \sin [c+d x]}} dx$$

Optimal (type 3, 244 leaves, 8 steps):

$$\begin{aligned} & -\frac{a (e \cos [c+d x])^{7/2}}{2 d e (a+a \sin [c+d x])^{3/2}} + \frac{e (e \cos [c+d x])^{3/2}}{4 d \sqrt{a+a \sin [c+d x]}} + \\ & \frac{3 e^{5/2} \operatorname{ArcSinh} \left[\frac{\sqrt{e \cos [c+d x]}}{\sqrt{e}} \right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{4 d (a+a \cos [c+d x]+a \sin [c+d x])} + \\ & \left(\frac{3 e^{5/2} \operatorname{ArcTan} \left[\frac{\sqrt{e} \sin [c+d x]}{\sqrt{e \cos [c+d x]} \sqrt{1+\cos [c+d x]}} \right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{4 d (a+a \cos [c+d x]+a \sin [c+d x])} \right) / \end{aligned}$$

Result (type 4, 2305 leaves):

$$\begin{aligned} & \left((e \cos [c+d x])^{5/2} \sec [c+d x]^2 \left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right) \right. \\ & \quad \left. \left(-\frac{1}{2} \cos \left[\frac{1}{2} (c+d x) \right] + \frac{1}{4} \cos \left[\frac{3}{2} (c+d x) \right] + \frac{1}{2} \sin \left[\frac{1}{2} (c+d x) \right] + \frac{1}{4} \sin \left[\frac{3}{2} (c+d x) \right] \right) \right) / \\ & \left(d \sqrt{a (1 + \sin [c+d x])} \right) - \\ & \left(9 \cos \left[\frac{1}{4} (c+d x) \right]^2 (e \cos [c+d x])^{5/2} \left(\sqrt{2} \left(\log \left[\sec \left[\frac{1}{4} (c+d x) \right]^2 \right] - \right. \right. \right. \\ & \quad \left. \left. \left. \log \left[2 + \sqrt{2} \sqrt{\cos [c+d x] \sec \left[\frac{1}{4} (c+d x) \right]^4 - 2 \tan \left[\frac{1}{4} (c+d x) \right]^2} \right] \right) \right) \right. \\ & \quad \left. \sqrt{\cos [c+d x] \sec \left[\frac{1}{4} (c+d x) \right]^4} + 4 \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c+d x) \right]}{\sqrt{3-2 \sqrt{2}}} \right], 17-12 \sqrt{2} \right] \right. \\ & \quad \left. \sqrt{3-2 \sqrt{2} - \tan \left[\frac{1}{4} (c+d x) \right]^2} \sqrt{1 + (-3+2 \sqrt{2}) \tan \left[\frac{1}{4} (c+d x) \right]^2} + \right. \end{aligned}$$

$$\begin{aligned}
 & 8 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \\
 & \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{1+(-3+2\sqrt{2})\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \Bigg) / \\
 & \left(64 d \operatorname{Cos}[c+dx]^{5/2} \sqrt{a(1+\operatorname{Sin}[c+dx])} \right. \\
 & \left. \left(\frac{1}{16\sqrt{\operatorname{Cos}[c+dx]}} 3 \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right] \operatorname{Sin}\left[\frac{1}{4}(c+dx)\right] \left(\sqrt{2} \left(\operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]\right]^2 \right) - \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Log}\left[2+\sqrt{2}\sqrt{\operatorname{Cos}[c+dx]\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^4-2\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}\right] \right) \right. \right. \\
 & \left. \left. \sqrt{\operatorname{Cos}[c+dx]\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^4} + 4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], \right. \right. \right. \\
 & \left. \left. \left. 17-12\sqrt{2}\right] \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{1+(-3+2\sqrt{2})\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} + \right. \right. \\
 & \left. \left. 8 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right. \right. \\
 & \left. \left. \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{1+(-3+2\sqrt{2})\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) - \right. \\
 & \left. \frac{1}{16\operatorname{Cos}[c+dx]^{3/2}} 3 \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Sin}[c+dx] \left(\sqrt{2} \left(\operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]\right]^2 \right) - \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Log}\left[2+\sqrt{2}\sqrt{\operatorname{Cos}[c+dx]\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^4-2\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}\right] \right) \right. \right. \\
 & \left. \left. \sqrt{\operatorname{Cos}[c+dx]\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^4} + 4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], \right. \right. \right. \\
 & \left. \left. \left. 17-12\sqrt{2}\right] \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{1+(-3+2\sqrt{2})\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & 8 \operatorname{EllipticPi}\left[-3+2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \\
 & \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{1+(-3+2\sqrt{2})\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} - \\
 & \frac{1}{8\sqrt{\operatorname{Cos}[c+dx]}} 3 \operatorname{Cos}\left[\frac{1}{4}(c+dx)\right]^2 \left(\left(\left(\operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]\right]^2 \right) - \operatorname{Log}\left[\right. \right. \right. \\
 & \left. \left. \left. 2+\sqrt{2} \sqrt{\operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^4 - 2\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right] \right) \right. \right. \\
 & \left. \left. \left(-\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^4 \operatorname{Sin}[c+dx] + \operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^4 \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \right) \right) \right) / \left(\sqrt{2} \sqrt{\operatorname{Cos}[c+dx] \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^4} \right) + \\
 & \left((-3+2\sqrt{2}) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) / \\
 & \left(\sqrt{1+(-3+2\sqrt{2})\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) + \left(2(-3+2\sqrt{2}) \operatorname{EllipticPi}\left[-3+2\sqrt{2}, \right. \right. \\
 & \left. \left. -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \right. \\
 & \left. \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) / \left(\sqrt{1+(-3+2\sqrt{2})\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) - \\
 & \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3-2\sqrt{2}}}\right], 17-12\sqrt{2}\right] \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \right. \\
 & \left. \sqrt{1+(-3+2\sqrt{2})\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) / \left(\sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 \operatorname{EllipticPi} \left[-3 + 2\sqrt{2}, -\operatorname{ArcSin} \left[\frac{\operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]}{\sqrt{3 - 2\sqrt{2}}} \right], 17 - 12\sqrt{2} \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right] \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \right) / \\
 & \left(\sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \right) + \left(\operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \right. \\
 & \quad \left. \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \right) / \\
 & \left(\sqrt{3 - 2\sqrt{2}} \sqrt{1 - \frac{\operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{3 - 2\sqrt{2}}} \sqrt{1 - \frac{(17 - 12\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{3 - 2\sqrt{2}}} \right) - \\
 & \left(2 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \right. \\
 & \quad \left. \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \right) / \left(\sqrt{3 - 2\sqrt{2}} \sqrt{1 - \frac{\operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{3 - 2\sqrt{2}}} \right. \\
 & \quad \left. \sqrt{1 - \frac{(17 - 12\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{3 - 2\sqrt{2}}} \left(1 - \frac{(-3 + 2\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{3 - 2\sqrt{2}} \right) \right) + \\
 & \sqrt{2} \sqrt{\operatorname{Cos}[c + dx] \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^4} \left(\frac{1}{2} \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right] - \left(-\operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\right. \right. \right. \\
 & \quad \left. \left. \frac{1}{4} (c + dx) \right] + \left(-\operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^4 \operatorname{Sin}[c + dx] + \operatorname{Cos}[c + dx] \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^4 \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right] \right) \right) / \left(\sqrt{2} \sqrt{\operatorname{Cos}[c + dx] \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^4} \right) \right) / \\
 & \left(2 + \sqrt{2} \sqrt{\operatorname{Cos}[c + dx] \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^4 - 2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \right) \right) \right) \right)
 \end{aligned}$$

Problem 299: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c+d x])^{3/2}}{\sqrt{a+a \sin [c+d x]}} d x$$

Optimal (type 3, 200 leaves, 7 steps):

$$\frac{e \sqrt{e \cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{a d} - \frac{e^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos [c+d x]}}{\sqrt{e}}\right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{a d (1+\cos [c+d x]+\sin [c+d x])} + \left(\frac{e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin [c+d x]}{\sqrt{e \cos [c+d x]} \sqrt{1+\cos [c+d x]}}\right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{a d (1+\cos [c+d x]+\sin [c+d x])} \right) /$$

Result (type 4, 2723 leaves):

$$\frac{(e \cos [c+d x])^{3/2} \operatorname{Sec}[c+d x] \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2}{d \sqrt{a(1+\sin [c+d x])}} - \left(\sqrt{3-2 \sqrt{2}} (e \cos [c+d x])^{3/2} \operatorname{Sec}[c+d x] \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right) \right) \sqrt{\frac{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2 \left(1+\tan \left[\frac{1}{4}(c+d x)\right]\right)^2}{-3+2 \sqrt{2}} \frac{-3+2 \sqrt{2}+\tan \left[\frac{1}{4}(c+d x)\right]^2}{-3+2 \sqrt{2}}} \sqrt{\frac{-3+2 \sqrt{2}+17 \tan \left[\frac{1}{4}(c+d x)\right]^2-12 \sqrt{2} \tan \left[\frac{1}{4}(c+d x)\right]^2}{-3+2 \sqrt{2}}} \sqrt{1-3 \tan \left[\frac{1}{4}(c+d x)\right]^2+2 \sqrt{2} \tan \left[\frac{1}{4}(c+d x)\right]^2} \left(2-2 \tan \left[\frac{1}{4}(c+d x)\right]^2+\sqrt{2} \sqrt{1-6 \tan \left[\frac{1}{4}(c+d x)\right]^2+\tan \left[\frac{1}{4}(c+d x)\right]^4}\right) \left(4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2} \right) \sqrt{1+(-3+2 \sqrt{2}) \tan \left[\frac{1}{4}(c+d x)\right]^2} \sqrt{1-6 \tan \left[\frac{1}{4}(c+d x)\right]^2+\tan \left[\frac{1}{4}(c+d x)\right]^4} +$$

$$\begin{aligned}
 & 8 \operatorname{EllipticPi} \left[-3 + 2\sqrt{2}, -\operatorname{ArcSin} \left[\frac{\operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]}{\sqrt{3 - 2\sqrt{2}}} \right], 17 - 12\sqrt{2} \right] \\
 & \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \\
 & \sqrt{1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^4} - \sqrt{2} \left(\operatorname{Log} \left[1 + \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 \right] - \right. \\
 & \left. \operatorname{Log} \left[2 - 2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + \sqrt{2} \sqrt{1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^4} \right] \right) \\
 & \left. \left(1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^4 \right) \right) \Bigg) / \\
 & \left(2d \left(\operatorname{Cos} \left[\frac{1}{2} (c + dx) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + dx) \right] \right) \sqrt{a (1 + \operatorname{Sin} [c + dx])} \right. \\
 & \left(-4 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 + 3\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 + 52 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 - \right. \\
 & 39\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 - 200 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^4 + \\
 & 150\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^4 + 200 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^6 - \\
 & 150\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^6 - 52 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^8 + \\
 & 39\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^8 + 4 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^{10} - \\
 & \left. 3\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^{10} + 2\sqrt{2(3 - 2\sqrt{2})} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \right. \\
 & \left. \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right] \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{-3 + 2\sqrt{2}}} \right. \\
 & \left. \sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 - 12\sqrt{2} \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{-3 + 2\sqrt{2}}} \right. \\
 & \left. \sqrt{1 - 3 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + 2\sqrt{2} \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} - 12\sqrt{2(3 - 2\sqrt{2})} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
& \tan\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2} + 2\sqrt{2(3-2\sqrt{2})} \sec\left[\frac{1}{4}(c+dx)\right]^2 \\
& \tan\left[\frac{1}{4}(c+dx)\right]^5 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
& \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
& \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2} + \\
& 6\sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
& 4\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
& 48\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
& 32\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
& 84\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
& 56\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
& 48\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
& 32\sqrt{2}\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} +
\end{aligned}$$

$$\begin{aligned}
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \\
 & \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} - 4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \left. \left. \left. \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} \right) \right) \right)
 \end{aligned}$$

Problem 300: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{e \operatorname{Cos}[c+dx]}}{\sqrt{a+a \operatorname{Sin}[c+dx]}} dx$$

Optimal (type 3, 169 leaves, 6 steps):

$$\frac{2 \sqrt{e} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos [c+d x]}}{\sqrt{e}}\right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{d\left(a+a \cos [c+d x]+a \sin [c+d x]\right)} +$$

$$\left(\frac{2 \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin [c+d x]}{\sqrt{e \cos [c+d x]} \sqrt{1+\cos [c+d x]}}\right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{d\left(a+a \cos [c+d x]+a \sin [c+d x]\right)}\right) /$$

Result (type 4, 2607 leaves):

$$\left(\sqrt{3-2 \sqrt{2}} \sqrt{e \cos [c+d x]} \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}\left(1+\tan \left[\frac{1}{4}(c+d x)\right]^2\right)\right.$$

$$\sqrt{\frac{-3+2 \sqrt{2}+\tan \left[\frac{1}{4}(c+d x)\right]^2}{-3+2 \sqrt{2}}}\sqrt{\frac{-3+2 \sqrt{2}+17 \tan \left[\frac{1}{4}(c+d x)\right]^2-12 \sqrt{2} \tan \left[\frac{1}{4}(c+d x)\right]^2}{-3+2 \sqrt{2}}}$$

$$\sqrt{1-3 \tan \left[\frac{1}{4}(c+d x)\right]^2+2 \sqrt{2} \tan \left[\frac{1}{4}(c+d x)\right]^2}$$

$$\left(2-2 \tan \left[\frac{1}{4}(c+d x)\right]^2+\sqrt{2} \sqrt{1-6 \tan \left[\frac{1}{4}(c+d x)\right]^2+\tan \left[\frac{1}{4}(c+d x)\right]^4}\right)$$

$$\left(4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2}\right.$$

$$\sqrt{1+(-3+2 \sqrt{2}) \tan \left[\frac{1}{4}(c+d x)\right]^2} \sqrt{1-6 \tan \left[\frac{1}{4}(c+d x)\right]^2+\tan \left[\frac{1}{4}(c+d x)\right]^4} +$$

$$8 \operatorname{EllipticPi}\left[-3+2 \sqrt{2},-\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x)\right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right]$$

$$\sqrt{3-2 \sqrt{2}-\tan \left[\frac{1}{4}(c+d x)\right]^2} \sqrt{1+(-3+2 \sqrt{2}) \tan \left[\frac{1}{4}(c+d x)\right]^2}$$

$$\sqrt{1-6 \tan \left[\frac{1}{4}(c+d x)\right]^2+\tan \left[\frac{1}{4}(c+d x)\right]^4} + \sqrt{2}\left(\operatorname{Log}\left[1+\tan \left[\frac{1}{4}(c+d x)\right]^2\right]-\right.$$

$$\left.\operatorname{Log}\left[2-2 \tan \left[\frac{1}{4}(c+d x)\right]^2+\sqrt{2} \sqrt{1-6 \tan \left[\frac{1}{4}(c+d x)\right]^2+\tan \left[\frac{1}{4}(c+d x)\right]^4}\right]\right)$$

$$\left. \left(1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4 \right) \right) \Bigg/ \left(d \sqrt{a(1+\sin[c+dx])} \right)$$

$$\left(4 \sec\left[\frac{1}{4}(c+dx)\right]^2 - 3\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 - 52 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \right.$$

$$39\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 + 200 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 -$$

$$150\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 - 200 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 +$$

$$150\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 + 52 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^8 -$$

$$39\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^8 - 4 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^{10} +$$

$$3\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^{10} + 2\sqrt{2(3-2\sqrt{2})} \sec\left[\frac{1}{4}(c+dx)\right]^2$$

$$\tan\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}}$$

$$\sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}}$$

$$\sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2(3-2\sqrt{2})}\sec\left[\frac{1}{4}(c+dx)\right]^2}$$

$$\tan\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}}$$

$$\sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}}$$

$$\sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2(3-2\sqrt{2})}\sec\left[\frac{1}{4}(c+dx)\right]^2}$$

$$\tan\left[\frac{1}{4}(c+dx)\right]^5 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}}$$

$$\sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}}$$

$$\begin{aligned}
 & \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} - \\
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} + \\
 & 4\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} + \\
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} - \\
 & 32\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} - \\
 & 84 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} + \\
 & 56\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} + \\
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^6 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} - \\
 & 32\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^6 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} - \\
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} + \\
 & 4\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^8 \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} + \\
 & 4\sqrt{3 - 2\sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right] \\
 & \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\
 & \sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \\
 & \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4 - 4\sqrt{3 - 2\sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2} \\
 & \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^3 \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\
 & \sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\
 & \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \\
 & \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} \Bigg)
 \end{aligned}$$

Problem 305: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \operatorname{Cos}[c + dx])^{7/2}}{(a + a \operatorname{Sin}[c + dx])^{3/2}} dx$$

Optimal (type 3, 247 leaves, 8 steps):

$$\begin{aligned}
 & \frac{e (e \operatorname{Cos}[c + dx])^{5/2}}{2 a d \sqrt{a + a \operatorname{Sin}[c + dx]}} + \frac{5 e^3 \sqrt{e \operatorname{Cos}[c + dx]} \sqrt{a + a \operatorname{Sin}[c + dx]}}{4 a^2 d} - \\
 & \frac{5 e^{7/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \operatorname{Cos}[c + dx]}}{\sqrt{e}}\right] \sqrt{1 + \operatorname{Cos}[c + dx]} \sqrt{a + a \operatorname{Sin}[c + dx]}}{4 a^2 d (1 + \operatorname{Cos}[c + dx] + \operatorname{Sin}[c + dx])} + \\
 & \left(\frac{5 e^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \operatorname{Sin}[c + dx]}{\sqrt{e \operatorname{Cos}[c + dx]} \sqrt{1 + \operatorname{Cos}[c + dx]}}\right] \sqrt{1 + \operatorname{Cos}[c + dx]} \sqrt{a + a \operatorname{Sin}[c + dx]}}{(4 a^2 d (1 + \operatorname{Cos}[c + dx] + \operatorname{Sin}[c + dx]))} \right) /
 \end{aligned}$$

Result (type 4, 2786 leaves):

$$\begin{aligned}
 & \left((e \operatorname{Cos}[c + dx])^{7/2} \operatorname{Sec}[c + dx]^3 \left(\operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] \right)^3 \right. \\
 & \left. \left(\frac{3}{2} \operatorname{Cos}\left[\frac{1}{2}(c + dx)\right] + \frac{1}{4} \operatorname{Cos}\left[\frac{3}{2}(c + dx)\right] + \frac{3}{2} \operatorname{Sin}\left[\frac{1}{2}(c + dx)\right] - \frac{1}{4} \operatorname{Sin}\left[\frac{3}{2}(c + dx)\right] \right) \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(d \left(a \left(1 + \sin [c + d x] \right) \right)^{3/2} \right) - \left(5 \sqrt{3 - 2 \sqrt{2}} \left(e \cos [c + d x] \right)^{7/2} \sec [c + d x]^3 \right. \\
 & \left. \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3 \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} \left(1 + \tan \left[\frac{1}{4} (c + d x) \right]^2 \right) \right. \\
 & \sqrt{\frac{-3 + 2 \sqrt{2} + \tan \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan \left[\frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \tan \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\
 & \sqrt{1 - 3 \tan \left[\frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \tan \left[\frac{1}{4} (c + d x) \right]^2} \\
 & \left(2 - 2 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \sqrt{2} \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} \right) \\
 & \left(4 \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} \right. \\
 & \left. \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} + \right. \\
 & \left. 8 \operatorname{EllipticPi} \left[-3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \right. \\
 & \left. \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[\frac{1}{4} (c + d x) \right]^2} \right. \\
 & \left. \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} - \sqrt{2} \left(\log \left[1 + \tan \left[\frac{1}{4} (c + d x) \right]^2 \right] - \right. \right. \\
 & \left. \left. \log \left[2 - 2 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \sqrt{2} \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} \right] \right) \right) \\
 & \left. \left(1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4 \right) \right) \Bigg) / \\
 & \left(8 d \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right) \left(a \left(1 + \sin [c + d x] \right) \right)^{3/2} \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(-4 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 + 3\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 + 52 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 - \right. \\
 & 39\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 - 200 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 + \\
 & 150\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 + 200 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 - \\
 & 150\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 - 52 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 + \\
 & 39\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 + 4 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^{10} - \\
 & \left. 3\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^{10} + 2\sqrt{2(3-2\sqrt{2})} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \right. \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}-12\sqrt{2(3-2\sqrt{2})}\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}+2\sqrt{2(3-2\sqrt{2})}\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^5 \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \left. \sqrt{1-3\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 32 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 84 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 56 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 32 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \\
 & \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}
 \end{aligned}$$

$$\begin{aligned} & \sqrt{1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} - 4\sqrt{3-2\sqrt{2}} \sec\left[\frac{1}{4}(c+dx)\right]^2 \\ & \tan\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2} + \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\ & \sqrt{\frac{-3+2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c+dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\ & \sqrt{1 - 3 \tan\left[\frac{1}{4}(c+dx)\right]^2 + 2\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2} \\ & \left. \sqrt{1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} \right) \end{aligned}$$

Problem 306: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c+dx])^{5/2}}{(a+a \sin[c+dx])^{3/2}} dx$$

Optimal (type 3, 215 leaves, 7 steps):

$$\begin{aligned} & \frac{e (e \cos[c+dx])^{3/2}}{a d \sqrt{a+a \sin[c+dx]}} + \frac{3 e^{5/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c+dx]}}{\sqrt{e}}\right] \sqrt{1+\cos[c+dx]} \sqrt{a+a \sin[c+dx]}}{d (a^2+a^2 \cos[c+dx]+a^2 \sin[c+dx])} + \\ & \left(\frac{3 e^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c+dx]}{\sqrt{e \cos[c+dx]} \sqrt{1+\cos[c+dx]}}\right] \sqrt{1+\cos[c+dx]} \sqrt{a+a \sin[c+dx]}}{d (a^2+a^2 \cos[c+dx]+a^2 \sin[c+dx])} \right) / \end{aligned}$$

Result (type 4, 2726 leaves):

$$\begin{aligned} & \left((e \cos[c+dx])^{5/2} \sec[c+dx]^2 \left(\cos\left[\frac{1}{2}(c+dx)\right] - \sin\left[\frac{1}{2}(c+dx)\right] \right) \right. \\ & \left. \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^3 \right) / (d (a (1+\sin[c+dx]))^{3/2}) + \\ & \left(3\sqrt{3-2\sqrt{2}} (e \cos[c+dx])^{5/2} \sec[c+dx]^2 \left(\cos\left[\frac{1}{2}(c+dx)\right] + \sin\left[\frac{1}{2}(c+dx)\right] \right)^2 \right. \\ & \left. \sqrt{3-2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \left(1 + \tan\left[\frac{1}{4}(c+dx)\right]^2 \right) \sqrt{\frac{-3+2\sqrt{2} + \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \right) \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\
 & \sqrt{1 - 3 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \\
 & \left(2 - 2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \sqrt{2} \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4}\right) \\
 & \left(4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}\right. \\
 & \left. \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} + \right. \\
 & \left. 8 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right. \\
 & \left. \sqrt{3 - 2\sqrt{2} - \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2}\right. \\
 & \left. \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4} + \sqrt{2} \left(\operatorname{Log}\left[1 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2\right] - \right. \right. \\
 & \left. \left. \operatorname{Log}\left[2 - 2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \sqrt{2} \sqrt{1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4}\right]\right) \right. \\
 & \left. \left. \left(1 - 6 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4\right)\right)\right) \Bigg/ \left(2d(a(1 + \operatorname{Sin}[c + dx]))^{3/2}\right) \\
 & \left(4 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 - 3\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 - 52 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + \right. \\
 & 39\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^2 + 200 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4 - \\
 & 150\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^4 - 200 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^6 + \\
 & 150\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^6 + 52 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^8 - \\
 & \left. 39\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^8 - 4 \operatorname{Sec}\left[\frac{1}{4}(c + dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c + dx)\right]^{10} + \right.
 \end{aligned}$$

$$\begin{aligned}
 & 3\sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^{10} + 2\sqrt{2(3-2\sqrt{2})} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2(3-2\sqrt{2})}\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2(3-2\sqrt{2})}\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^5 \sqrt{3-2\sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} - \\
 & 6\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 4\sqrt{2}\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 48\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 32\sqrt{2}\operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} -
 \end{aligned}$$

$$\begin{aligned}
 & 84 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 56 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 32 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \\
 & \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}-4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}
 \end{aligned}$$

$$\sqrt{1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4}$$

Problem 307: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c + dx])^{3/2}}{(a + a \sin[c + dx])^{3/2}} dx$$

Optimal (type 3, 236 leaves, 8 steps):

$$\begin{aligned} & - \frac{2 (e \cos[c + dx])^{5/2}}{d e (a + a \sin[c + dx])^{3/2}} - \frac{2 e \sqrt{e \cos[c + dx]} \sqrt{a + a \sin[c + dx]}}{a^2 d} + \\ & \frac{2 e^{3/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos[c + dx]}}{\sqrt{e}}\right] \sqrt{1 + \cos[c + dx]} \sqrt{a + a \sin[c + dx]}}{a^2 d (1 + \cos[c + dx] + \sin[c + dx])} - \\ & \left(\frac{2 e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin[c + dx]}{\sqrt{e \cos[c + dx]} \sqrt{1 + \cos[c + dx]}}\right] \sqrt{1 + \cos[c + dx]} \sqrt{a + a \sin[c + dx]}}{a^2 d (1 + \cos[c + dx] + \sin[c + dx])} \right) / \end{aligned}$$

Result (type 4, 2723 leaves):

$$\begin{aligned} & - \left(\left(4 (e \cos[c + dx])^{3/2} \sec[c + dx] \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^2 \right) / \right. \\ & \quad \left. (d (a (1 + \sin[c + dx]))^{3/2}) \right) + \\ & \left(\sqrt{3 - 2\sqrt{2}} (e \cos[c + dx])^{3/2} \sec[c + dx] \left(\cos\left[\frac{1}{2}(c + dx)\right] + \sin\left[\frac{1}{2}(c + dx)\right] \right)^3 \right. \\ & \quad \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \left(1 + \tan\left[\frac{1}{4}(c + dx)\right]^2 \right) \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\ & \quad \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\ & \quad \sqrt{1 - 3 \tan\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \tan\left[\frac{1}{4}(c + dx)\right]^2} \\ & \quad \left. \left(2 - 2 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4} \right) \right) \end{aligned}$$

$$\begin{aligned}
& \left(4 \operatorname{EllipticF} \left[\operatorname{ArcSin} \left[\frac{\operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \right. \\
& \sqrt{1 + (-3 + 2 \sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^4} + \\
& 8 \operatorname{EllipticPi} \left[-3 + 2 \sqrt{2}, -\operatorname{ArcSin} \left[\frac{\operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \\
& \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 + (-3 + 2 \sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \\
& \sqrt{1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^4} - \sqrt{2} \left(\operatorname{Log} \left[1 + \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 \right] - \right. \\
& \left. \operatorname{Log} \left[2 - 2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 + \sqrt{2} \sqrt{1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^4} \right] \right) \\
& \left. \left(1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^4 \right) \right) \Bigg/ \\
& \left(d \left(\operatorname{Cos} \left[\frac{1}{2} (c + d x) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + d x) \right] \right) (a (1 + \operatorname{Sin} [c + d x]))^{3/2} \right. \\
& \left(-4 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 + 3 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 + 52 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 - \right. \\
& 39 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2 - 200 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^4 + \\
& 150 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^4 + 200 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^6 - \\
& 150 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^6 - 52 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^8 + \\
& 39 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^8 + 4 \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^{10} - \\
& 3 \sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^{10} + 2 \sqrt{2 (3 - 2 \sqrt{2})} \operatorname{Sec} \left[\frac{1}{4} (c + d x) \right]^2 \\
& \left. \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right] \sqrt{3 - 2 \sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{\frac{-3 + 2 \sqrt{2} + \operatorname{Tan} \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \right)
\end{aligned}$$

$$\begin{aligned}
 & \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c+dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3 + 2\sqrt{2}}} \\
 & \sqrt{1 - 3 \tan\left[\frac{1}{4}(c+dx)\right]^2 + 2\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2 - 12\sqrt{2(3-2\sqrt{2})} \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \tan\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3 + 2\sqrt{2}}} \\
 & \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c+dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3 + 2\sqrt{2}}} \\
 & \sqrt{1 - 3 \tan\left[\frac{1}{4}(c+dx)\right]^2 + 2\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2 + 2\sqrt{2(3-2\sqrt{2})} \sec\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \tan\left[\frac{1}{4}(c+dx)\right]^5 \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3 + 2\sqrt{2}}} \\
 & \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c+dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3 + 2\sqrt{2}}} \\
 & \sqrt{1 - 3 \tan\left[\frac{1}{4}(c+dx)\right]^2 + 2\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2} + \\
 & 6 \sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 4\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 48 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 32\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 84 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} -
 \end{aligned}$$

$$\begin{aligned}
 & 56 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 48 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 32 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \\
 & \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}-4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4} \right)
 \end{aligned}$$

Problem 313: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{9/2}}{(a + a \sin [c + d x])^{5/2}} dx$$

Optimal (type 3, 261 leaves, 9 steps):

$$\frac{e (e \cos [c + d x])^{7/2}}{2 a d (a + a \sin [c + d x])^{3/2}} + \frac{7 e^3 (e \cos [c + d x])^{3/2}}{4 a^2 d \sqrt{a + a \sin [c + d x]}} +$$

$$\frac{21 e^{9/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos [c + d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos [c + d x]} \sqrt{a + a \sin [c + d x]}}{4 d (a^3 + a^3 \cos [c + d x] + a^3 \sin [c + d x])} +$$

$$\left(\frac{21 e^{9/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin [c + d x]}{\sqrt{e \cos [c + d x]}}\right] \sqrt{1 + \cos [c + d x]} \sqrt{a + a \sin [c + d x]}}{\sqrt{e \cos [c + d x]} \sqrt{1 + \cos [c + d x]}} \right) /$$

$$(4 d (a^3 + a^3 \cos [c + d x] + a^3 \sin [c + d x]))$$

Result (type 4, 2330 leaves):

$$\left((e \cos [c + d x])^{9/2} \operatorname{Sec}[c + d x]^4 \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^5 \right.$$

$$\left. \left(\frac{5}{2} \cos\left[\frac{1}{2}(c + d x)\right] - \frac{1}{4} \cos\left[\frac{3}{2}(c + d x)\right] - \frac{5}{2} \sin\left[\frac{1}{2}(c + d x)\right] - \frac{1}{4} \sin\left[\frac{3}{2}(c + d x)\right] \right) \right) /$$

$$\left(d (a (1 + \sin [c + d x]))^{5/2} \right) - \left(441 \cos\left[\frac{1}{4}(c + d x)\right]^2 (e \cos [c + d x])^{9/2} \right.$$

$$\left. \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right] \right)^4 \left(\sqrt{2} \left(\operatorname{Log}\left[\operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^2\right] - \right. \right. \right.$$

$$\left. \left. \operatorname{Log}\left[2 + \sqrt{2} \sqrt{\cos [c + d x] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^4 - 2 \tan\left[\frac{1}{4}(c + d x)\right]^2}\right] \right) \right.$$

$$\left. \sqrt{\cos [c + d x] \operatorname{Sec}\left[\frac{1}{4}(c + d x)\right]^4} + 4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right.$$

$$\left. \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + d x)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c + d x)\right]^2} + \right.$$

$$\left. 8 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + d x)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right)$$

$$\begin{aligned}
 & \left. \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) / \\
 & \left(64 d \cos[c + dx]^{9/2} (a (1 + \sin[c + dx]))^{5/2} \right. \\
 & \left. \left(\frac{1}{16 \sqrt{\cos[c + dx]}} 21 \cos\left[\frac{1}{4}(c + dx)\right] \sin\left[\frac{1}{4}(c + dx)\right] \left(\sqrt{2} \left(\log\left[\sec\left[\frac{1}{4}(c + dx)\right]^2\right] - \right. \right. \right. \right. \\
 & \left. \left. \left. \log\left[2 + \sqrt{2} \sqrt{\cos[c + dx] \sec\left[\frac{1}{4}(c + dx)\right]^4 - 2 \tan\left[\frac{1}{4}(c + dx)\right]^2}\right] \right) \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\cos[c + dx] \sec\left[\frac{1}{4}(c + dx)\right]^4} + 4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], \right. \right. \right. \\
 & \left. \left. \left. 17 - 12\sqrt{2} \right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c + dx)\right]^2} + \right. \right. \\
 & \left. \left. \left. 8 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2} \right] \right) \right. \right. \\
 & \left. \left. \left. \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c + dx)\right]^2} \right) - \right. \right. \\
 & \left. \left. \left. \frac{1}{16 \cos[c + dx]^{3/2}} 21 \cos\left[\frac{1}{4}(c + dx)\right]^2 \sin[c + dx] \left(\sqrt{2} \left(\log\left[\sec\left[\frac{1}{4}(c + dx)\right]^2\right] - \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \log\left[2 + \sqrt{2} \sqrt{\cos[c + dx] \sec\left[\frac{1}{4}(c + dx)\right]^4 - 2 \tan\left[\frac{1}{4}(c + dx)\right]^2}\right] \right) \right) \right. \right. \\
 & \left. \left. \left. \sqrt{\cos[c + dx] \sec\left[\frac{1}{4}(c + dx)\right]^4} + 4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], \right. \right. \right. \\
 & \left. \left. \left. 17 - 12\sqrt{2} \right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c + dx)\right]^2} + \right. \right. \\
 & \left. \left. \left. 8 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c + dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2} \right] \right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c+dx)\right]^2} \right) - \\
 & \frac{1}{8\sqrt{\cos[c+dx]}} 21 \cos\left[\frac{1}{4}(c+dx)\right]^2 \left(\left(\left(\log\left[\sec\left[\frac{1}{4}(c+dx)\right]^2\right] - \log\left[\right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. 2 + \sqrt{2} \sqrt{\cos[c+dx] \sec\left[\frac{1}{4}(c+dx)\right]^4 - 2 \tan\left[\frac{1}{4}(c+dx)\right]^2} \right) \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \left(-\sec\left[\frac{1}{4}(c+dx)\right]^4 \sin[c+dx] + \cos[c+dx] \sec\left[\frac{1}{4}(c+dx)\right]^4 \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \tan\left[\frac{1}{4}(c+dx)\right] \right) \right) \right) \right) / \left(\sqrt{2} \sqrt{\cos[c+dx] \sec\left[\frac{1}{4}(c+dx)\right]^4} \right) + \\
 & \left((-3 + 2\sqrt{2}) \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right. \\
 & \left. \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right] \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \\
 & \left(\sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c+dx)\right]^2} \right) + \left(2(-3 + 2\sqrt{2}) \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, \right. \right. \\
 & \left. \left. -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right] \right. \\
 & \left. \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \left(\sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c+dx)\right]^2} \right) - \\
 & \left(\operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right] \right. \\
 & \left. \sqrt{1 + (-3 + 2\sqrt{2}) \tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \left(\sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \right) - \\
 & \left(2 \operatorname{EllipticPi}\left[-3 + 2\sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan\left[\frac{1}{4}(c+dx)\right]}{\sqrt{3 - 2\sqrt{2}}}\right], 17 - 12\sqrt{2}\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right] \sqrt{1+(-3+2\sqrt{2})\tan\left[\frac{1}{4}(c+dx)\right]^2} \right/ \\
 & \left(\sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \right) + \left(\sec\left[\frac{1}{4}(c+dx)\right]^2 \right. \\
 & \left. \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{1+(-3+2\sqrt{2})\tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \\
 & \left(\sqrt{3-2\sqrt{2}} \sqrt{1-\frac{\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \sqrt{1-\frac{(17-12\sqrt{2})\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \right) - \\
 & \left(2 \sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \right. \\
 & \left. \sqrt{1+(-3+2\sqrt{2})\tan\left[\frac{1}{4}(c+dx)\right]^2} \right) / \left(\sqrt{3-2\sqrt{2}} \sqrt{1-\frac{\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \right. \\
 & \left. \sqrt{1-\frac{(17-12\sqrt{2})\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}}} \left(1-\frac{(-3+2\sqrt{2})\tan\left[\frac{1}{4}(c+dx)\right]^2}{3-2\sqrt{2}} \right) \right) + \\
 & \sqrt{2} \sqrt{\cos[c+dx] \sec\left[\frac{1}{4}(c+dx)\right]^4} \left(\frac{1}{2} \tan\left[\frac{1}{4}(c+dx)\right] - \left(-\sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right] \right. \right. \\
 & \left. \left. + \left(-\sec\left[\frac{1}{4}(c+dx)\right]^4 \sin[c+dx] + \cos[c+dx] \sec\left[\frac{1}{4}(c+dx)\right]^4 \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}(c+dx)\right] \right) \right) / \left(\sqrt{2} \sqrt{\cos[c+dx] \sec\left[\frac{1}{4}(c+dx)\right]^4} \right) \right) / \\
 & \left(2 + \sqrt{2} \sqrt{\cos[c+dx] \sec\left[\frac{1}{4}(c+dx)\right]^4 - 2 \tan\left[\frac{1}{4}(c+dx)\right]^2} \right) \right) \right) \right) \right)
 \end{aligned}$$

Problem 314: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{7/2}}{(a + a \sin [c + d x])^{5/2}} dx$$

Optimal (type 3, 239 leaves, 8 steps):

$$\begin{aligned} & -\frac{4 e (e \cos [c + d x])^{5/2}}{a d (a + a \sin [c + d x])^{3/2}} - \frac{5 e^3 \sqrt{e \cos [c + d x]} \sqrt{a + a \sin [c + d x]}}{a^3 d} + \\ & \frac{5 e^{7/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos [c + d x]}}{\sqrt{e}}\right] \sqrt{1 + \cos [c + d x]} \sqrt{a + a \sin [c + d x]}}{a^3 d (1 + \cos [c + d x] + \sin [c + d x])} - \\ & \left(\frac{5 e^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin [c + d x]}{\sqrt{e \cos [c + d x]} \sqrt{1 + \cos [c + d x]}}\right] \sqrt{1 + \cos [c + d x]} \sqrt{a + a \sin [c + d x]}}{a^3 d (1 + \cos [c + d x] + \sin [c + d x])} \right) / \end{aligned}$$

Result (type 4, 2779 leaves):

$$\begin{aligned} & \left((e \cos [c + d x])^{7/2} \sec [c + d x]^3 \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^5 \right. \\ & \left. \left(-\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] - \frac{8}{\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right]} \right) \right) / \\ & \left(d (a (1 + \sin [c + d x]))^{5/2} \right) + \left(5 \sqrt{3 - 2 \sqrt{2}} (e \cos [c + d x])^{7/2} \sec [c + d x]^3 \right. \\ & \left. \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^5 \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} \left(1 + \tan \left[\frac{1}{4} (c + d x) \right] \right)^2 \right) \\ & \sqrt{\frac{-3 + 2 \sqrt{2} + \tan \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \sqrt{\frac{-3 + 2 \sqrt{2} + 17 \tan \left[\frac{1}{4} (c + d x) \right]^2 - 12 \sqrt{2} \tan \left[\frac{1}{4} (c + d x) \right]^2}{-3 + 2 \sqrt{2}}} \\ & \sqrt{1 - 3 \tan \left[\frac{1}{4} (c + d x) \right]^2 + 2 \sqrt{2} \tan \left[\frac{1}{4} (c + d x) \right]^2} \\ & \left(2 - 2 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \sqrt{2} \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} \right) \\ & \left(4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4} (c + d x) \right]}{\sqrt{3 - 2 \sqrt{2}}} \right], 17 - 12 \sqrt{2} \right] \sqrt{3 - 2 \sqrt{2} - \tan \left[\frac{1}{4} (c + d x) \right]^2} \right. \\ & \left. \sqrt{1 + (-3 + 2 \sqrt{2}) \tan \left[\frac{1}{4} (c + d x) \right]^2} \sqrt{1 - 6 \tan \left[\frac{1}{4} (c + d x) \right]^2 + \tan \left[\frac{1}{4} (c + d x) \right]^4} + \right. \end{aligned}$$

$$\begin{aligned}
 & 8 \operatorname{EllipticPi} \left[-3 + 2\sqrt{2}, -\operatorname{ArcSin} \left[\frac{\operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]}{\sqrt{3 - 2\sqrt{2}}} \right], 17 - 12\sqrt{2} \right] \\
 & \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \sqrt{1 + (-3 + 2\sqrt{2}) \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \\
 & \sqrt{1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^4} - \sqrt{2} \left(\operatorname{Log} \left[1 + \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 \right] - \right. \\
 & \left. \operatorname{Log} \left[2 - 2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + \sqrt{2} \sqrt{1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^4} \right] \right) \\
 & \left. \left(1 - 6 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^4 \right) \right) \Bigg) / \\
 & \left(2d \left(\operatorname{Cos} \left[\frac{1}{2} (c + dx) \right] - \operatorname{Sin} \left[\frac{1}{2} (c + dx) \right] \right) (a (1 + \operatorname{Sin} [c + dx]))^{5/2} \right. \\
 & \left. \left(-4 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 + 3\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 + 52 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 - \right. \right. \\
 & 39\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 - 200 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^4 + \\
 & 150\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^4 + 200 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^6 - \\
 & 150\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^6 - 52 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^8 + \\
 & 39\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^8 + 4 \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^{10} - \\
 & \left. 3\sqrt{2} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^{10} + 2\sqrt{2(3 - 2\sqrt{2})} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \right. \\
 & \left. \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right] \sqrt{3 - 2\sqrt{2} - \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{-3 + 2\sqrt{2}}} \right. \\
 & \left. \sqrt{\frac{-3 + 2\sqrt{2} + 17 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 - 12\sqrt{2} \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2}{-3 + 2\sqrt{2}}} \right. \\
 & \left. \sqrt{1 - 3 \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2 + 2\sqrt{2} \operatorname{Tan} \left[\frac{1}{4} (c + dx) \right]^2} - 12\sqrt{2(3 - 2\sqrt{2})} \operatorname{Sec} \left[\frac{1}{4} (c + dx) \right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2} + 2\sqrt{2(3-2\sqrt{2})} \sec\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \tan\left[\frac{1}{4}(c+dx)\right]^5 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2} + \\
 & 6 \sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 4\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 48 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 32\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 84 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 56\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 48 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 32\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} +
 \end{aligned}$$

$$\begin{aligned}
 & 6 \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}- \\
 & 4 \sqrt{2} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}+ \\
 & 4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right] \\
 & \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}-4 \sqrt{3-2 \sqrt{2}} \operatorname{Sec}\left[\frac{1}{4}(c+dx)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2 \sqrt{2}-\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2 \sqrt{2}+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{\frac{-3+2 \sqrt{2}+17 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2-12 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+2 \sqrt{2} \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2} \\
 & \left. \left. \left. \sqrt{1-6 \operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^2+\operatorname{Tan}\left[\frac{1}{4}(c+dx)\right]^4}\right)\right)\right)
 \end{aligned}$$

Problem 315: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \operatorname{Cos}[c+dx])^{5/2}}{(a+a \operatorname{Sin}[c+dx])^{5/2}} dx$$

Optimal (type 3, 218 leaves, 7 steps):

$$\begin{aligned}
 & - \frac{4 e (e \cos [c+d x])^{3/2}}{3 a d (a+a \sin [c+d x])^{3/2}} - \frac{2 e^{5/2} \operatorname{ArcSinh}\left[\frac{\sqrt{e \cos [c+d x]}}{\sqrt{e}}\right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{d\left(a^3+a^3 \cos [c+d x]+a^3 \sin [c+d x]\right)} \\
 & \left(\frac{2 e^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{e} \sin [c+d x]}{\sqrt{e \cos [c+d x]} \sqrt{1+\cos [c+d x]}}\right] \sqrt{1+\cos [c+d x]} \sqrt{a+a \sin [c+d x]}}{d\left(a^3+a^3 \cos [c+d x]+a^3 \sin [c+d x]\right)} \right) /
 \end{aligned}$$

Result (type 4, 2766 leaves):

$$\begin{aligned}
 & \left((e \cos [c+d x])^{5/2} \operatorname{Sec}[c+d x]^2 \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^5 \right. \\
 & \left. \left(\frac{8 \sin \left[\frac{1}{2}(c+d x) \right]}{3 \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^2} - \frac{4}{3 \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)} \right) \right) / \\
 & \left(d (a (1 + \sin [c+d x]))^{5/2} \right) - \sqrt{3-2 \sqrt{2}} (e \cos [c+d x])^{5/2} \operatorname{Sec}[c+d x]^2 \\
 & \left(\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right)^4 \sqrt{3-2 \sqrt{2} - \tan \left[\frac{1}{4}(c+d x) \right]^2} \left(1 + \tan \left[\frac{1}{4}(c+d x) \right]^2 \right) \\
 & \sqrt{\frac{-3+2 \sqrt{2} + \tan \left[\frac{1}{4}(c+d x) \right]^2}{-3+2 \sqrt{2}}} \sqrt{\frac{-3+2 \sqrt{2} + 17 \tan \left[\frac{1}{4}(c+d x) \right]^2 - 12 \sqrt{2} \tan \left[\frac{1}{4}(c+d x) \right]^2}{-3+2 \sqrt{2}}} \\
 & \sqrt{1-3 \tan \left[\frac{1}{4}(c+d x) \right]^2 + 2 \sqrt{2} \tan \left[\frac{1}{4}(c+d x) \right]^2} \\
 & \left(2 - 2 \tan \left[\frac{1}{4}(c+d x) \right]^2 + \sqrt{2} \sqrt{1-6 \tan \left[\frac{1}{4}(c+d x) \right]^2 + \tan \left[\frac{1}{4}(c+d x) \right]^4} \right) \\
 & \left(4 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x) \right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \sqrt{3-2 \sqrt{2} - \tan \left[\frac{1}{4}(c+d x) \right]^2} \right. \\
 & \left. \sqrt{1+(-3+2 \sqrt{2}) \tan \left[\frac{1}{4}(c+d x) \right]^2} \sqrt{1-6 \tan \left[\frac{1}{4}(c+d x) \right]^2 + \tan \left[\frac{1}{4}(c+d x) \right]^4} + \right. \\
 & \left. 8 \operatorname{EllipticPi}\left[-3+2 \sqrt{2}, -\operatorname{ArcSin}\left[\frac{\tan \left[\frac{1}{4}(c+d x) \right]}{\sqrt{3-2 \sqrt{2}}}\right], 17-12 \sqrt{2}\right] \right) \\
 & \sqrt{3-2 \sqrt{2} - \tan \left[\frac{1}{4}(c+d x) \right]^2} \sqrt{1+(-3+2 \sqrt{2}) \tan \left[\frac{1}{4}(c+d x) \right]^2}
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4} + \sqrt{2} \left(\log\left[1 + \tan\left[\frac{1}{4}(c+dx)\right]^2\right] - \right. \\
 & \left. \log\left[2 - 2 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \sqrt{2} \sqrt{1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4}\right]\right) \\
 & \left. \left(1 - 6 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \tan\left[\frac{1}{4}(c+dx)\right]^4\right)\right) \Bigg) / \left(d (a (1 + \sin[c+dx]))^{5/2} \right. \\
 & \left. \left(4 \sec\left[\frac{1}{4}(c+dx)\right]^2 - 3\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 - 52 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 + \right. \right. \\
 & 39\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 + 200 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 - \right. \\
 & 150\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 - 200 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 + \right. \\
 & 150\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 + 52 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^8 - \right. \\
 & 39\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^8 - 4 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^{10} + \right. \\
 & \left. 3\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^{10} + 2\sqrt{2(3-2\sqrt{2})} \sec\left[\frac{1}{4}(c+dx)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{4}(c+dx)\right] \sqrt{3-2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2} + \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \right. \\
 & \left. \sqrt{\frac{-3+2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c+dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \right. \\
 & \left. \sqrt{1 - 3 \tan\left[\frac{1}{4}(c+dx)\right]^2 + 2\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2} - 12\sqrt{2(3-2\sqrt{2})} \sec\left[\frac{1}{4}(c+dx)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{4}(c+dx)\right]^3 \sqrt{3-2\sqrt{2} - \tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2} + \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \right. \\
 & \left. \sqrt{\frac{-3+2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c+dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \right. \\
 & \left. \sqrt{1 - 3 \tan\left[\frac{1}{4}(c+dx)\right]^2 + 2\sqrt{2} \tan\left[\frac{1}{4}(c+dx)\right]^2} + 2\sqrt{2(3-2\sqrt{2})} \sec\left[\frac{1}{4}(c+dx)\right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}(c+dx)\right]^5 \sqrt{3-2\sqrt{2}-\tan\left[\frac{1}{4}(c+dx)\right]^2} \sqrt{\frac{-3+2\sqrt{2}+\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{\frac{-3+2\sqrt{2}+17\tan\left[\frac{1}{4}(c+dx)\right]^2-12\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2}{-3+2\sqrt{2}}} \\
 & \sqrt{1-3\tan\left[\frac{1}{4}(c+dx)\right]^2+2\sqrt{2}\tan\left[\frac{1}{4}(c+dx)\right]^2} - \\
 & 6 \sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 4\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 48 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 32\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^2 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 84 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 56\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^4 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 48 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 32\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^6 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} - \\
 & 6 \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 4\sqrt{2} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]^8 \sqrt{1-6\tan\left[\frac{1}{4}(c+dx)\right]^2+\tan\left[\frac{1}{4}(c+dx)\right]^4} + \\
 & 4\sqrt{3-2\sqrt{2}} \sec\left[\frac{1}{4}(c+dx)\right]^2 \tan\left[\frac{1}{4}(c+dx)\right]
 \end{aligned}$$

$$\begin{aligned} & \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\ & \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\ & \sqrt{1 - 3 \tan\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \tan\left[\frac{1}{4}(c + dx)\right]^2} \\ & \sqrt{1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4 - 4\sqrt{3 - 2\sqrt{2}} \sec\left[\frac{1}{4}(c + dx)\right]^2} \\ & \tan\left[\frac{1}{4}(c + dx)\right]^3 \sqrt{3 - 2\sqrt{2} - \tan\left[\frac{1}{4}(c + dx)\right]^2} \sqrt{\frac{-3 + 2\sqrt{2} + \tan\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\ & \sqrt{\frac{-3 + 2\sqrt{2} + 17 \tan\left[\frac{1}{4}(c + dx)\right]^2 - 12\sqrt{2} \tan\left[\frac{1}{4}(c + dx)\right]^2}{-3 + 2\sqrt{2}}} \\ & \sqrt{1 - 3 \tan\left[\frac{1}{4}(c + dx)\right]^2 + 2\sqrt{2} \tan\left[\frac{1}{4}(c + dx)\right]^2} \\ & \sqrt{1 - 6 \tan\left[\frac{1}{4}(c + dx)\right]^2 + \tan\left[\frac{1}{4}(c + dx)\right]^4} \right) \end{aligned}$$

Problem 327: Attempted integration timed out after 120 seconds.

$$\int (e \cos[c + dx])^p (a + a \sin[c + dx])^8 dx$$

Optimal (type 5, 95 leaves, 2 steps):

$$-\frac{1}{d e (1+p)} 2^{\frac{17+p}{2}} a^8 (e \cos[c + dx])^{1+p} \text{Hypergeometric2F1}\left[\frac{1}{2}(-15-p), \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2}(1 - \sin[c + dx])\right] (1 + \sin[c + dx])^{\frac{1}{2}(-1-p)}$$

Result (type 1, 1 leaves):

???

Problem 328: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (e \cos [c + d x])^p (a + a \sin [c + d x])^3 dx$$

Optimal (type 5, 95 leaves, 2 steps):

$$-\frac{1}{d e (1+p)} 2^{\frac{7+p}{2}} a^3 (e \cos [c + d x])^{1+p}$$

$$\text{Hypergeometric2F1}\left[\frac{1}{2}(-5-p), \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2}(1-\sin [c + d x])\right] (1 + \sin [c + d x])^{\frac{1}{2}(-1-p)}$$

Result (type 5, 462 leaves):

$$\frac{1}{d \left(\cos \left[\frac{1}{2}(c + d x)\right] + \sin \left[\frac{1}{2}(c + d x)\right]\right)^6} i 2^{-3-p} \left(e^{-i(c+d x)} + e^{i(c+d x)}\right)^p \left(1 + e^{2i(c+d x)}\right)^{-p} \cos [c + d x]^{-p}$$

$$(e \cos [c + d x])^p \left(-\frac{i e^{-3i(c+d x)} \text{Hypergeometric2F1}\left[-\frac{3}{2} - \frac{p}{2}, -p, -\frac{1}{2} - \frac{p}{2}, -e^{2i(c+d x)}\right]}{3+p} - \frac{6 e^{-2i(c+d x)} \text{Hypergeometric2F1}\left[-1 - \frac{p}{2}, -p, -\frac{p}{2}, -e^{2i(c+d x)}\right]}{2+p} + \frac{15 i e^{-i(c+d x)} \text{Hypergeometric2F1}\left[-\frac{1}{2} - \frac{p}{2}, -p, \frac{1}{2} - \frac{p}{2}, -e^{2i(c+d x)}\right]}{1+p} - \frac{15 i e^{i(c+d x)} \text{Hypergeometric2F1}\left[\frac{1}{2} - \frac{p}{2}, -p, \frac{3}{2} - \frac{p}{2}, -e^{2i(c+d x)}\right]}{-1+p} - \frac{6 e^{2i(c+d x)} \text{Hypergeometric2F1}\left[1 - \frac{p}{2}, -p, 2 - \frac{p}{2}, -e^{2i(c+d x)}\right]}{-2+p} + \frac{i e^{3i(c+d x)} \text{Hypergeometric2F1}\left[\frac{3}{2} - \frac{p}{2}, -p, \frac{5}{2} - \frac{p}{2}, -e^{2i(c+d x)}\right]}{-3+p} + \frac{20 \text{Hypergeometric2F1}\left[-p, -\frac{p}{2}, 1 - \frac{p}{2}, -e^{2i(c+d x)}\right]}{p} \right) (a + a \sin [c + d x])^3$$

Problem 329: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (e \cos [c + d x])^p (a + a \sin [c + d x])^2 dx$$

Optimal (type 5, 95 leaves, 2 steps):

$$-\frac{1}{d e (1+p)} 2^{\frac{5+p}{2}} a^2 (e \cos [c+d x])^{1+p}$$

$$\text{Hypergeometric2F1}\left[\frac{1}{2}(-3-p), \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2}(1-\sin [c+d x])\right] (1+\sin [c+d x])^{\frac{1}{2}(-1-p)}$$

Result (type 5, 351 leaves):

$$\frac{1}{d \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^4} 2^{-2-p} \left(e^{-i(c+d x)} + e^{i(c+d x)}\right)^p \left(1 + e^{2i(c+d x)}\right)^{-p} \cos [c+d x]^{-p}$$

$$(e \cos [c+d x])^p \left(-\frac{i e^{-2i(c+d x)} \text{Hypergeometric2F1}\left[-1-\frac{p}{2}, -p, -\frac{p}{2}, -e^{2i(c+d x)}\right]}{2+p} - \frac{4 e^{-i(c+d x)} \text{Hypergeometric2F1}\left[-\frac{1}{2}-\frac{p}{2}, -p, \frac{1}{2}-\frac{p}{2}, -e^{2i(c+d x)}\right]}{1+p} + \frac{4 e^{i(c+d x)} \text{Hypergeometric2F1}\left[\frac{1}{2}-\frac{p}{2}, -p, \frac{3}{2}-\frac{p}{2}, -e^{2i(c+d x)}\right]}{-1+p} - \frac{i e^{2i(c+d x)} \text{Hypergeometric2F1}\left[1-\frac{p}{2}, -p, 2-\frac{p}{2}, -e^{2i(c+d x)}\right]}{-2+p} + \frac{6 i \text{Hypergeometric2F1}\left[-p, -\frac{p}{2}, 1-\frac{p}{2}, -e^{2i(c+d x)}\right]}{p} \right) (a + a \sin [c+d x])^2$$

Problem 330: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (e \cos [c+d x])^p (a + a \sin [c+d x]) dx$$

Optimal (type 5, 93 leaves, 2 steps):

$$-\frac{1}{d e (1+p)} 2^{\frac{3+p}{2}} a (e \cos [c+d x])^{1+p}$$

$$\text{Hypergeometric2F1}\left[\frac{1}{2}(-1-p), \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2}(1-\sin [c+d x])\right] (1+\sin [c+d x])^{\frac{1}{2}(-1-p)}$$

Result (type 5, 266 leaves):

$$\frac{1}{d (-1+p) p (1+p) \left(\cos \left[\frac{1}{2}(c+d x)\right] + \sin \left[\frac{1}{2}(c+d x)\right]\right)^2} 2^{-1-p} a \left(1 + e^{2i(c+d x)}\right)^{-1-p} \left(e^{-i(c+d x)} \left(1 + e^{2i(c+d x)}\right)\right)^{1+p} \cos [c+d x]^{-p} (e \cos [c+d x])^p$$

$$\left(-(-1+p) p \text{Hypergeometric2F1}\left[\frac{1}{2}(-1-p), -p, \frac{1-p}{2}, -e^{2i(c+d x)}\right] + e^{i(c+d x)} (1+p) \left(e^{i(c+d x)} p \text{Hypergeometric2F1}\left[\frac{1-p}{2}, -p, \frac{3-p}{2}, -e^{2i(c+d x)}\right] + 2 i (-1+p) \text{Hypergeometric2F1}\left[-p, -\frac{p}{2}, 1-\frac{p}{2}, -e^{2i(c+d x)}\right] \right) \right) (1+\sin [c+d x])$$

Problem 331: Unable to integrate problem.

$$\int \frac{(e \cos [c + d x])^p}{a + a \sin [c + d x]} dx$$

Optimal (type 5, 95 leaves, 2 steps):

$$-\frac{1}{a d e (1+p)} 2^{-\frac{1+p}{2}} (e \cos [c + d x])^{1+p} \text{Hypergeometric2F1}\left[\frac{3-p}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 - \sin [c + d x])\right] (1 + \sin [c + d x])^{\frac{1}{2}(-1-p)}$$

Result (type 8, 25 leaves):

$$\int \frac{(e \cos [c + d x])^p}{a + a \sin [c + d x]} dx$$

Problem 332: Unable to integrate problem.

$$\int \frac{(e \cos [c + d x])^p}{(a + a \sin [c + d x])^2} dx$$

Optimal (type 5, 93 leaves, 2 steps):

$$-\frac{1}{a^2 d e (1+p)} 2^{\frac{1}{2}(-3+p)} (e \cos [c + d x])^{1+p} \text{Hypergeometric2F1}\left[\frac{5-p}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 - \sin [c + d x])\right] (1 + \sin [c + d x])^{\frac{1}{2}(-1-p)}$$

Result (type 8, 25 leaves):

$$\int \frac{(e \cos [c + d x])^p}{(a + a \sin [c + d x])^2} dx$$

Problem 333: Unable to integrate problem.

$$\int \frac{(e \cos [c + d x])^p}{(a + a \sin [c + d x])^3} dx$$

Optimal (type 5, 93 leaves, 2 steps):

$$-\frac{1}{a^3 d e (1+p)} 2^{\frac{1}{2}(-5+p)} (e \cos [c + d x])^{1+p} \text{Hypergeometric2F1}\left[\frac{7-p}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 - \sin [c + d x])\right] (1 + \sin [c + d x])^{\frac{1}{2}(-1-p)}$$

Result (type 8, 25 leaves):

$$\int \frac{(e \cos [c + d x])^p}{(a + a \sin [c + d x])^3} dx$$

Problem 334: Unable to integrate problem.

$$\int \frac{(e \cos [c + d x])^p}{(a + a \sin [c + d x])^8} dx$$

Optimal (type 5, 93 leaves, 2 steps):

$$-\frac{1}{a^8 d e (1+p)} 2^{\frac{1}{2}(-15+p)} (e \cos [c + d x])^{1+p} \\ \text{Hypergeometric2F1}\left[\frac{17-p}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2}(1 - \sin [c + d x])\right] (1 + \sin [c + d x])^{\frac{1}{2}(-1-p)}$$

Result (type 8, 25 leaves):

$$\int \frac{(e \cos [c + d x])^p}{(a + a \sin [c + d x])^8} dx$$

Problem 335: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (e \cos [c + d x])^p (a + a \sin [c + d x])^{7/2} dx$$

Optimal (type 5, 103 leaves, 3 steps):

$$-\left(2^{4+\frac{p}{2}} a^4 (e \cos [c + d x])^{1+p} \text{Hypergeometric2F1}\left[\frac{1}{2}(-6-p), \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2}(1 - \sin [c + d x])\right] \right. \\ \left. (1 + \sin [c + d x])^{-p/2}\right) / \left(d e (1+p) \sqrt{a + a \sin [c + d x]}\right)$$

Result (type 5, 629 leaves):

$$\begin{aligned}
 & \frac{1}{d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^7} \\
 & (1 + i) 2^{-3-p} e^{i p (c+d x)} \left(e^{-i (c+d x)} + e^{i (c+d x)} \right)^p \left(1 + e^{2 i (c+d x)} \right)^{-p} \cos [c + d x]^{-p} \left(e \cos [c + d x] \right)^p \\
 & \left(\frac{1}{7+2 p} e^{-\frac{1}{2} i (7+2 p) (c+d x)} \operatorname{Hypergeometric2F1} \left[-\frac{7}{4} - \frac{p}{2}, -p, -\frac{3}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \right. \\
 & \quad \frac{1}{5+2 p} 7 i e^{-\frac{1}{2} i (5+2 p) (c+d x)} \operatorname{Hypergeometric2F1} \left[-\frac{5}{4} - \frac{p}{2}, -p, -\frac{1}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \\
 & \quad \frac{1}{3+2 p} 21 e^{-\frac{1}{2} i (3+2 p) (c+d x)} \operatorname{Hypergeometric2F1} \left[-\frac{3}{4} - \frac{p}{2}, -p, \frac{1}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] + \\
 & \quad \frac{1}{1+2 p} 35 i e^{-\frac{1}{2} i (1+2 p) (c+d x)} \operatorname{Hypergeometric2F1} \left[-\frac{1}{4} - \frac{p}{2}, -p, \frac{3}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] + \\
 & \quad \frac{1}{-1+2 p} 35 e^{\frac{1}{2} i (-1+2 p) (c+d x)} \operatorname{Hypergeometric2F1} \left[\frac{1}{4} - \frac{p}{2}, -p, \frac{5}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \\
 & \quad \frac{1}{-3+2 p} 21 i e^{\frac{1}{2} i (3-2 p) (c+d x)} \operatorname{Hypergeometric2F1} \left[\frac{3}{4} - \frac{p}{2}, -p, \frac{7}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \\
 & \quad \frac{1}{-5+2 p} 7 e^{\frac{1}{2} i (5-2 p) (c+d x)} \operatorname{Hypergeometric2F1} \left[\frac{5}{4} - \frac{p}{2}, -p, \frac{9}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] + \\
 & \quad \left. \frac{1}{-7+2 p} i e^{-\frac{1}{2} i (-7+2 p) (c+d x)} \operatorname{Hypergeometric2F1} \left[\frac{7}{4} - \frac{p}{2}, -p, \frac{11}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] \right) \\
 & (a (1 + \sin [c + d x]))^{7/2}
 \end{aligned}$$

Problem 336: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (e \cos [c + d x])^p (a + a \sin [c + d x])^{5/2} dx$$

Optimal (type 5, 103 leaves, 3 steps):

$$\begin{aligned}
 & - \left(2^{3+\frac{p}{2}} a^3 (e \cos [c + d x])^{1+p} \operatorname{Hypergeometric2F1} \left[\frac{1}{2} (-4 - p), \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 - \sin [c + d x]) \right] \right. \\
 & \quad \left. (1 + \sin [c + d x])^{-p/2} \right) / \left(d e (1+p) \sqrt{a + a \sin [c + d x]} \right)
 \end{aligned}$$

Result (type 5, 504 leaves):

$$\frac{1}{d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^5} \left((1 - i) 2^{-3-p} e^{i p (c+d x)} \left(e^{-i (c+d x)} + e^{i (c+d x)} \right)^p \left(1 + e^{2 i (c+d x)} \right)^{-p} \cos [c + d x]^{-p} \left(e \cos [c + d x] \right)^p \right. \\ \left(-\frac{1}{5+2 p} 2 e^{-\frac{1}{2} i (5+2 p) (c+d x)} \text{Hypergeometric2F1} \left[-\frac{5}{4} - \frac{p}{2}, -p, -\frac{1}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] + \right. \\ \frac{1}{3+2 p} 10 i e^{-\frac{1}{2} i (3+2 p) (c+d x)} \text{Hypergeometric2F1} \left[-\frac{3}{4} - \frac{p}{2}, -p, \frac{1}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] + \\ \frac{1}{1+2 p} 20 e^{-\frac{1}{2} i (1+2 p) (c+d x)} \text{Hypergeometric2F1} \left[-\frac{1}{4} - \frac{p}{2}, -p, \frac{3}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \\ \frac{1}{-1+2 p} 20 i e^{\frac{1}{2} i (1-2 p) (c+d x)} \text{Hypergeometric2F1} \left[\frac{1}{4} - \frac{p}{2}, -p, \frac{5}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \\ \frac{1}{-3+2 p} 10 e^{\frac{1}{2} i (3-2 p) (c+d x)} \text{Hypergeometric2F1} \left[\frac{3}{4} - \frac{p}{2}, -p, \frac{7}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] + \\ \left. \left. \frac{1}{-5+2 p} 2 i e^{-\frac{1}{2} i (-5+2 p) (c+d x)} \text{Hypergeometric2F1} \left[\frac{5}{4} - \frac{p}{2}, -p, \frac{9}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] \right) \right) \\ (a (1 + \sin [c + d x]))^{5/2}$$

Problem 337: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int (e \cos [c + d x])^p (a + a \sin [c + d x])^{3/2} dx$$

Optimal (type 5, 103 leaves, 3 steps):

$$- \left(\left(2^{2+\frac{p}{2}} a^2 (e \cos [c + d x])^{1+p} \text{Hypergeometric2F1} \left[\frac{1}{2} (-2-p), \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 - \sin [c + d x]) \right] \right) \right. \\ \left. (1 + \sin [c + d x])^{-p/2} \right) / \left(d e (1+p) \sqrt{a + a \sin [c + d x]} \right)$$

Result (type 5, 378 leaves):

$$\frac{1}{d \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^3} \left((1 + i) 2^{-2-p} e^{i p (c+d x)} \left(e^{-i (c+d x)} + e^{i (c+d x)} \right)^p \left(1 + e^{2 i (c+d x)} \right)^{-p} \cos [c + d x]^{-p} \left(e \cos [c + d x] \right)^p \right. \\ \left(\frac{1}{3+2 p} 2 e^{-\frac{1}{2} i (3+2 p) (c+d x)} \text{Hypergeometric2F1} \left[-\frac{3}{4} - \frac{p}{2}, -p, \frac{1}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \right. \\ \frac{1}{1+2 p} 6 i e^{-\frac{1}{2} i (1+2 p) (c+d x)} \text{Hypergeometric2F1} \left[-\frac{1}{4} - \frac{p}{2}, -p, \frac{3}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] - \\ \frac{1}{-1+2 p} 6 e^{\frac{1}{2} i (1-2 p) (c+d x)} \text{Hypergeometric2F1} \left[\frac{1}{4} - \frac{p}{2}, -p, \frac{5}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] + \\ \left. \frac{1}{-3+2 p} 2 i e^{-\frac{1}{2} i (-3+2 p) (c+d x)} \text{Hypergeometric2F1} \left[\frac{3}{4} - \frac{p}{2}, -p, \frac{7}{4} - \frac{p}{2}, -e^{2 i (c+d x)} \right] \right) \\ (a (1 + \sin [c + d x]))^{3/2}$$

Problem 338: Result unnecessarily involves complex numbers and more than

twice size of optimal antiderivative.

$$\int (e \cos [c + d x])^p \sqrt{a + a \sin [c + d x]} dx$$

Optimal (type 5, 97 leaves, 3 steps):

$$- \left(\left(2^{1+\frac{p}{2}} a (e \cos [c + d x])^{1+p} \operatorname{Hypergeometric2F1} \left[-\frac{p}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 - \sin [c + d x]) \right] \right) \right. \\ \left. (1 + \sin [c + d x])^{-p/2} \right) / \left(d e (1+p) \sqrt{a + a \sin [c + d x]} \right)$$

Result (type 5, 310 leaves):

$$\frac{1}{d (-1 + 2 p) (1 + 2 p) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)} \\ (1 + i) 2^{-p} e^{-\frac{1}{2} i d x} \cos [c + d x]^{-p} (e \cos [c + d x])^p \\ \left(e^{i d x} (1 + 2 p) \operatorname{Hypergeometric2F1} \left[\frac{1}{4} (1 - 2 p), -p, \frac{1}{4} (5 - 2 p), -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \right. \\ \left(\cos \left[\frac{c}{2} \right] + i \sin \left[\frac{c}{2} \right] \right) + (-1 + 2 p) \operatorname{Hypergeometric2F1} \left[\frac{1}{4} (-1 - 2 p), \right. \\ \left. -p, \frac{1}{4} (3 - 2 p), -e^{2 i d x} (\cos [c] + i \sin [c])^2 \right] \left(i \cos \left[\frac{c}{2} \right] + \sin \left[\frac{c}{2} \right] \right) \left. \right) \\ (e^{-i d x} ((1 + e^{2 i d x}) \cos [c] + i (-1 + e^{2 i d x}) \sin [c]))^p \\ (1 + e^{2 i d x} \cos [2 c] + i e^{2 i d x} \sin [2 c])^{-p} \sqrt{a (1 + \sin [c + d x])}$$

Problem 340: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^p}{(a + a \sin [c + d x])^{3/2}} dx$$

Optimal (type 5, 102 leaves, 3 steps):

$$- \left(\left(2^{-1+\frac{p}{2}} (e \cos [c + d x])^{1+p} \operatorname{Hypergeometric2F1} \left[\frac{4-p}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2} (1 - \sin [c + d x]) \right] \right) \right. \\ \left. (1 + \sin [c + d x])^{1-\frac{p}{2}} \right) / \left(d e (1+p) (a + a \sin [c + d x])^{3/2} \right)$$

Result (type 5, 228 leaves):

$$\frac{1}{a d p (-4 + p^2) \sqrt{2 - 2 \sin [c + d x]} (a (1 + \sin [c + d x]))^{3/2}} \\ 2^{-1+\frac{p}{2}} \cos [c + d x] (e \cos [c + d x])^p (1 - \sin [c + d x])^{-p/2} \\ \left(4 a p (2 + p) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}(-1 - p), \frac{1}{2}(-2 + p), \frac{p}{2}, \frac{1}{2}(1 + \sin [c + d x])\right] + \right. \\ (-2 + p) (1 + \sin [c + d x]) \\ \left. \left(2 a (2 + p) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}(-1 - p), \frac{p}{2}, \frac{2 + p}{2}, \frac{1}{2}(1 + \sin [c + d x])\right] + \right. \right. \\ \left. \left. a p \operatorname{Hypergeometric2F1}\left[\frac{1 - p}{2}, \frac{2 + p}{2}, \frac{4 + p}{2}, \frac{1}{2}(1 + \sin [c + d x])\right] (1 + \sin [c + d x]) \right) \right) \right)$$

Problem 341: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^p}{(a + a \sin [c + d x])^{5/2}} dx$$

Optimal (type 5, 105 leaves, 3 steps):

$$-\left(\left(2^{-2+\frac{p}{2}} (e \cos [c + d x])^{1+p} \operatorname{Hypergeometric2F1}\left[\frac{6-p}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \frac{1}{2}(1 - \sin [c + d x])\right] \right) \right. \\ \left. (1 + \sin [c + d x])^{1-\frac{p}{2}} \right) / (a d e (1 + p) (a + a \sin [c + d x])^{3/2})$$

Result (type 5, 304 leaves):

$$\frac{1}{a^4 d (-4 + p) (-2 + p) p (2 + p) \sqrt{2 - 2 \sin [c + d x]} (1 + \sin [c + d x])^3} \\ 2^{-2+\frac{p}{2}} \cos [c + d x] (e \cos [c + d x])^p (1 - \sin [c + d x])^{-p/2} \sqrt{a (1 + \sin [c + d x])} \\ \left(8 a p (-4 + p^2) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}(-1 - p), \frac{1}{2}(-4 + p), \frac{1}{2}(-2 + p), \frac{1}{2}(1 + \sin [c + d x])\right] + \right. \\ (-4 + p) (1 + \sin [c + d x]) \left(4 a p (2 + p) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}(-1 - p), \right. \right. \\ \left. \left. \frac{1}{2}(-2 + p), \frac{p}{2}, \frac{1}{2}(1 + \sin [c + d x])\right] + (-2 + p) (1 + \sin [c + d x]) \right) \\ \left. \left(2 a (2 + p) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}(-1 - p), \frac{p}{2}, \frac{2 + p}{2}, \frac{1}{2}(1 + \sin [c + d x])\right] + \right. \right. \\ \left. \left. a p \operatorname{Hypergeometric2F1}\left[\frac{1 - p}{2}, \frac{2 + p}{2}, \frac{4 + p}{2}, \frac{1}{2}(1 + \sin [c + d x])\right] (1 + \sin [c + d x]) \right) \right) \right)$$

Problem 343: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \cos [c + d x]^7 (a + a \sin [c + d x])^m dx$$

Optimal (type 3, 109 leaves, 3 steps):

$$\frac{8 (a + a \sin [c + d x])^{4+m}}{a^4 d (4+m)} - \frac{12 (a + a \sin [c + d x])^{5+m}}{a^5 d (5+m)} +$$

$$\frac{6 (a + a \sin [c + d x])^{6+m}}{a^6 d (6+m)} - \frac{(a + a \sin [c + d x])^{7+m}}{a^7 d (7+m)}$$

Result (type 3, 796 leaves):

$$\frac{1}{d} (a (1 + \sin [c + d x]))^m \left(\frac{6144 + 1084 m + 117 m^2 + 5 m^3}{16 (4+m) (5+m) (6+m) (7+m)} + \right.$$

$$\left. \left((29400 + 2578 m + 171 m^2 + 5 m^3) \left(-\frac{1}{128} \operatorname{Im} \cos [c + d x] + \frac{1}{128} \operatorname{Im} \sin [c + d x] \right) \right) / \right.$$

$$\left. ((4+m) (5+m) (6+m) (7+m)) + \right.$$

$$\left. \left((29400 + 2578 m + 171 m^2 + 5 m^3) \left(\frac{1}{128} \operatorname{Im} \cos [c + d x] + \frac{1}{128} \operatorname{Im} \sin [c + d x] \right) \right) / \right.$$

$$\left. ((4+m) (5+m) (6+m) (7+m)) + \right.$$

$$\left. \left((804 m + 109 m^2 + 5 m^3) \left(\frac{3}{64} \operatorname{Im} \cos [2 (c + d x)] - \frac{3}{64} \operatorname{Im} \sin [2 (c + d x)] \right) \right) / \right.$$

$$\left. ((4+m) (5+m) (6+m) (7+m)) + \right.$$

$$\left. \left((804 m + 109 m^2 + 5 m^3) \left(\frac{3}{64} \operatorname{Im} \cos [2 (c + d x)] + \frac{3}{64} \operatorname{Im} \sin [2 (c + d x)] \right) \right) / \right.$$

$$\left. ((4+m) (5+m) (6+m) (7+m)) + \right.$$

$$\left. \left((1960 + 1070 m + 93 m^2 + 3 m^3) \left(-\frac{3}{128} \operatorname{Im} \cos [3 (c + d x)] + \frac{3}{128} \operatorname{Im} \sin [3 (c + d x)] \right) \right) / \right.$$

$$\left. ((4+m) (5+m) (6+m) (7+m)) + \right.$$

$$\left. \left((1960 + 1070 m + 93 m^2 + 3 m^3) \left(\frac{3}{128} \operatorname{Im} \cos [3 (c + d x)] + \frac{3}{128} \operatorname{Im} \sin [3 (c + d x)] \right) \right) / \right.$$

$$\left. ((4+m) (5+m) (6+m) (7+m)) + \right.$$

$$\frac{(44 m + 17 m^2 + m^3) \left(\frac{3}{32} \operatorname{Im} \cos [4 (c + d x)] - \frac{3}{32} \operatorname{Im} \sin [4 (c + d x)] \right)}{(4+m) (5+m) (6+m) (7+m)} +$$

$$\frac{(44 m + 17 m^2 + m^3) \left(\frac{3}{32} \operatorname{Im} \cos [4 (c + d x)] + \frac{3}{32} \operatorname{Im} \sin [4 (c + d x)] \right)}{(4+m) (5+m) (6+m) (7+m)} +$$

$$\left((294 + 103 m + 5 m^2) \left(-\frac{1}{128} \operatorname{Im} \cos [5 (c + d x)] + \frac{1}{128} \operatorname{Im} \sin [5 (c + d x)] \right) \right) /$$

$$\left((5+m) (6+m) (7+m) \right) + \frac{(294 + 103 m + 5 m^2) \left(\frac{1}{128} \operatorname{Im} \cos [5 (c + d x)] + \frac{1}{128} \operatorname{Im} \sin [5 (c + d x)] \right)}{(5+m) (6+m) (7+m)} +$$

$$\frac{\frac{1}{64} m \operatorname{Im} \cos [6 (c + d x)] - \frac{1}{64} \operatorname{Im} \sin [6 (c + d x)]}{(6+m) (7+m)} + \frac{\frac{1}{64} m \operatorname{Im} \cos [6 (c + d x)] + \frac{1}{64} \operatorname{Im} \sin [6 (c + d x)]}{(6+m) (7+m)} +$$

$$\left. \left. \frac{-\frac{1}{128} \operatorname{Im} \cos [7 (c + d x)] + \frac{1}{128} \operatorname{Im} \sin [7 (c + d x)]}{7+m} + \frac{\frac{1}{128} \operatorname{Im} \cos [7 (c + d x)] + \frac{1}{128} \operatorname{Im} \sin [7 (c + d x)]}{7+m} \right) \right)$$

Problem 347: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \text{Sec}[c + d x] (a + a \text{Sin}[c + d x])^m dx$$

Optimal (type 5, 40 leaves, 2 steps):

$$\frac{1}{2 d m} \text{Hypergeometric2F1}\left[1, m, 1 + m, \frac{1}{2} (1 + \text{Sin}[c + d x])\right] (a + a \text{Sin}[c + d x])^m$$

Result (type 6, 7227 leaves):

$$\begin{aligned} & - \left(\left(\text{Cot}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2 (a + a \text{Sin}[c + d x])^m \right. \right. \\ & \left. \left(\frac{1 - \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2}{1 + \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2} \right)^{2m} \left(- \left(\left(2 \text{AppellF1}\left[1, 1 - 2 m, 2 m, 2, \right. \right. \right. \right. \\ & \left. \left. \left. \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^4 \right) / \right. \\ & \left. \left(-2 \text{AppellF1}\left[1, 1 - 2 m, 2 m, 2, \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] + \right. \right. \\ & \left. \left(2 m \text{AppellF1}\left[2, 1 - 2 m, 1 + 2 m, 3, \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, \right. \right. \right. \\ & \left. \left. \left. -\text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] + (-1 + 2 m) \text{AppellF1}\left[2, 2 - 2 m, 2 m, 3, \right. \right. \right. \\ & \left. \left. \left. \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, -\text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] \right) \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2 \right) \right) + \\ & \left((1 + m) \text{AppellF1}\left[1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} - \frac{1}{2} \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, \right. \right. \\ & \left. \left. 1 - \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] \left(-1 + \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2 \right)^2 \right) / \right. \\ & \left. \left((1 + 2 m) \left(-2 (1 + m) \text{AppellF1}\left[1 + 2 m, 2 m, 1, 2 + 2 m, \frac{1}{2} - \frac{1}{2} \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, \right. \right. \right. \right. \right. \\ & \left. \left. \left. 1 - \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] + \left(\text{AppellF1}\left[2 + 2 m, 2 m, 2, 3 + 2 m, \right. \right. \right. \right. \\ & \left. \left. \left. \frac{1}{2} - \frac{1}{2} \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, 1 - \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] + m \right. \right. \right. \\ & \left. \left. \left. \text{AppellF1}\left[2 + 2 m, 1 + 2 m, 1, 3 + 2 m, \frac{1}{2} - \frac{1}{2} \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2, \right. \right. \right. \right. \\ & \left. \left. \left. 1 - \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2\right] \right) \left(-1 + \text{Tan}\left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x\right)\right]^2 \right) \right) \right) \right) / \\ & \left(d \left(\text{Cos}\left[\frac{\pi}{4} + \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right)\right] - \text{Sin}\left[\frac{\pi}{4} + \frac{1}{2} \left(c - \frac{\pi}{2} + d x\right)\right] \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left(\cos \left[\frac{\pi}{4} + \frac{1}{2} \left(c - \frac{\pi}{2} + dx \right) \right] + \right. \\
 & \quad \left. \sin \left[\frac{\pi}{4} + \frac{1}{2} \left(c - \frac{\pi}{2} + dx \right) \right] \right) \\
 & \left(1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \left(\frac{1}{2 \left(1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2} \right. \\
 & \quad \left. \operatorname{Csc} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \left(\frac{1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2}{1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{2m} \right. \\
 & \quad \left. - \left(\left(2 \operatorname{AppellF1} \left[1, 1 - 2m, 2m, 2, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^4 \right) / \left(-2 \operatorname{AppellF1} \left[1, 1 - 2m, 2m, 2, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \left(2m \operatorname{AppellF1} \left[2, \right. \right. \right. \\
 & \quad \left. \left. 1 - 2m, 1 + 2m, 3, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \\
 & \quad \left. \left. (-1 + 2m) \operatorname{AppellF1} \left[2, 2 - 2m, 2m, 3, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \quad \left((1+m) \operatorname{AppellF1} \left[1 + 2m, 2m, 1, 2 + 2m, \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \left(-1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2 \right) / \\
 & \quad \left((1+2m) \left(-2(1+m) \operatorname{AppellF1} \left[1 + 2m, 2m, 1, 2 + 2m, \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \left(\operatorname{AppellF1} \left[2 + 2m, 2m, 2, 3 + 2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \\
 & \quad \left. \left. m \operatorname{AppellF1} \left[2 + 2m, 1 + 2m, 1, 3 + 2m, \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \left(-1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) \right) - \\
 & \quad \frac{1}{2 \left(1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)} \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \operatorname{Csc} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \\
 & \quad \left(\frac{1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2}{1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{2m} \\
 & \quad \left. - \left(\left(2 \operatorname{AppellF1} \left[1, 1 - 2m, 2m, 2, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^4 \right) / \left(-2 \operatorname{AppellF1}\left[1, 1 - 2m, 2m, 2, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \left(2m \operatorname{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - 2m, 1 + 2m, 3, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (-1 + 2m) \operatorname{AppellF1}\left[2, 2 - 2m, 2m, 3, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
 & \left((1+m) \operatorname{AppellF1}\left[1 + 2m, 2m, 1, 2 + 2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \left(-1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2 \right) / \\
 & \left((1+2m) \left(-2(1+m) \operatorname{AppellF1}\left[1 + 2m, 2m, 1, 2 + 2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \left(\operatorname{AppellF1}\left[2 + 2m, 2m, 2, 3 + 2m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, 1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. m \operatorname{AppellF1}\left[2 + 2m, 1 + 2m, 1, 3 + 2m, \frac{1}{2} - \frac{1}{2} \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \left(-1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \right) \right) + \\
 & \frac{1}{1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2} 2m \operatorname{Cot}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left(\frac{1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2}{1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2} \right)^{-1+2m} \\
 & \left(- \left(\left(\operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \right) \right) / \\
 & \left(2 \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right)^2 \right) - \frac{\operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]}{2 \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right)} \right) \\
 & \left(- \left(\left(2 \operatorname{AppellF1}\left[1, 1 - 2m, 2m, 2, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^4 \right) \right) / \left(-2 \operatorname{AppellF1}\left[1, 1 - 2m, 2m, 2, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \left(2m \operatorname{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - 2m, 1 + 2m, 3, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (-1 + 2m) \operatorname{AppellF1}\left[2, 2 - 2m, 2m, 3, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left((1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \left(-1 + \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2 \right) / \\
 & \left((1+2m) \left(-2(1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \left(\operatorname{AppellF1}\left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
 & \quad \left. \left. m \operatorname{AppellF1}\left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \left(-1 + \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \right) \right) + \\
 & \frac{1}{1 - \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2} \operatorname{Cot}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left(\frac{1 - \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2}{1 + \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2}\right)^{2m} \\
 & \left(-\left(\left(2 \operatorname{AppellF1}\left[1, 1-2m, 2m, 2, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^3\right) / \left(-2 \operatorname{AppellF1}\left[1, 1-2m, 2m, \right. \right. \right. \\
 & \quad \left. \left. 2, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \left(2m \operatorname{AppellF1}\left[2, \right. \right. \right. \\
 & \quad \left. \left. 1-2m, 1+2m, 3, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
 & \quad \left. \left. \left(-1+2m\right) \operatorname{AppellF1}\left[2, 2-2m, 2m, 3, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) - \\
 & \left(2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^4 \left(-\frac{1}{2} m \operatorname{AppellF1}\left[2, 1-2m, 1+2m, 3, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{1}{4}(1-2m) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[2, 2-2m, 2m, 3, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) \right) / \\
 & \left(-2 \operatorname{AppellF1}\left[1, 1-2m, 2m, 2, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
 & \quad \left. \left(2m \operatorname{AppellF1}\left[2, 1-2m, 1+2m, 3, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-1+2m) \operatorname{AppellF1}\left[2, 2-2m, 2m, 3, \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right)^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \left((1+m) \operatorname{AppellF1} \left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \left(-1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right] \right) / \\
 & \left((1+2m) \left(-2(1+m) \operatorname{AppellF1} \left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \left(\operatorname{AppellF1} \left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. m \operatorname{AppellF1} \left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \left(-1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) \right) + \\
 & \left((1+m) \left(-\frac{1}{2(2+2m)} (1+2m) \operatorname{AppellF1} \left[2+2m, 2m, 2, 3+2m, \frac{1}{2} - \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] - \frac{1}{2(2+2m)} \right. \right. \\
 & \quad \left. \left. m(1+2m) \operatorname{AppellF1} \left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \left(-1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right] \right) / \\
 & \left((1+2m) \left(-2(1+m) \operatorname{AppellF1} \left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \left(\operatorname{AppellF1} \left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. m \operatorname{AppellF1} \left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \left(-1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) \right) + \\
 & \left(2 \operatorname{AppellF1} \left[1, 1-2m, 2m, 2, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \\
 & \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^4 \left(\frac{1}{2} \left(2m \operatorname{AppellF1} \left[2, 1-2m, 1+2m, 3, \right. \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & (-1+2m) \operatorname{AppellF1}\left[2, 2-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] - \\
 & 2\left(-\frac{1}{2}m \operatorname{AppellF1}\left[2, 1-2m, 1+2m, 3, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] + \right. \\
 & \quad \left. \frac{1}{4}(1-2m) \operatorname{AppellF1}\left[2, 2-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right) + \\
 & \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \left(2m\left(-\frac{1}{3}(1+2m) \operatorname{AppellF1}\left[3, 1-2m, 2+2m, \right. \right. \right. \\
 & \quad \left. \left. 4, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] + \frac{1}{3}(1-2m) \operatorname{AppellF1}\left[3, \right. \right. \\
 & \quad \left. \left. 2-2m, 1+2m, 4, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right) + (-1+2m) \\
 & \left(-\frac{2}{3}m \operatorname{AppellF1}\left[3, 2-2m, 1+2m, 4, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] + \frac{1}{3}(2-2m) \operatorname{AppellF1}\left[3, 3-2m, \right. \right. \\
 & \quad \left. \left. 2m, 4, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right) \Bigg) / \\
 & \left(-2 \operatorname{AppellF1}\left[1, 1-2m, 2m, 2, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + \right. \\
 & \quad \left. \left(2m \operatorname{AppellF1}\left[2, 1-2m, 1+2m, 3, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + \right. \\
 & \quad \left. (-1+2m) \operatorname{AppellF1}\left[2, 2-2m, 2m, 3, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right) - \\
 & \left. \left((1+m) \operatorname{AppellF1}\left[1+2m, 2m, 1, 2+2m, \frac{1}{2}-\frac{1}{2} \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. 1 - \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \left(-1 + \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)^2 \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{1}{2} \left(\text{AppellF1} \left[2+2m, 2m, 2, 3+2m, \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + m \text{AppellF1} \left[2+2m, 1+2m, 1, 3+2m, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \right) \\
 & \text{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] - 2(1+m) \\
 & \left(-\frac{1}{2(2+2m)} (1+2m) \text{AppellF1} \left[2+2m, 2m, 2, 3+2m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \\
 & \text{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] - \frac{1}{2(2+2m)} m(1+2m) \\
 & \text{AppellF1} \left[2+2m, 1+2m, 1, 3+2m, \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, 1 - \right. \\
 & \quad \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \right) + \\
 & \left(-1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \left(-\frac{1}{3+2m} (2+2m) \text{AppellF1} \left[3+2m, \right. \right. \\
 & \quad \left. \left. 2m, 3, 4+2m, \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \\
 & \text{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] - \frac{1}{2(3+2m)} \\
 & m(2+2m) \text{AppellF1} \left[3+2m, 1+2m, 2, 4+2m, \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \\
 & \quad \left. 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] + \\
 & m \left(-\frac{1}{2(3+2m)} (2+2m) \text{AppellF1} \left[3+2m, 1+2m, 2, 4+2m, \right. \right. \\
 & \quad \left. \left. \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \\
 & \text{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] - \frac{1}{4(3+2m)} \\
 & (1+2m)(2+2m) \text{AppellF1} \left[3+2m, 2+2m, 1, 4+2m, \right. \\
 & \quad \left. \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \\
 & \left. \left. \text{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \right) \right) \right) / \\
 & \left((1+2m) \left(-2(1+m) \text{AppellF1} \left[1+2m, 2m, 1, 2+2m, \frac{1}{2} - \frac{1}{2} \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \left(\text{AppellF1} \left[2+2m, 2m, 2, 3+2m, \right. \right. \right. \right.
 \end{aligned}$$

$$\frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] +$$

$$m \operatorname{AppellF1}\left[2 + 2m, 1 + 2m, 1, 3 + 2m, \frac{1}{2} - \frac{1}{2} \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right.$$

$$\left. 1 - \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right)\left(-1 + \operatorname{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)\right)\right)\right)\right)$$

Problem 348: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c + dx]^3 (a + a \operatorname{Sin}[c + dx])^m dx$$

Optimal (type 5, 47 leaves, 2 steps):

$$-\frac{1}{4d(1-m)} a \operatorname{Hypergeometric2F1}\left[2, -1+m, m, \frac{1}{2}(1 + \operatorname{Sin}[c + dx])\right] (a + a \operatorname{Sin}[c + dx])^{-1+m}$$

Result (type 6, 27 160 leaves): Display of huge result suppressed!

Problem 349: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c + dx]^5 (a + a \operatorname{Sin}[c + dx])^m dx$$

Optimal (type 5, 51 leaves, 2 steps):

$$-\frac{1}{8d(2-m)} a^2 \operatorname{Hypergeometric2F1}\left[3, -2+m, -1+m, \frac{1}{2}(1 + \operatorname{Sin}[c + dx])\right] (a + a \operatorname{Sin}[c + dx])^{-2+m}$$

Result (type 5, 443 leaves):

$$\begin{aligned}
& -\frac{1}{32d} \left(\operatorname{Sec} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^m (a + a \operatorname{Sin}[c + dx])^m \left(1 + \operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{-m} \\
& \left(-\frac{1}{m} 6 \left(1 + \operatorname{Cot} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^m \operatorname{Hypergeometric2F1} [m, m, 1+m, -\operatorname{Cot} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2] - \right. \\
& \frac{1}{1+m} 4 \operatorname{Cot} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \left(1 + \operatorname{Cot} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^m \\
& \operatorname{Hypergeometric2F1} [m, 1+m, 2+m, -\operatorname{Cot} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2] - \frac{1}{2+m} \operatorname{Cot} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^4 \\
& \left. \left(1 + \operatorname{Cot} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^m \operatorname{Hypergeometric2F1} [m, 2+m, 3+m, -\operatorname{Cot} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2] + \right. \\
& \left. 4 \frac{\left(-1 - \operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 + \left(1 + \operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^m \right)}{-1+m} + \right. \\
& \left. \left(-1 + \operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^4 + \left(1 + \operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^m - \right. \\
& \left. m \left(\operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 + \operatorname{Tan} \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^4 \right) \right) / \left((-2+m) (-1+m) \right)
\end{aligned}$$

Problem 350: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c + dx]^4 (a + a \operatorname{Sin}[c + dx])^m dx$$

Optimal (type 5, 83 leaves, 3 steps):

$$\begin{aligned}
& -\frac{1}{5d} 2^{\frac{5}{2}+m} a^2 \operatorname{Cos}[c + dx]^5 \operatorname{Hypergeometric2F1} \left[\frac{5}{2}, -\frac{3}{2}-m, \frac{7}{2}, \frac{1}{2} (1 - \operatorname{Sin}[c + dx]) \right] \\
& (1 + \operatorname{Sin}[c + dx])^{-\frac{1}{2}-m} (a + a \operatorname{Sin}[c + dx])^{-2+m}
\end{aligned}$$

Result (type 6, 9362 leaves):

$$\begin{aligned}
& -\left(\left(3072 \operatorname{Cos}[c + dx]^4 (a + a \operatorname{Sin}[c + dx])^m \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \right. \right. \\
& \left. \left(1 - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{2(2+m)} \left(\frac{1}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{9+2m} \right. \\
& \left. \left(\operatorname{AppellF1} \left[\frac{1}{2}, -2(2+m), 7+2m, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \right. \\
& \left. \left. \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2 \right) / \left(3 \operatorname{AppellF1} \left[\frac{1}{2}, -2(2+m), \right. \right. \right. \\
& \left. \left. \left. 7+2m, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \right. \\
& \left. \left. 2 \left(2(2+m) \operatorname{AppellF1} \left[\frac{3}{2}, -3-2m, 7+2m, \frac{5}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+(7+2m)\operatorname{AppellF1}\left[\frac{3}{2},-2(2+m),2(4+m),\frac{5}{2},\right. \\
 & \left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)+ \\
 & \operatorname{AppellF1}\left[\frac{1}{2},-2(2+m),9+2m,\frac{3}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)/ \\
 & \left(3\operatorname{AppellF1}\left[\frac{1}{2},-2(2+m),9+2m,\frac{3}{2},\right. \right. \\
 & \left. \left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]-\right. \\
 & \left.2\left(2(2+m)\operatorname{AppellF1}\left[\frac{3}{2},-3-2m,9+2m,\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+(9+2m)\operatorname{AppellF1}\left[\frac{3}{2},-2(2+m),2(5+m),\frac{5}{2},\right. \right. \\
 & \left. \left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)+ \right. \\
 & \left. \left(2\operatorname{AppellF1}\left[\frac{1}{2},-2(2+m),2(4+m),\frac{3}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\right)/ \\
 & \left(-3\operatorname{AppellF1}\left[\frac{1}{2},-2(2+m),2(4+m),\frac{3}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+ \right. \\
 & \left. 4\left((2+m)\operatorname{AppellF1}\left[\frac{3}{2},-3-2m,8+2m,\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+(4+m)\operatorname{AppellF1}\left[\frac{3}{2},-2(2+m),9+2m,\frac{5}{2},\right. \right. \\
 & \left. \left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\right)/ \\
 & \left(d\left(768\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)^{2(2+m)}\right. \right. \\
 & \left. \left.\left(\frac{1}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2}\right)^{9+2m}\right. \right. \\
 & \left. \left.\left(\left(\operatorname{AppellF1}\left[\frac{1}{2},-2(2+m),7+2m,\frac{3}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\right. \right. \right. \\
 & \left. \left. \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)^2\right)\right)/\left(3\operatorname{AppellF1}\left[\frac{1}{2},-2(2+m),7+ \right. \right. \\
 & \left. \left. 2m,\frac{3}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]- \right. \\
 & \left. \left. 2\left(2(2+m)\operatorname{AppellF1}\left[\frac{3}{2},-3-2m,7+2m,\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+(7+2m)\operatorname{AppellF1}\left[\frac{3}{2},-2(2+m),2(4+m),\frac{5}{2},\right. \\
& \left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)+ \\
& \operatorname{AppellF1}\left[\frac{1}{2},-2(2+m),9+2m,\frac{3}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right. \\
& \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]/\left(3\operatorname{AppellF1}\left[\frac{1}{2},-2(2+m),9+\right.\right. \\
& \left.\left.2m,\frac{3}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]-\right. \\
& \left.2\left(2(2+m)\operatorname{AppellF1}\left[\frac{3}{2},-3-2m,9+2m,\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right.\right. \\
& \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+(9+2m)\operatorname{AppellF1}\left[\frac{3}{2},-2(2+m),2(5+m),\frac{5}{2},\right.\right.\right. \\
& \left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)+\right. \\
& \left.\left(2\operatorname{AppellF1}\left[\frac{1}{2},-2(2+m),2(4+m),\frac{3}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right.\right. \\
& \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\right)/\left(-3\operatorname{AppellF1}\left[\frac{1}{2},-2\right.\right.\right. \\
& \left.\left.\left.(2+m),2(4+m),\frac{3}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+ \right. \\
& \left.4\left((2+m)\operatorname{AppellF1}\left[\frac{3}{2},-3-2m,8+2m,\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right.\right. \\
& \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+(4+m)\operatorname{AppellF1}\left[\frac{3}{2},-2(2+m),9+2m,\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right.\right. \\
& \left.\left.\left.\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\right)- \\
& 3072(2+m)\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \\
& \left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)^{-1+2(2+m)} \\
& \left(\frac{1}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2}\right)^{9+2m} \\
& \left(\left(\operatorname{AppellF1}\left[\frac{1}{2},-2(2+m),7+2m,\frac{3}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\right.\right. \\
& \left.\left.\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)^2\right)\right)/\left(3\operatorname{AppellF1}\left[\frac{1}{2},-2(2+m),7+\right.\right. \\
& \left.\left.2m,\frac{3}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]-\right. \\
& \left.2\left(2(2+m)\operatorname{AppellF1}\left[\frac{3}{2},-3-2m,7+2m,\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right.\right. \\
& \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+(7+2m)\operatorname{AppellF1}\left[\frac{3}{2},-2(2+m),2(4+m),\frac{5}{2},\right.\right.\right.
\end{aligned}$$

$$\begin{aligned}
 & \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 + \\
 & \text{AppellF1}\left[\frac{1}{2}, -2(2+m), 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \\
 & \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] / \left(3 \text{AppellF1}\left[\frac{1}{2}, -2(2+m), 9+ \right. \right. \\
 & \left. \left. 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & \left. 2\left(2(2+m) \text{AppellF1}\left[\frac{3}{2}, -3-2m, 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (9+2m) \text{AppellF1}\left[\frac{3}{2}, -2(2+m), 2(5+m), \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 + \\
 & \left(2 \text{AppellF1}\left[\frac{1}{2}, -2(2+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) / \left(-3 \text{AppellF1}\left[\frac{1}{2}, -2 \right. \right. \right. \\
 & \left. \left. (2+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
 & \left. 4\left((2+m) \text{AppellF1}\left[\frac{3}{2}, -3-2m, 8+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (4+m) \text{AppellF1}\left[\frac{3}{2}, -2(2+m), 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 - \\
 & 1536(9+2m) \text{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
 & \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^{2(2+m)} \\
 & \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2}\right)^{10+2m} \\
 & \left(\left(\text{AppellF1}\left[\frac{1}{2}, -2(2+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \right. \\
 & \left. \left. \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2\right) / \left(3 \text{AppellF1}\left[\frac{1}{2}, -2(2+m), 7+ \right. \right. \right. \\
 & \left. \left. 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & \left. 2\left(2(2+m) \text{AppellF1}\left[\frac{3}{2}, -3-2m, 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (7+2m) \text{AppellF1}\left[\frac{3}{2}, -2(2+m), 2(4+m), \frac{5}{2}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 +
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{1}{2}, -2(2+m), 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] / \left(3 \text{AppellF1}\left[\frac{1}{2}, -2(2+m), 9+ \right. \right. \\
 & \quad \left. \left. 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & \quad \left. 2\left(2(2+m) \text{AppellF1}\left[\frac{3}{2}, -3-2m, 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (9+2m) \text{AppellF1}\left[\frac{3}{2}, -2(2+m), 2(5+m), \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + \right. \\
 & \quad \left. \left(2 \text{AppellF1}\left[\frac{1}{2}, -2(2+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)\right) / \right. \\
 & \quad \left. \left(-3 \text{AppellF1}\left[\frac{1}{2}, -2(2+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + 4\left((2+m) \text{AppellF1}\left[\frac{3}{2}, -3-2m, \right. \right. \right. \\
 & \quad \left. \left. 8+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (4+m) \text{AppellF1}\left[\frac{3}{2}, -2(2+m), 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + \right. \\
 & \quad \left. 3072 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^{2(2+m)} \right. \\
 & \quad \left. \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2}\right)^{9+2m} \right. \\
 & \quad \left. \left(\left(\text{AppellF1}\left[\frac{1}{2}, -2(2+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \right. \right. \\
 & \quad \left. \left. \text{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)\right) / \right. \\
 & \quad \left. \left(3 \text{AppellF1}\left[\frac{1}{2}, -2(2+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & \quad \left. 2\left(2(2+m) \text{AppellF1}\left[\frac{3}{2}, -3-2m, 7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (7+2m) \text{AppellF1}\left[\frac{3}{2}, -2(2+m), 2(4+m), \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(-\frac{1}{6} (7+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 8+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] - \frac{1}{3} \right. \\
 & \quad (2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(2+m), 7+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] \right) \\
 & \quad \left(1 + \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right)^2 \Big/ \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(2+m), 7+ \right. \right. \\
 & \quad \left. \left. 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] - \right. \\
 & \quad \left. 2 \left(2(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -3-2m, 7+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + (7+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 2(4+m), \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) + \\
 & \quad \left(-\frac{1}{6} (9+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 10+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] - \right. \\
 & \quad \left. \frac{1}{3} (2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(2+m), 9+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] \right) \Big/ \\
 & \quad \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(2+m), 9+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] - \right. \\
 & \quad \left. 2 \left(2(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -3-2m, 9+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + (9+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 2(5+m), \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) + \\
 & \quad \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(2+m), 2(4+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] \right) \Big/ \\
 & \quad \left(-3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(2+m), 2(4+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + \right. \\
 & \quad \left. 4 \left((2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -3-2m, 8+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+(4+m) \operatorname{AppellF1}\left[\frac{3}{2},-2(2+m),9+2m,\frac{5}{2},\right. \\
 & \left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)+ \\
 & \left(2\left(-\frac{1}{3}(4+m) \operatorname{AppellF1}\left[\frac{3}{2},-2(2+m),1+2(4+m),\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]-\frac{1}{3}\right.\right. \\
 & \left.\left.(2+m) \operatorname{AppellF1}\left[\frac{3}{2},1-2(2+m),2(4+m),\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right.\right. \\
 & \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)\right) \\
 & \left.\left.\left.\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\right)\right) / \left(-3 \operatorname{AppellF1}\left[\frac{1}{2},-2(2+m),2\right.\right.\right. \\
 & \left.\left.\left.(4+m),\frac{3}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right)+ \\
 & 4\left((2+m) \operatorname{AppellF1}\left[\frac{3}{2},-3-2m,8+2m,\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+(4+m) \operatorname{AppellF1}\left[\frac{3}{2},-2(2+m),9+2m,\frac{5}{2},\right.\right. \\
 & \left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\right)\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)- \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2},-2(2+m),7+2m,\frac{3}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right) \\
 & \left.\left.\left.\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\right)^2\right)\left(-\left(2(2+m) \operatorname{AppellF1}\left[\frac{3}{2},-3-2m,7+2m,\right.\right.\right. \right. \\
 & \left.\left.\left.\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right)+ \right. \\
 & \left.\left.\left.\left(7+2m\right) \operatorname{AppellF1}\left[\frac{3}{2},-2(2+m),2(4+m),\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right.\right. \right. \\
 & \left.\left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right)\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)+ \\
 & 3\left(-\frac{1}{6}(7+2m) \operatorname{AppellF1}\left[\frac{3}{2},-2(2+m),8+2m,\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]- \right. \\
 & \left.\frac{1}{3}(2+m) \operatorname{AppellF1}\left[\frac{3}{2},1-2(2+m),7+2m,\frac{5}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right. \\
 & \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)\right)-2 \\
 & \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\left(2(2+m)\left(-\frac{3}{10}(7+2m) \operatorname{AppellF1}\left[\frac{5}{2},-3-2m,\right.\right.\right. \\
 & \left.\left.\left.8+2m,\frac{7}{2},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right) \right. \\
 & \left.\left.\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]+\frac{3}{10}(-3-2m)\right)\right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{5}{2}, -2-2m, 7+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\right.\right. \\
 & \quad \left.\left.(-c+\frac{\pi}{2}-dx)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] + \\
 & (7+2m) \left(-\frac{3}{5}(4+m) \text{AppellF1}\left[\frac{5}{2}, -2(2+m), 1+2(4+m), \frac{7}{2}, \tan\left[\frac{1}{4}\right.\right.\right. \\
 & \quad \left.\left.(-c+\frac{\pi}{2}-dx)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \\
 & \quad \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] - \frac{3}{5}(2+m) \text{AppellF1}\left[\frac{5}{2}, 1-2(2+m), \right. \\
 & \quad \left.2(4+m), \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \\
 & \quad \left.\left.\left.\text{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)\right)\right) / \\
 & \left(3 \text{AppellF1}\left[\frac{1}{2}, -2(2+m), 7+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right.\right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] - 2\left(2(2+m) \text{AppellF1}\left[\frac{3}{2}, -3-2m, \right.\right.\right. \\
 & \quad \left.\left.\left.7+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + \right.\right. \\
 & \quad \left.\left.(7+2m) \text{AppellF1}\left[\frac{3}{2}, -2(2+m), 2(4+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right.\right.\right. \\
 & \quad \left.\left.\left.-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 - \right. \\
 & \left. \left(\text{AppellF1}\left[\frac{1}{2}, -2(2+m), 9+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right.\right. \\
 & \quad \left.\left. - \left(2(2+m) \text{AppellF1}\left[\frac{3}{2}, -3-2m, 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right.\right.\right. \right. \\
 & \quad \left.\left.\left.-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + (9+2m) \text{AppellF1}\left[\frac{3}{2}, -2(2+m), \right.\right.\right. \\
 & \quad \left.\left.\left.2(5+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right)\right) \\
 & \quad \text{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] + 3\left(-\frac{1}{6}(9+2m) \right. \\
 & \quad \left. \text{AppellF1}\left[\frac{3}{2}, -2(2+m), 10+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right.\right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] - \right. \\
 & \quad \left.\frac{1}{3}(2+m) \text{AppellF1}\left[\frac{3}{2}, 1-2(2+m), 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right.\right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \text{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right) - 2 \\
 & \quad \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \left(2(2+m) \left(-\frac{3}{10}(9+2m) \text{AppellF1}\left[\frac{5}{2}, -3-2m, \right.\right.\right. \\
 & \quad \left.\left.\left.10+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right) \right)
 \end{aligned}$$

$$\begin{aligned}
& \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] + \frac{3}{10}(-3-2m) \\
& \operatorname{AppellF1}\left[\frac{5}{2}, -2-2m, 9+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\right.\right. \\
& \quad \left.\left.(-c+\frac{\pi}{2}-dx)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] \Big) + \\
& (9+2m) \left(-\frac{3}{5}(5+m) \operatorname{AppellF1}\left[\frac{5}{2}, -2(2+m), 1+2(5+m), \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\right.\right.\right. \\
& \quad \left.\left.(-c+\frac{\pi}{2}-dx)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \\
& \quad \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] - \frac{3}{5}(2+m) \operatorname{AppellF1}\left[\frac{5}{2}, 1-2(2+m), \right. \\
& \quad \left.2(5+m), \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \\
& \quad \left.\left.\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)\right) \Big) \Big) / \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(2+m), 9+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right.\right. \\
& \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] - 2\left(2(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -3-2m, \right.\right.\right. \\
& \quad \left.\left.9+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + \right. \\
& \quad \left.\left.(9+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 2(5+m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right.\right.\right. \\
& \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 - \right. \\
& \left. \left(2 \operatorname{AppellF1}\left[\frac{1}{2}, -2(2+m), 2(4+m), \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right.\right.\right. \\
& \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right) \right. \\
& \quad \left. \left(2\left((2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -3-2m, 8+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right.\right.\right.\right. \\
& \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + (4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), \right.\right. \\
& \quad \left.\left.9+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right) \\
& \quad \left.\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] - 3 \right. \\
& \quad \left. \left(-\frac{1}{3}(4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 1+2(4+m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right.\right.\right. \\
& \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] - \right. \\
& \quad \left. \frac{1}{3}(2+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(2+m), 2(4+m), \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right.\right. \\
& \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right) + 4
\end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left((2+m) \left(-\frac{3}{10}(8+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -3-2m, \right.\right.\right. \\
 & \quad \left.\left.\left. 9+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{3}{10}(-3-2m) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, -2-2m, 8+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\right.\right.\right. \\
 & \quad \quad \left.\left.\left. \left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) + \\
 & (4+m) \left(-\frac{3}{10}(9+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -2(2+m), 10+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\right.\right.\right. \\
 & \quad \left.\left.\left. \left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \frac{3}{5}(2+m) \operatorname{AppellF1}\left[\frac{5}{2}, 1-2(2+m), \right.\right. \\
 & \quad \left.\left. 9+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) \Bigg) / \\
 & \left(-3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(2+m), 2(4+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right.\right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + 4 \left((2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -3-2m, \right.\right.\right. \\
 & \quad \left.\left.\left. 8+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) + \right. \\
 & \quad \left. (4+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(2+m), 9+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right.\right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Bigg) \Bigg) \Bigg)
 \end{aligned}$$

Problem 351: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \cos[c+dx]^2 (a+a \sin[c+dx])^m dx$$

Optimal (type 5, 81 leaves, 3 steps):

$$\begin{aligned}
 & -\frac{1}{3d} 2^{\frac{3}{2}+m} a \cos[c+dx]^3 \operatorname{Hypergeometric2F1}\left[\frac{3}{2}, -\frac{1}{2}-m, \frac{5}{2}, \frac{1}{2}(1-\sin[c+dx])\right] \\
 & (1+\sin[c+dx])^{-\frac{1}{2}-m} (a+a \sin[c+dx])^{-1+m}
 \end{aligned}$$

Result (type 6, 6167 leaves):

$$-\left(\left(192 \left(\cos\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right)^{5+2m} \cos[c+dx]^2 \right. \right.$$

$$\begin{aligned}
& (a + a \sin[c + dx])^m \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^{2(1+m)} \\
& \left(-\left(\text{AppellF1}\left[\frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) / \right. \\
& \quad \left(3 \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \right. \right. \\
& \quad \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
& \quad \left. 2\left(2(1+m) \text{AppellF1}\left[\frac{3}{2}, -1-2m, 5+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (5+2m) \text{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(3+m), \frac{5}{2}, \right. \right. \\
& \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
& \quad \left(\text{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
& \quad \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) / \left(3 \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \right. \right. \\
& \quad \quad \left. \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
& \quad \left. 4\left((1+m) \text{AppellF1}\left[\frac{3}{2}, -1-2m, 4+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (2+m) \text{AppellF1}\left[\frac{3}{2}, -2(1+m), 5+2m, \frac{5}{2}, \right. \right. \\
& \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \right) / \\
& \quad \left(d \left(48 \cos\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^8 \left(\cos\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^{2m} \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^{2(1+m)} \right. \\
& \quad \left(-\left(\text{AppellF1}\left[\frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] / \left(3 \text{AppellF1}\left[\frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \right. \right. \right. \\
& \quad \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 2\left(2(1+m) \text{AppellF1}\left[\frac{3}{2}, \right. \right. \right. \\
& \quad \quad \left. \left. -1-2m, 5+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \quad \quad \left. (5+2m) \text{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(3+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
& \quad \left(\text{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) / \left(3 \text{AppellF1}\left[\frac{1}{2}, -2 \right. \right. \\
& \quad \quad \left. (1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right.
\end{aligned}$$

$$\begin{aligned}
 & -1 - 2m, 5 + 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big] + \\
 & (5 + 2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(3+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \\
 & \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) + \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 4\left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, \right. \right. \right. \\
 & \left. \left. 4+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
 & \left. (2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 5+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \Big) + \\
 192 & \left(\cos\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^{5+2m} \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \\
 & \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^{2(1+m)} \\
 & \left(-\left(\left(-\frac{1}{6}(5+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 6+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \frac{1}{3} \right. \right. \\
 & \left. \left. (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 5+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) \Big) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, \right. \right. \right. \\
 & \left. \left. 5+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
 & \left. (5+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(3+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \Big) + \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) /
 \end{aligned}$$

$$\begin{aligned}
& \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left(2(1+m) \left(-\frac{3}{10}(5+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -1-2m, \right.\right.\right. \\
& \quad \left.\left.\left.6+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \\
& \quad \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{3}{10}(-1-2m) \operatorname{AppellF1}\left[\frac{5}{2}, -2m, \right. \\
& \quad \left.5+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \\
& \quad \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \\
& \quad (5+2m) \left(-\frac{3}{5}(3+m) \operatorname{AppellF1}\left[\frac{5}{2}, -2(1+m), 1+2(3+m), \frac{7}{2}, \tan\left[\frac{1}{4}\right.\right.\right. \\
& \quad \left.\left.\left.(-c + \frac{\pi}{2} - dx)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \\
& \quad \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \frac{3}{5}(1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 1-2(1+m), \right. \\
& \quad \left.2(3+m), \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \\
& \quad \left.\left.\left.\sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)\right)\right) / \\
& \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 5+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right.\right. \\
& \quad \left.\left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 2\left(2(1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, \right.\right.\right. \\
& \quad \left.\left.\left.5+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right.\right. \\
& \quad \left.\left.(5+2m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 2(3+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right.\right.\right. \\
& \quad \left.\left.\left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) - \right. \\
& \quad \left.\left(\operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right.\right.\right. \\
& \quad \left.\left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \\
& \quad \left(-2\left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, 4+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right.\right.\right. \\
& \quad \left.\left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), \right.\right. \\
& \quad \left.\left.5+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \\
& \quad \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + 3\left(-\frac{1}{3}(2+m) \right. \\
& \quad \left.\operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 1+2(2+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right.\right. \\
& \quad \left.\left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \right.
\end{aligned}$$

$$\begin{aligned}
 & \frac{1}{3} (1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 1-2(1+m), 2(2+m), \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] - 4 \\
 & \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \left((1+m) \left(-\frac{3}{10} (4+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -1-2m, \right. \right. \right. \\
 & \quad \left. \left. \left. 5+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \right. \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] + \frac{3}{10} (-1-2m) \operatorname{AppellF1}\left[\frac{5}{2}, \right. \\
 & \quad \left. -2m, 4+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] \right) + (2+m) \\
 & \quad \left(-\frac{3}{10} (5+2m) \operatorname{AppellF1}\left[\frac{5}{2}, -2(1+m), 6+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] - \frac{3}{5} (1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 1-2(1+m), \right. \right. \\
 & \quad \left. \left. 5+2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \\
 & \quad \left. \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] \right) \right) \right) / \\
 & \left(3 \operatorname{AppellF1}\left[\frac{1}{2}, -2(1+m), 2(2+m), \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] - 4 \left((1+m) \operatorname{AppellF1}\left[\frac{3}{2}, -1-2m, \right. \right. \right. \\
 & \quad \left. \left. \left. 4+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right) + \right. \\
 & \quad \left. (2+m) \operatorname{AppellF1}\left[\frac{3}{2}, -2(1+m), 5+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) \right) \right) \right)
 \end{aligned}$$

Problem 352: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+dx]^2 (a+a \operatorname{Sin}[c+dx])^m dx$$

Optimal (type 5, 73 leaves, 3 steps):

$$\frac{1}{d} 2^{-\frac{1}{2}+m} \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{3}{2}-m, \frac{1}{2}, \frac{1}{2} (1-\operatorname{Sin}[c+dx])\right] \\
 \operatorname{Sec}[c+dx] (1+\operatorname{Sin}[c+dx])^{\frac{1}{2}-m} (a+a \operatorname{Sin}[c+dx])^m$$

Result (type 6, 12061 leaves):

$$\begin{aligned}
 & - \left(\left(\cot \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] (a + a \sin [c + dx]) \right)^m \right. \\
 & \quad \left(1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{2(-1+m)} \left(\frac{1}{1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{2m} \\
 & \quad \left(- \left(\left(5 \operatorname{AppellF1} \left[-\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) / \right. \\
 & \quad \left(\operatorname{AppellF1} \left[-\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
 & \quad 4 \left(m \operatorname{AppellF1} \left[\frac{1}{2}, 2-2m, 1+2m, \frac{3}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-1+m) \operatorname{AppellF1} \left[\frac{1}{2}, 3-2m, 2m, \frac{3}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) + \\
 & \quad \left(15 \operatorname{AppellF1} \left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
 & \quad \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) / \\
 & \quad \left(\operatorname{AppellF1} \left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
 & \quad \frac{4}{3} \left(m \operatorname{AppellF1} \left[\frac{3}{2}, 2-2m, 1+2m, \frac{5}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-1+m) \operatorname{AppellF1} \left[\frac{3}{2}, 3-2m, 2m, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \quad \left(25 \operatorname{AppellF1} \left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
 & \quad \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^4 \right) / \\
 & \quad \left(5 \operatorname{AppellF1} \left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
 & \quad 4 \left(m \operatorname{AppellF1} \left[\frac{5}{2}, 2-2m, 1+2m, \frac{7}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-1+m) \operatorname{AppellF1} \left[\frac{5}{2}, 3-2m, 2m, \frac{7}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \quad \left(7 \operatorname{AppellF1} \left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
 & \quad \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^6 \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(7 \operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] - \right. \\
 & \quad 4 \left(m \operatorname{AppellF1}\left[\frac{7}{2}, 2-2m, 1+2m, \frac{9}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + (-1+m) \operatorname{AppellF1}\left[\frac{7}{2}, 3-2m, 2m, \frac{9}{2}, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) \right) / \\
 & \left(2\theta d \left(\cos\left[\frac{\pi}{4} + \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right)\right] \right)^2 \right. \\
 & \quad \left(\cos\left[\frac{\pi}{4} + \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right)\right] + \sin\left[\frac{\pi}{4} + \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right)\right] \right)^2 \\
 & \quad \left. - \frac{1}{2\theta} (-1+m) \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right. \\
 & \quad \left. \left(1 - \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right)^{-1+2(-1+m)} \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2} \right)^{2m} \right. \\
 & \quad \left(- \left(\left(5 \operatorname{AppellF1}\left[-\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) \right) / \left(\operatorname{AppellF1}\left[-\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) - 4 \left(m \operatorname{AppellF1}\left[\frac{1}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. 2-2m, 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) \right. \right. \\
 & \quad \quad \left. \left. + (-1+m) \operatorname{AppellF1}\left[\frac{1}{2}, 3-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) \right) + \\
 & \quad \left(15 \operatorname{AppellF1}\left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) / \\
 & \quad \left(\operatorname{AppellF1}\left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) - \right. \\
 & \quad \frac{4}{3} \left(m \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) \right) + (-1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3-2m, 2m, \frac{5}{2}, \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) \tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(25 \operatorname{AppellF1} \left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^4 \right) / \\
 & \left(5 \operatorname{AppellF1} \left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
 & \quad 4 \left(m \operatorname{AppellF1} \left[\frac{5}{2}, 2-2m, 1+2m, \frac{7}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-1+m) \operatorname{AppellF1} \left[\frac{5}{2}, 3-2m, 2m, \frac{7}{2}, \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \left(7 \operatorname{AppellF1} \left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^6 \right) / \\
 & \left(7 \operatorname{AppellF1} \left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
 & \quad 4 \left(m \operatorname{AppellF1} \left[\frac{7}{2}, 2-2m, 1+2m, \frac{9}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-1+m) \operatorname{AppellF1} \left[\frac{7}{2}, 3-2m, 2m, \frac{9}{2}, \operatorname{Tan} \left[\right. \right. \right. \\
 & \quad \quad \quad \left. \left. \frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) - \\
 & \frac{1}{80} \operatorname{Csc} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \left(1 - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{2(-1+m)} \\
 & \left(\frac{1}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{2m} \\
 & \left(- \left(\left(5 \operatorname{AppellF1} \left[-\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \right) / \left(\operatorname{AppellF1} \left[-\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - 4 \left(m \operatorname{AppellF1} \left[\frac{1}{2}, \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. 2-2m, 1+2m, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) + \right. \\
 & \quad \left. (-1+m) \operatorname{AppellF1} \left[\frac{1}{2}, 3-2m, 2m, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \left(15 \operatorname{AppellF1} \left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(\text{AppellF1}\left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] - \right. \\
 & \quad \frac{4}{3} \left(m \text{AppellF1}\left[\frac{3}{2}, 2-2m, 1+2m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + (-1+m) \text{AppellF1}\left[\frac{3}{2}, 3-2m, 2m, \frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right) \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) + \\
 & \left(25 \text{AppellF1}\left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \\
 & \quad \left. \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^4 \right) / \\
 & \left(5 \text{AppellF1}\left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] - \right. \\
 & \quad 4 \left(m \text{AppellF1}\left[\frac{5}{2}, 2-2m, 1+2m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + (-1+m) \text{AppellF1}\left[\frac{5}{2}, 3-2m, 2m, \frac{7}{2}, \right. \right. \\
 & \quad \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right) \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) + \\
 & \left(7 \text{AppellF1}\left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \\
 & \quad \left. \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^6 \right) / \\
 & \left(7 \text{AppellF1}\left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] - \right. \\
 & \quad 4 \left(m \text{AppellF1}\left[\frac{7}{2}, 2-2m, 1+2m, \frac{9}{2}, \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + (-1+m) \text{AppellF1}\left[\frac{7}{2}, 3-2m, 2m, \frac{9}{2}, \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right) \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right) - \\
 & \frac{1}{20} m \text{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \left(1 - \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)^{2(-1+m)} \\
 & \left(\frac{1}{1 + \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2} \right)^{1+2m} \\
 & \left(- \left(\left(5 \text{AppellF1}\left[-\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right) \right) / \left(\text{AppellF1}\left[-\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \right. \right. \right. \\
 & \quad \left. \left. \left. \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] - 4 \left(m \text{AppellF1}\left[\frac{1}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 2-2m, 1+2m, \frac{3}{2}, \text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right) + \right.
 \end{aligned}$$

$$\begin{aligned}
 & (-1+m) \operatorname{AppellF1}\left[\frac{1}{2}, 3-2m, 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \Bigg) + \\
 & \left(15 \operatorname{AppellF1}\left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right) / \\
 & \left(\operatorname{AppellF1}\left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] - \right. \\
 & \quad \frac{4}{3} \left(m \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 1+2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + (-1+m) \operatorname{AppellF1}\left[\frac{3}{2}, 3-2m, 2m, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \Bigg) + \\
 & \left(25 \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^4\right) / \\
 & \left(5 \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] - \right. \\
 & \quad 4 \left(m \operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 1+2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + (-1+m) \operatorname{AppellF1}\left[\frac{5}{2}, 3-2m, 2m, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \Bigg) + \\
 & \left(7 \operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^6\right) / \\
 & \left(7 \operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] - \right. \\
 & \quad 4 \left(m \operatorname{AppellF1}\left[\frac{7}{2}, 2-2m, 1+2m, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + (-1+m) \operatorname{AppellF1}\left[\frac{7}{2}, 3-2m, 2m, \frac{9}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right) \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \Bigg) + \\
 & \frac{1}{2\theta} \operatorname{Cot}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] \left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)^{2(-1+m)} \\
 & \quad \left(\frac{1}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2}\right)^{2m}
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \\
 & \frac{5}{14}(2-2m) \operatorname{AppellF1}\left[\frac{7}{2}, 3-2m, 2m, \frac{9}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \\
 & \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right] \Big/ \\
 & \left(7 \operatorname{AppellF1}\left[\frac{5}{2}, 2-2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & 4 \left(m \operatorname{AppellF1}\left[\frac{7}{2}, 2-2m, 1+2m, \frac{9}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-1+m) \operatorname{AppellF1}\left[\frac{7}{2}, 3-2m, 2m, \frac{9}{2}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + \\
 & \left(5 \operatorname{AppellF1}\left[-\frac{1}{2}, 2-2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
 & \left(m \operatorname{AppellF1}\left[\frac{1}{2}, 2-2m, 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \frac{1}{2} \right. \\
 & \left.(2-2m) \operatorname{AppellF1}\left[\frac{1}{2}, 3-2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - 2 \right. \\
 & \left(m \operatorname{AppellF1}\left[\frac{1}{2}, 2-2m, 1+2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-1+m) \operatorname{AppellF1}\left[\frac{1}{2}, 3-2m, \right. \right. \\
 & \left. \left. 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \\
 & \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - 4 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
 & \left(m\left(-\frac{1}{6}(1+2m) \operatorname{AppellF1}\left[\frac{3}{2}, 2-2m, 2+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \right. \\
 & \left. \left. \frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \right. \\
 & \left. \frac{1}{6}(2-2m) \operatorname{AppellF1}\left[\frac{3}{2}, 3-2m, 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) + (-1+m) \left(-\frac{1}{3}m \operatorname{AppellF1}\left[\frac{3}{2}, 3-2m, \right. \right. \\
 & \left. \left. 1+2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
 & \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{1}{6}(3-2m) \operatorname{AppellF1}\left[\right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{3}{2}, 4 - 2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
 & \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \Bigg) \Bigg) \Bigg) \Bigg) \Bigg) / \\
 & \left(\text{AppellF1}\left[-\frac{1}{2}, 2 - 2m, 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & \quad 4 \left(m \text{AppellF1}\left[\frac{1}{2}, 2 - 2m, 1 + 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\right. \right. \right. \\
 & \quad \left. \left. \left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-1 + m) \text{AppellF1}\left[\frac{1}{2}, 3 - 2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) - \\
 & \left. \left(15 \text{AppellF1}\left[\frac{1}{2}, 2 - 2m, 2m, \frac{3}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left(-\frac{1}{3} m \text{AppellF1}\left[\frac{3}{2}, 2 - 2m, 1 + 2m, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{1}{6} (2 - 2m) \right. \\
 & \quad \left. \text{AppellF1}\left[\frac{3}{2}, 3 - 2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \frac{2}{3} \left(m \text{AppellF1}\left[\frac{3}{2}, 2 - 2m, 1 + 2m, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-1 + m) \text{AppellF1}\left[\right. \right. \right. \\
 & \quad \left. \left. \left. \frac{3}{2}, 3 - 2m, 2m, \frac{5}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \frac{4}{3} \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \\
 & \quad \left. \left(m \left(-\frac{3}{10} (1 + 2m) \text{AppellF1}\left[\frac{5}{2}, 2 - 2m, 2 + 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{3}{10} (2 - 2m) \text{AppellF1}\left[\frac{5}{2}, 3 - 2m, 1 + 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\right. \right. \right. \\
 & \quad \left. \left. \left. \left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) + (-1 + m) \left(-\frac{3}{5} m \text{AppellF1}\left[\frac{5}{2}, 3 - 2m, \right. \right. \right. \\
 & \quad \left. \left. \left. 1 + 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{3}{10} (3 - 2m) \text{AppellF1}\left[\right. \right. \\
 & \quad \left. \left. \frac{5}{2}, 4 - 2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \text{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\bigg)\bigg)\bigg)\bigg)\bigg)\bigg) / \\
 & \left(\text{AppellF1}\left[\frac{1}{2}, 2-2m, 2m, \frac{3}{2}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & \quad \frac{4}{3} \left(m \text{AppellF1}\left[\frac{3}{2}, 2-2m, 1+2m, \frac{5}{2}, \right. \right. \\
 & \quad \quad \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + \\
 & \quad \quad (-1+m) \text{AppellF1}\left[\frac{3}{2}, 3-2m, 2m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \\
 & \quad \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) - \right. \\
 & \left(25 \text{AppellF1}\left[\frac{3}{2}, 2-2m, 2m, \frac{5}{2}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
 & \quad \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^4 \left(-2 \left(m \text{AppellF1}\left[\frac{5}{2}, 2-2m, 1+2m, \frac{7}{2}, \right. \right. \right. \\
 & \quad \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + (-1+m) \text{AppellF1}\left[\right. \right. \\
 & \quad \quad \left. \left. \frac{5}{2}, 3-2m, 2m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \\
 & \quad \text{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + 5 \left(-\frac{3}{5} m \text{AppellF1}\left[\frac{5}{2}, \right. \right. \\
 & \quad \quad \left. \left. 2-2m, 1+2m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right. \\
 & \quad \quad \left. \text{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{3}{10} (2-2m) \text{AppellF1}\left[\right. \right. \\
 & \quad \quad \left. \left. \frac{5}{2}, 3-2m, 2m, \frac{7}{2}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right. \\
 & \quad \quad \left. \text{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) - 4 \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
 & \left(m \left(-\frac{5}{14} (1+2m) \text{AppellF1}\left[\frac{7}{2}, 2-2m, 2+2m, \frac{9}{2}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \text{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \text{Tan}\left[\right. \right. \\
 & \quad \quad \left. \left. \frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{5}{14} (2-2m) \text{AppellF1}\left[\frac{7}{2}, 3-2m, 1+2m, \frac{9}{2}, \text{Tan}\left[\frac{1}{4} \right. \right. \right. \\
 & \quad \quad \quad \left. \left. \left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \text{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \\
 & \quad \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) + (-1+m) \left(-\frac{5}{7} m \text{AppellF1}\left[\frac{7}{2}, 3-2m, \right. \right. \\
 & \quad \quad \left. \left. 1+2m, \frac{9}{2}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \\
 & \quad \text{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{5}{14} (3-2m) \text{AppellF1}\left[\right. \\
 & \quad \quad \frac{7}{2}, 4-2m, 2m, \frac{9}{2}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right]
 \end{aligned}$$

$$\begin{aligned}
& 2m, \frac{11}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
& \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \Big) \Big) \Big) \Big) / \\
& \left(7 \operatorname{AppellF1}\left[\frac{5}{2}, 2 - 2m, 2m, \frac{7}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]^2 - \right. \\
& \quad 4 \left(m \operatorname{AppellF1}\left[\frac{7}{2}, 2 - 2m, 1 + 2m, \frac{9}{2}, \right. \right. \\
& \quad \quad \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + \\
& \quad \left. (-1 + m) \operatorname{AppellF1}\left[\frac{7}{2}, 3 - 2m, 2m, \frac{9}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \right) \Big) \Big) \Big) \Big)
\end{aligned}$$

Problem 353: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \sec[c + dx]^4 (a + a \sin[c + dx])^m dx$$

Optimal (type 5, 83 leaves, 3 steps):

$$\frac{1}{3ad} 2^{-\frac{3}{2}+m} \operatorname{Hypergeometric2F1}\left[-\frac{3}{2}, \frac{5}{2} - m, -\frac{1}{2}, \frac{1}{2} (1 - \sin[c + dx])\right] \sec[c + dx]^3 (1 + \sin[c + dx])^{\frac{1}{2}-m} (a + a \sin[c + dx])^{1+m}$$

Result (type 6, 3545 leaves):

$$\begin{aligned}
& \left(\operatorname{AppellF1}\left[-\frac{3}{2}, 4 - 2m, -7 + 2m, -\frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
& \quad \left. \cos\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^{2m} \operatorname{Csc}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^{13} \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] (a + a \sin[c + dx])^m \right) / \\
& \left(192d \left(-1 + \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^4 \left(2(-7 + 2m) \operatorname{AppellF1}\left[-\frac{1}{2}, 4 - 2m, \right. \right. \right. \\
& \quad \left. \left. -6 + 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + 4(-2 + m) \right. \right. \\
& \quad \left. \operatorname{AppellF1}\left[-\frac{1}{2}, 5 - 2m, -7 + 2m, \frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \quad \left. \operatorname{AppellF1}\left[-\frac{3}{2}, 4 - 2m, -7 + 2m, -\frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
& \quad \left. \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \left(\cos\left[\frac{\pi}{4} + \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right)\right] - \sin\left[\frac{\pi}{4} + \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right)\right] \right)^4 \\
& \left(\cos\left[\frac{\pi}{4} + \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right)\right] + \sin\left[\frac{\pi}{4} + \frac{1}{2}\left(c - \frac{\pi}{2} + dx\right)\right] \right)^4 \\
& \left(\left(13 \operatorname{AppellF1}\left[-\frac{3}{2}, 4 - 2m, -7 + 2m, -\frac{1}{2}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \left(\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \text{AppellF1} \left[-\frac{3}{2}, 4-2m, -7+2m, \right. \\
 & \left. -\frac{1}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \cot \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \Big) - \\
 & \left(\cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^{2m} \csc \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^{13} \sec \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \right. \\
 & \left(-\frac{3}{2} (-7+2m) \text{AppellF1} \left[-\frac{1}{2}, 4-2m, -6+2m, \frac{1}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \sec \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \frac{3}{2} (4-2m) \text{AppellF1} \left[-\frac{1}{2}, 5-2m, -7+2m, \frac{1}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \\
 & \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \sec \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \Big) / \\
 & \left(192 \left(-1 + \cot \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^4 \left(2 (-7+2m) \text{AppellF1} \left[-\frac{1}{2}, 4-2m, \right. \right. \right. \\
 & \left. \left. -6+2m, \frac{1}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \right. \\
 & \left. 4 (-2+m) \text{AppellF1} \left[-\frac{1}{2}, 5-2m, -7+2m, \frac{1}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \text{AppellF1} \left[-\frac{3}{2}, 4-2m, -7+2m, -\frac{1}{2}, \right. \right. \\
 & \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \cot \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \Big) + \\
 & \left(\text{AppellF1} \left[-\frac{3}{2}, 4-2m, -7+2m, -\frac{1}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
 & \left. \cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^{2m} \csc \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^{13} \sec \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \left(-\frac{1}{2} \text{AppellF1} \left[\right. \right. \right. \\
 & \left. \left. \left. -\frac{3}{2}, 4-2m, -7+2m, -\frac{1}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \right. \\
 & \left. \left. \cot \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \csc \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 + \cot \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right. \right. \\
 & \left. \left. \left(-\frac{3}{2} (-7+2m) \text{AppellF1} \left[-\frac{1}{2}, 4-2m, -6+2m, \frac{1}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \sec \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \right. \\
 & \left. \frac{3}{2} (4-2m) \text{AppellF1} \left[-\frac{1}{2}, 5-2m, -7+2m, \frac{1}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \sec \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \Big) + \\
 & 2 (-7+2m) \left(\frac{1}{2} (-6+2m) \text{AppellF1} \left[\frac{1}{2}, 4-2m, -5+2m, \frac{3}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \left. \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \sec \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) - \right. \\
 & \left. \frac{1}{2} (4-2m) \text{AppellF1} \left[\frac{1}{2}, 5-2m, -6+2m, \frac{3}{2}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] + \\
 & 4(-2+m)\left(\frac{1}{2}(-7+2m) \operatorname{AppellF1}\left[\frac{1}{2}, 5-2m, -6+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] - \right. \\
 & \quad \left.\frac{1}{2}(5-2m) \operatorname{AppellF1}\left[\frac{1}{2}, 6-2m, -7+2m, \frac{3}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)\right) / \\
 & \left(192\left(-1+\operatorname{Cot}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)^4\left(2(-7+2m) \operatorname{AppellF1}\left[-\frac{1}{2}, 4-2m, -6+2m,\right.\right.\right. \\
 & \quad \left.\left.\frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + \right. \\
 & \quad \left.4(-2+m) \operatorname{AppellF1}\left[-\frac{1}{2}, 5-2m, -7+2m, \frac{1}{2}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + \operatorname{AppellF1}\left[-\frac{3}{2}, 4-2m, -7+2m, -\frac{1}{2},\right.\right. \\
 & \quad \left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Cot}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\right)
 \end{aligned}$$

Problem 354: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (e \operatorname{Cos}[c+dx])^{5/2} (a+a \operatorname{Sin}[c+dx])^m dx$$

Optimal (type 5, 88 leaves, 3 steps):

$$\begin{aligned}
 & -\frac{1}{7de} 2^{\frac{11}{4}+m} a (e \operatorname{Cos}[c+dx])^{7/2} \operatorname{Hypergeometric2F1}\left[\frac{7}{4}, -\frac{3}{4}-m, \frac{11}{4}, \frac{1}{2}(1-\operatorname{Sin}[c+dx])\right] \\
 & (1+\operatorname{Sin}[c+dx])^{-\frac{3}{4}-m} (a+a \operatorname{Sin}[c+dx])^{-1+m}
 \end{aligned}$$

Result (type 6, 32821 leaves): Display of huge result suppressed!

Problem 355: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int (e \operatorname{Cos}[c+dx])^{3/2} (a+a \operatorname{Sin}[c+dx])^m dx$$

Optimal (type 5, 88 leaves, 3 steps):

$$\begin{aligned}
 & -\frac{1}{5de} 2^{\frac{9}{4}+m} a (e \operatorname{Cos}[c+dx])^{5/2} \operatorname{Hypergeometric2F1}\left[\frac{5}{4}, -\frac{1}{4}-m, \frac{9}{4}, \frac{1}{2}(1-\operatorname{Sin}[c+dx])\right] \\
 & (1+\operatorname{Sin}[c+dx])^{-\frac{1}{4}-m} (a+a \operatorname{Sin}[c+dx])^{-1+m}
 \end{aligned}$$

Result (type 6, 13703 leaves):

$$\begin{aligned}
 & \left(64 \cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^{-2m} \left(e \cos [c + dx] \right)^{3/2} \left(a + a \sin [c + dx] \right)^m \right. \\
 & \quad \left(\cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^{2m} \cos [c + dx]^{7/2} + \cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^{2m} \cos [c + dx]^{3/2} \sin [c + dx]^2 \right) \\
 & \quad \left(1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \right)^{2m} \left(\frac{1}{1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{3+2m} \\
 & \quad \sqrt{\frac{\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^3}{\left(1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2}} \\
 & \quad \left(\left(25 \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \right. \\
 & \quad \left. \left. \left(1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) \right) / \\
 & \quad \left(-5 \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) + \\
 & \quad 2 \left((6 + 4m) \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (1 + 4m) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \quad \left(25 \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) / \\
 & \quad \left(5 \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) - \\
 & \quad 2 \left(4(2 + m) \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2} - 2m, 5 + 2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (1 + 4m) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \quad 9 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \left(- \left(\operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \left(1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) / \left(-9 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2} - \right. \right. \right. \\
 & \quad \left. \left. 2m, 3 + 2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) + \\
 & \quad 2 \left((6 + 4m) \operatorname{AppellF1} \left[\frac{9}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (1 + 4m) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{13}{4}, \tan \left[\right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right)^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \text{AppellF1} \left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] / \\
 & \left(-9 \text{AppellF1} \left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \right. \right. \\
 & \quad \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \\
 & \quad 2 \left(4(2+m) \text{AppellF1} \left[\frac{9}{4}, -\frac{1}{2} - 2m, 5 + 2m, \frac{13}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (1+4m) \text{AppellF1} \left[\frac{9}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \tan \left[\right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) \Bigg) / \\
 & \left(5 d \cos [c + dx]^{3/2} \left(\frac{64}{5} m \sec \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \right. \right. \\
 & \quad \left. \left. \left(1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{-1+2m} \right. \right. \\
 & \quad \left. \left. \left(\frac{1}{1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{3+2m} \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^3}{\left(1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2}} \right. \right. \\
 & \quad \left. \left. \left(\left(25 \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \right. \right. \right. \\
 & \quad \left. \left. \left(1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) \right) / \left(-5 \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
 & \quad \left. \left. \left. 3 + 2m, \frac{5}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \right. \\
 & \quad \left. \left. 2 \left((6+4m) \text{AppellF1} \left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (1+4m) \text{AppellF1} \left[\frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \right. \right. \right. \\
 & \quad \left. \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \right. \\
 & \quad \left. \left(25 \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \right) \right) \Bigg) /
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\bigg] \bigg/ \\
 & \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}-2m, 4+2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] - \right. \\
 & 2\left(4(2+m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 5+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m, 4+2m, \frac{9}{4}, \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right) + \\
 & 9 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \left(-\left(\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 3+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\right) \bigg/ \\
 & \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 3+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + 2\left((6+4m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, \right. \right. \right. \\
 & \left. \left. 4+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + \right. \\
 & \left. (1+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 3+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right) \right) + \\
 & \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 4+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \bigg/ \\
 & \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 4+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + 2\left(4(2+m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, \right. \right. \right. \\
 & \left. \left. 5+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + \right. \\
 & \left. (1+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 4+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right) \right) \bigg) + \\
 & \frac{32}{5}(3+2m) \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] \\
 & \left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)^{2m} \\
 & \left(\frac{1}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2}\right)^{4+2m}
 \end{aligned}$$

$$\begin{aligned}
& \sqrt{\frac{\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^3}{\left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^2}} \\
& \left(\left(25 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \right. \\
& \quad \left. \left. \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^2 \right) \right) / \left(-5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, \right. \right. \\
& \quad \left. \left. 3 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \quad 2 \left((6 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (1 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
& \quad \left(25 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) / \\
& \quad \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
& \quad 2 \left(4(2 + m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 5 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (1 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
& \quad 9 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left(- \left(\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^2 \right) \right) / \\
& \quad \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + 2 \left((6 + 4m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
& \quad \left. \left. 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \quad \left. (1 + 4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \right) + \\
& \quad \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] / \\
& \quad \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+2\left(4(2+m)\operatorname{AppellF1}\left[\frac{9}{4},-\frac{1}{2}-2m,\right.\right. \\
 & \quad \left.\left.5+2m,\frac{13}{4},\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+ \right. \\
 & \quad \left.(1+4m)\operatorname{AppellF1}\left[\frac{9}{4},\frac{1}{2}-2m,4+2m,\frac{13}{4},\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right)\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\right)- \\
 & \frac{1}{5\sqrt{\frac{\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^3}{\left(1+\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)^2}}}32\left(1-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)^{2m} \\
 & \left(\frac{1}{1+\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2}\right)^{3+2m} \\
 & \left(\left(\frac{1}{4}\sec\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2-\frac{3}{4}\sec\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)/\right. \\
 & \quad \left.\left(1+\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)^2-\left(\sec\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right.\right. \\
 & \quad \left.\left.\left(\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^3\right)\right)/\left(1+\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)^3\right) \\
 & \left(\left(25\operatorname{AppellF1}\left[\frac{1}{4},-\frac{1}{2}-2m,3+2m,\frac{5}{4},\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right.\right. \\
 & \quad \left.\left.\left(1+\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\right)/\left(-5\operatorname{AppellF1}\left[\frac{1}{4},-\frac{1}{2}-2m,\right.\right.\right. \\
 & \quad \left.\left.\left.3+2m,\frac{5}{4},\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+ \right.\right. \\
 & \quad \left.\left.2\left((6+4m)\operatorname{AppellF1}\left[\frac{5}{4},-\frac{1}{2}-2m,4+2m,\frac{9}{4},\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right.\right. \right. \\
 & \quad \left.\left.\left.-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+(1+4m)\operatorname{AppellF1}\left[\frac{5}{4},\frac{1}{2}-2m,3+2m,\frac{9}{4},\right.\right.\right. \\
 & \quad \left.\left.\left.\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right)\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)+ \\
 & \left(25\operatorname{AppellF1}\left[\frac{1}{4},-\frac{1}{2}-2m,4+2m,\frac{5}{4},\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right. \\
 & \quad \left.\left.-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right)/\left(5\operatorname{AppellF1}\left[\frac{1}{4},-\frac{1}{2}-2m,4+2m,\right.\right. \\
 & \quad \left.\left.\frac{5}{4},\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]- \right. \\
 & \quad \left.2\left(4(2+m)\operatorname{AppellF1}\left[\frac{5}{4},-\frac{1}{2}-2m,5+2m,\frac{9}{4},\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right.\right. \\
 & \quad \left.\left.\left.-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+(1+4m)\operatorname{AppellF1}\left[\frac{5}{4},\frac{1}{2}-2m,4+2m,\frac{9}{4},\right.\right.\right. \\
 & \quad \left.\left.\left.\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right)\tan\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)+
 \end{aligned}$$

$$\begin{aligned}
 & 9 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\left(-\left(\operatorname{AppellF1}\left[\frac{5}{4},-\frac{1}{2}-2 m, 3+2 m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right.\right.\right. \\
 & \quad \left.\left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)\right) / \right. \\
 & \quad \left(-9 \operatorname{AppellF1}\left[\frac{5}{4},-\frac{1}{2}-2 m, 3+2 m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right.\right. \\
 & \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]+2\left((6+4 m) \operatorname{AppellF1}\left[\frac{9}{4},-\frac{1}{2}-2 m, \right.\right. \\
 & \quad \left.4+2 m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)+ \\
 & \quad \left.(1+4 m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2 m, 3+2 m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right.\right. \\
 & \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)\left.\right) \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)+\operatorname{AppellF1}\left[\frac{5}{4}, \right. \\
 & \quad \left.-\frac{1}{2}-2 m, 4+2 m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right) / \\
 & \quad \left(-9 \operatorname{AppellF1}\left[\frac{5}{4},-\frac{1}{2}-2 m, 4+2 m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right.\right. \\
 & \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right]+2\left(4(2+m) \operatorname{AppellF1}\left[\frac{9}{4},-\frac{1}{2}-2 m, \right.\right. \\
 & \quad \left.5+2 m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)+ \\
 & \quad \left.(1+4 m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2 m, 4+2 m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right.\right. \\
 & \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)\left.\right) \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)\right)- \\
 & \frac{64}{5}\left(1-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)^{2 m}\left(\frac{1}{1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2}\right)^{3+2 m} \\
 & \sqrt{\frac{\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^3}{\left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)^2}} \\
 & \left(\left(25 \operatorname{AppellF1}\left[\frac{1}{4},-\frac{1}{2}-2 m, 3+2 m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)\right.\right. \\
 & \quad \left.\left.\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]\right) / \right. \\
 & \quad \left(2\left(-5 \operatorname{AppellF1}\left[\frac{1}{4},-\frac{1}{2}-2 m, 3+2 m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right.\right.\right. \\
 & \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)+2\left((6+4 m) \operatorname{AppellF1}\left[\frac{5}{4},-\frac{1}{2}-2 m, \right.\right. \\
 & \quad \left.4+2 m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right)+ \\
 & \quad \left.(1+4 m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2 m, 3+2 m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-d x\right)\right]^2\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) + \\
 & \left(25\left(-\frac{1}{10}(3+2m)\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 4+2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2,\right.\right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \\
 & \quad \frac{1}{10}\left(-\frac{1}{2}-2m\right)\operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m, 3+2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \Big) \\
 & \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \Big) \Big/ \left(-5\operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}-2m, 3+2m, \right.\right. \\
 & \quad \left.\frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \\
 & \quad 2\left((6+4m)\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 4+2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2,\right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + (1+4m)\operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m, 3+2m, \frac{9}{4}, \right. \\
 & \quad \left.\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) + \\
 & \left(25\left(-\frac{1}{10}(4+2m)\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 5+2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2,\right.\right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \\
 & \quad \frac{1}{10}\left(-\frac{1}{2}-2m\right)\operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m, 4+2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \Big) \Big) \Big/ \\
 & \left(5\operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}-2m, 4+2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & \quad \left. 2\left(4(2+m)\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 5+2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2,\right.\right. \\
 & \quad \left.-\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + (1+4m)\operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m, 4+2m, \frac{9}{4}, \right. \\
 & \quad \left.\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) + \\
 & \frac{9}{2} \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \left(-\left(\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, \right.\right.\right. \\
 & \quad \left.\left.3+2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)\right) \\
 & \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \Big) \Big/ \left(-9\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 3+2m, \frac{9}{4}, \right.\right. \\
 & \quad \left.\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + 2\left((6+4m)\operatorname{AppellF1}\left[\frac{9}{4}, \right.\right. \\
 & \quad \left.-\frac{1}{2}-2m, 4+2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) +
 \end{aligned}$$

$$\begin{aligned}
 & (1+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 3+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \\
 & \quad \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2) + \\
 & \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 4+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] / \\
 & \quad \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 4+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + 2\left(4(2+m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, \right. \right. \right. \\
 & \quad \left. \left. 5+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (1+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 4+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right) - \right. \\
 & \left. \left(25 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}-2m, 3+2m, \frac{5}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \left(1+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right) \right. \right. \\
 & \quad \left. \left. \left(\left((6+4m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 4+2m, \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m, 3+2m, \frac{9}{4}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] - 5\left(-\frac{1}{10}(3+2m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}-2m, 4+2m, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{9}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] + \frac{1}{10}\left(-\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}-2m, 3+2m, \frac{9}{4}, \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right) + 2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \left((6+4m) \right. \right. \\
 & \quad \left. \left. \left(-\frac{5}{18}(4+2m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2}-2m, 5+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] + \right. \right. \\
 & \quad \left. \left. \frac{5}{18}\left(-\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 4+2m, \frac{13}{4}, \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right) + \right. \\
 & \left. (1+4m) \left(-\frac{5}{18}(3+2m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}-2m, 4+2m, \frac{13}{4}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
 & \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{5}{18}\left(\frac{1}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2} - 2m, \right. \\
 & \left. 3 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \\
 & \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) \Big/ \\
 & \left(-5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
 & \quad 2\left((6 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (1 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2 - \\
 & \left(25 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \\
 & \left(-\left(4(2 + m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 5 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (1 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
 & \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + 5\left(-\frac{1}{10}(4 + 2m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 5 + 2m, \right. \right. \\
 & \quad \left. \left. \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \\
 & \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{1}{10}\left(-\frac{1}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
 & \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - 2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left(4(2 + m) \right. \\
 & \quad \left(-\frac{5}{18}(5 + 2m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, 6 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \right. \\
 & \quad \left. \frac{5}{18}\left(-\frac{1}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 5 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) + \\
 & (1 + 4m) \left(-\frac{5}{18}(4 + 2m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 5 + 2m, \frac{13}{4}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left(\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
& \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{5}{18}\left(\frac{1}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2} - 2m, \right. \\
& \left. 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \\
& \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) \Big/ \\
& \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
& \left. 2\left(4(2+m) \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 5 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 4 + 2m, \frac{9}{4}, \right. \right. \right. \\
& \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right)^2 + \\
& 9 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left(- \left(\operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) \Big/ \\
& \left(2\left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + 2\left((6+4m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
& \left. \left. 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \left. (1+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \Big) - \\
& \left(\left(-\frac{5}{18}(3+2m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \right. \\
& \left. \frac{5}{18}\left(-\frac{1}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) \\
& \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \Big) \Big/ \left(-9 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2} - 2m, 3 + 2m, \right. \right. \\
& \left. \left. \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \left. 2\left((6+4m) \operatorname{AppellF1}\left[\frac{9}{4}, -\frac{1}{2} - 2m, 4 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2} - 2m, 3 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right)^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \left(-\frac{5}{18} (4+2m) \operatorname{AppellF1} \left[\frac{9}{4}, -\frac{1}{2} - 2m, 5+2m, \frac{13}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right], \right. \\
 & \quad \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] + \right. \\
 & \quad \left. \frac{5}{18} \left(-\frac{1}{2} - 2m \right) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2} - 2m, 4+2m, \frac{13}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right], \right. \\
 & \quad \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \right) / \\
 & \left(-9 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2} - 2m, 4+2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right], \right. \\
 & \quad \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + 2 \left(4(2+m) \operatorname{AppellF1} \left[\frac{9}{4}, -\frac{1}{2} - 2m, \right. \right. \\
 & \quad \left. \left. 5+2m, \frac{13}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right], -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \quad (1+4m) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2} - 2m, 4+2m, \frac{13}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right], \\
 & \quad \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \left(\operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2} - 2m, 3+2m, \frac{9}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right], -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \\
 & \quad \left(1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \left(\left((6+4m) \operatorname{AppellF1} \left[\frac{9}{4}, -\frac{1}{2} - 2m, 4+2m, \right. \right. \right. \\
 & \quad \left. \left. \frac{13}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right], -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \right. \\
 & \quad \left. (1+4m) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2} - 2m, 3+2m, \frac{13}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right], \right. \\
 & \quad \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] - \\
 & \quad 9 \left(-\frac{5}{18} (3+2m) \operatorname{AppellF1} \left[\frac{9}{4}, -\frac{1}{2} - 2m, 4+2m, \frac{13}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right], \right. \\
 & \quad \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] + \\
 & \quad \frac{5}{18} \left(-\frac{1}{2} - 2m \right) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2} - 2m, 3+2m, \frac{13}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right], \\
 & \quad \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \right) + \\
 & \quad 2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \left((6+4m) \left(-\frac{9}{26} (4+2m) \operatorname{AppellF1} \left[\frac{13}{4}, -\frac{1}{2} - 2m, \right. \right. \right. \\
 & \quad \left. \left. 5+2m, \frac{17}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right], -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \\
 & \quad \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] + \frac{9}{26} \left(-\frac{1}{2} - 2m \right) \\
 & \quad \operatorname{AppellF1} \left[\frac{13}{4}, \frac{1}{2} - 2m, 4+2m, \frac{17}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right],
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right] \\
 & +\left(1+4m\right)\left(-\frac{9}{26}\left(3+2m\right)\operatorname{AppellF1}\left[\frac{13}{4},\frac{1}{2}-2m,4+2m,\frac{17}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right. \\
 & \left.\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]+\frac{9}{26}\left(\frac{1}{2}-2m\right)\operatorname{AppellF1}\left[\frac{13}{4},\frac{3}{2}-2m,3+2m,\frac{17}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right. \\
 & \left.\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)\right)\right) \\
 & \left(-9\operatorname{AppellF1}\left[\frac{5}{4},-\frac{1}{2}-2m,3+2m,\frac{9}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right. \\
 & \left.+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)+2\left(\left(6+4m\right)\operatorname{AppellF1}\left[\frac{9}{4},-\frac{1}{2}-2m,4+2m,\frac{13}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right. \\
 & \left.+\left(1+4m\right)\operatorname{AppellF1}\left[\frac{9}{4},\frac{1}{2}-2m,3+2m,\frac{13}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right)\right) \\
 & \left(\operatorname{AppellF1}\left[\frac{5}{4},-\frac{1}{2}-2m,4+2m,\frac{9}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right)^2 \\
 & \left(\left(4\left(2+m\right)\operatorname{AppellF1}\left[\frac{9}{4},-\frac{1}{2}-2m,5+2m,\frac{13}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right. \right. \\
 & \left.+\left(1+4m\right)\operatorname{AppellF1}\left[\frac{9}{4},\frac{1}{2}-2m,4+2m,\frac{13}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right)\right) \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]- \\
 & 9\left(-\frac{5}{18}\left(4+2m\right)\operatorname{AppellF1}\left[\frac{9}{4},-\frac{1}{2}-2m,5+2m,\frac{13}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right. \\
 & \left.+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)+ \\
 & \frac{5}{18}\left(-\frac{1}{2}-2m\right)\operatorname{AppellF1}\left[\frac{9}{4},\frac{1}{2}-2m,4+2m,\frac{13}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right. \\
 & \left.+\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)\right) \\
 & 2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\left(4\left(2+m\right)\left(-\frac{9}{26}\left(5+2m\right)\operatorname{AppellF1}\left[\frac{13}{4},-\frac{1}{2}-2m,6+2m,\frac{17}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right. \right. \\
 & \left.\left.+\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]+\frac{9}{26}\left(-\frac{1}{2}-2m\right)\right)\right)
 \end{aligned}$$

$$\begin{aligned}
& \sin\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] (a + a \sin[c + dx])^m \Big/ \\
& \left(d \left(21 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 2 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \right. \\
& \quad 6 \left(4(1+m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2} - 2m, 2 + 2m, \frac{11}{4}, \right. \right. \\
& \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) \\
& \left(\left(14 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 2 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \right. \\
& \quad \left. \cos\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^{1+2m} \sqrt{\cos[c + dx]} \right) \Big/ \\
& \left(21 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 2 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
& \quad 6 \left(4(1+m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2} - 2m, 2 + 2m, \frac{11}{4}, \right. \right. \\
& \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) - \\
& \left(28m \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 2 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \\
& \quad \cos\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^{-1+2m} \sqrt{\cos[c + dx]} \sin\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) \Big/ \\
& \left(21 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 2 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
& \quad 6 \left(4(1+m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2} - 2m, 2 + 2m, \frac{11}{4}, \right. \right. \\
& \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
& \left(14 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 2 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \\
& \quad \cos\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^{2m} \sin\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \sin[c + dx] \Big) \Big/ \\
& \left(\sqrt{\cos[c + dx]} \left(21 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2} - 2m, 2 + 2m, \frac{7}{4}, \right. \right. \right. \\
& \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
& \quad \left. 6 \left(4(1+m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2} - 2m, 3 + 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
& \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2} - 2m, 2 + 2m, \frac{11}{4}, \right. \right. \right. \\
& \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \right) \Big)
\end{aligned}$$

$$\begin{aligned}
 & \left. \left(\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
 & \left(28 \cos\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^{2m} \sqrt{\cos[c+dx]} \sin\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right. \\
 & \quad \left(-\frac{3}{14} (2+2m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}-2m, 3+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \right. \\
 & \quad \left. \frac{3}{14} \left(-\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}-2m, 2+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) \Big/ \\
 & \left(21 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}-2m, 2+2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] - \right. \\
 & \quad 6 \left(4(1+m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}-2m, 3+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}-2m, 2+2m, \frac{11}{4}, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) - \\
 & \left(28 \operatorname{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}-2m, 2+2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right. \\
 & \quad \left. \cos\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^{2m} \sqrt{\cos[c+dx]} \sin\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right] \right. \\
 & \quad \left(-3 \left(4(1+m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}-2m, 3+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (1+4m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}-2m, 2+2m, \frac{11}{4}, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \\
 & \quad \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + 21 \left(-\frac{3}{14} (2+2m) \operatorname{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}-2m, \right. \right. \\
 & \quad \quad \left. \left. 3+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{3}{14} \left(-\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\right. \right. \\
 & \quad \quad \left. \left. \frac{7}{4}, \frac{1}{2}-2m, 2+2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \right. \\
 & \quad \quad \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) - 6 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
 & \quad \left(4(1+m) \left(-\frac{7}{22} (3+2m) \operatorname{AppellF1}\left[\frac{11}{4}, -\frac{1}{2}-2m, 4+2m, \frac{15}{4}, \right. \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{7}{22} \left(-\frac{1}{2}-2m\right) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{1}{2}-2m, 3+2m, \frac{15}{4}, \right. \right. \\
 \end{aligned}$$

$$\begin{aligned}
 & \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
 & \left(-\left(\left(5 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2} - 2m, 2m, \frac{5}{4}, \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right.\right.\right. \\
 & \quad \cos\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^{2m} \sqrt{\cos[c+dx]} \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^4 \\
 & \quad \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^3 \Big/ \left(\left(-1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^2 \left(-8m \operatorname{AppellF1}\left[\frac{5}{4},\right.\right.\right. \\
 & \quad \left.\left.\frac{1}{2} - 2m, 1 + 2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) + \\
 & \quad (2 - 8m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2} - 2m, 2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2,\right. \\
 & \quad \left.-\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + 5 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2} - 2m, 2m, \frac{5}{4},\right. \\
 & \quad \left.\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big)\Big) + \\
 & \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2} - 2m, 2m, \frac{5}{4}, \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right. \\
 & \quad \left.\cos\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]^{2m} \sqrt{\cos[c+dx]} \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^4 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right) \Big/ \\
 & \left(\left(-1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^2 \left(-8m \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 1 + 2m, \frac{9}{4},\right.\right.\right. \\
 & \quad \left.\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (2 - 8m) \right. \\
 & \quad \left.\operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2} - 2m, 2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
 & \quad \left.5 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2} - 2m, 2m, \frac{5}{4}, \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right. \\
 & \quad \left.\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + \left(10 \cos\left[\frac{1}{2}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^{2m} \\
 & \quad \sqrt{\cos[c+dx]} \left(\frac{1}{5} m \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 1 + 2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2,\right.\right. \\
 & \quad \left.-\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \operatorname{Csc}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 - \\
 & \quad \frac{1}{10} \left(\frac{1}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2} - 2m, 2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2,\right. \\
 & \quad \left.-\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \operatorname{Csc}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big/ \left(\left(-1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)^2\right) \\
 & \quad \left(-8m \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2} - 2m, 1 + 2m, \frac{9}{4}, \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2,\right.\right. \\
 & \quad \left.-\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (2 - 8m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2} - 2m, 2m, \frac{9}{4},\right. \\
 & \quad \left.\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + 5 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2} - 2m, 2m,\right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(10 \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
 & \quad \cos \left[\frac{1}{2} \left(-c + \frac{\pi}{2} - dx \right) \right]^{2m} \sqrt{\cos [c + dx]} \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \\
 & \quad \left(-8m \left(\frac{5}{18} (1 + 2m) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2} - 2m, 2 + 2m, \frac{13}{4}, \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. \left. -\operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \operatorname{Csc} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 - \frac{5}{18} \right. \right. \\
 & \quad \quad \left. \left(\frac{1}{2} - 2m \right) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{13}{4}, \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \operatorname{Csc} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \quad (2 - 8m) \left(\frac{5}{9} m \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{13}{4}, \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \operatorname{Csc} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 - \frac{5}{18} \right. \\
 & \quad \quad \left. \left(\frac{3}{2} - 2m \right) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \operatorname{Csc} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \quad \frac{5}{2} \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \\
 & \quad \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] + 5 \left(\frac{1}{5} m \operatorname{AppellF1} \left[\frac{5}{4}, \right. \right. \\
 & \quad \quad \left. \frac{1}{2} - 2m, 1 + 2m, \frac{9}{4}, \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \\
 & \quad \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \operatorname{Csc} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 - \frac{1}{10} \left(\frac{1}{2} - 2m \right) \\
 & \quad \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2} - 2m, 2m, \frac{9}{4}, \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \\
 & \quad \left. \left. \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \operatorname{Csc} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) / \\
 & \quad \left(\left(-1 + \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \left(-8m \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2} - 2m, 1 + 2m, \frac{9}{4}, \right. \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) + \\
 & \quad (2 - 8m) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2} - 2m, 2m, \frac{9}{4}, \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \\
 & \quad \quad \left. -\operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + 5 \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2} - 2m, 2m, \frac{5}{4}, \right. \\
 & \quad \quad \left. \left. \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) \right) \right)
 \end{aligned}$$

Problem 358: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(a + a \sin [c + d x])^m}{(e \cos [c + d x])^{3/2}} dx$$

Optimal (type 5, 82 leaves, 3 steps):

$$\left(2^{\frac{3}{4}+m} \text{Hypergeometric2F1} \left[-\frac{1}{4}, \frac{5}{4} - m, \frac{3}{4}, \frac{1}{2} (1 - \sin [c + d x]) \right] \right. \\ \left. (1 + \sin [c + d x])^{\frac{1}{4}-m} (a + a \sin [c + d x])^m \right) / (d e \sqrt{e \cos [c + d x]})$$

Result (type 6, 10902 leaves):

$$- \left(\left(\cot \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right] (a + a \sin [c + d x])^m \left(1 - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right] \right)^{2(-1+m)} \right. \right. \\ \left. \left(\frac{1}{1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2} \right)^{-1+2m} \sqrt{\frac{\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right] - \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^3}{\left(1 + \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right)^2}} \right. \\ \left. \left(\left(63 \text{AppellF1} \left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) / \right. \right. \\ \left. \left(-3 \text{AppellF1} \left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] + \right. \right. \\ \left. \left. 2 \left(4m \text{AppellF1} \left[\frac{3}{4}, \frac{3}{2} - 2m, 1+2m, \frac{7}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \right. \right. \\ \left. \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] + (-3+4m) \text{AppellF1} \left[\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{7}{4}, \right. \right. \right. \right. \\ \left. \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right) + \right. \\ \left. \left(98 \text{AppellF1} \left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right. \right. \\ \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right) / \right. \\ \left. \left(7 \text{AppellF1} \left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] - \right. \right. \\ \left. \left. 2 \left(4m \text{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2m, 1+2m, \frac{11}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \right. \right. \\ \left. \left. \left. -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] + (-3+4m) \text{AppellF1} \left[\frac{7}{4}, \frac{5}{2} - 2m, 2m, \frac{11}{4}, \right. \right. \right. \right. \\ \left. \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right) + \right. \\ \left. \left(33 \text{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, -\tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right. \right. \\ \left. \left. \tan \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^4 \right) / \right)$$

$$\begin{aligned}
 & \left(11 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
 & \quad 2 \left(4m \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{15}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3 + 4m) \operatorname{AppellF1} \left[\frac{11}{4}, \frac{5}{2} - 2m, 2m, \frac{15}{4}, \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \Bigg) / \\
 & \left(21d \left(e \operatorname{Cos} [c + dx] \right)^{3/2} \left(-\frac{1}{42} (-1 + 2m) \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right. \right. \\
 & \quad \left. \left. \left(1 - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{2(-1+m)} \left(\frac{1}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{2m} \right. \right. \\
 & \quad \left. \left. \sqrt{\frac{\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^3}{\left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2}} \right. \right. \\
 & \quad \left(\left(63 \operatorname{AppellF1} \left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) / \right. \\
 & \quad \left(-3 \operatorname{AppellF1} \left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - \right. \right. \right. \right. \\
 & \quad \quad \left. \left. \left. dx \right) \right]^2 \right) + 2 \left(4m \operatorname{AppellF1} \left[\frac{3}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3 + 4m) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{7}{4}, \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \quad \left(98 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) / \\
 & \quad \left(7 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
 & \quad 2 \left(4m \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{11}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3 + 4m) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{5}{2} - 2m, 2m, \frac{11}{4}, \right. \right. \\
 & \quad \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) +
 \end{aligned}$$

$$\begin{aligned}
 & \left(33 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^4 \right) / \\
 & \left(11 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
 & \quad 2 \left(4m \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{15}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3 + 4m) \operatorname{AppellF1} \left[\frac{11}{4}, \frac{5}{2} - 2m, 2m, \frac{15}{4}, \operatorname{Tan} \left[\right. \right. \right. \\
 & \quad \left. \left. \frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) - \\
 & \frac{1}{21} (-1 + m) \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \left(1 - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{-1+2(-1+m)} \\
 & \left(\frac{1}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{-1+2m} \\
 & \sqrt{\frac{\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^3}{\left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2}} \\
 & \left(\left(63 \operatorname{AppellF1} \left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) / \right. \\
 & \quad \left(-3 \operatorname{AppellF1} \left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - \right. \right. \right. \right. \\
 & \quad \left. \left. \left. dx \right) \right]^2 \right] + 2 \left(4m \operatorname{AppellF1} \left[\frac{3}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3 + 4m) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{7}{4}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \left(98 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \\
 & \quad \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) / \\
 & \left(7 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
 & \quad 2 \left(4m \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{11}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3 + 4m) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{5}{2} - 2m, 2m, \frac{11}{4}, \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \left(33 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^4 \Big/ \\
 & \left(11 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & 2 \left(4m \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{15}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-3 + 4m) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{5}{2} - 2m, 2m, \frac{15}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) - \\
 & \frac{1}{84} \operatorname{Csc}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^{2(-1+m)} \\
 & \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2}\right)^{-1+2m} \\
 & \sqrt{\frac{\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^3}{\left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2}} \\
 & \left(\left(63 \operatorname{AppellF1}\left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right]\right) \Big/ \right. \\
 & \quad \left(-3 \operatorname{AppellF1}\left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - \right. \right. \right. \\
 & \quad \left. \left. dx\right)\right]^2\right] + 2 \left(4m \operatorname{AppellF1}\left[\frac{3}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-3 + 4m) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{7}{4}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) + \\
 & \left(98 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \Big/ \\
 & \left(7 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & 2 \left(4m \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-3 + 4m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{5}{2} - 2m, 2m, \frac{11}{4}, \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) + \\
 & \left(33 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^4 \right) \Big/
 \end{aligned}$$

$$\begin{aligned}
 & \left(11 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
 & \quad 2 \left(4m \operatorname{AppellF1} \left[\frac{11}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{15}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3 + 4m) \operatorname{AppellF1} \left[\frac{11}{4}, \frac{5}{2} - 2m, 2m, \frac{15}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \frac{1}{\sqrt{\frac{\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^3}{\left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2}}} \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \\
 & 42 \sqrt{\frac{\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^3}{\left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2}} \\
 & \left(1 - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{2(-1+m)} \\
 & \left(\frac{1}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{-1+2m} \\
 & \left(\left(63 \operatorname{AppellF1} \left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) / \left(-3 \operatorname{AppellF1} \left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + 2 \left(4m \operatorname{AppellF1} \left[\frac{3}{4}, \right. \right. \right. \\
 & \quad \left. \left. \frac{3}{2} - 2m, 1 + 2m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) + \\
 & \quad \left(-3 + 4m \right) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \\
 & \quad \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \left(98 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) / \\
 & \left(7 \operatorname{AppellF1} \left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
 & \quad 2 \left(4m \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{11}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-3 + 4m) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{5}{2} - 2m, 2m, \frac{11}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) + \\
 & \left(33 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^4 \right) / \left(11 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 - 2 \left(4 m \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{15}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (-3 + 4m) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{5}{2} - 2m, 2m, \frac{15}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \\
 & \left(\left(\frac{1}{4} \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 - \frac{3}{4} \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) / \right. \\
 & \quad \left. \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right)^2 - \left(\sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \left(\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^3 \right) \right) / \left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right)^3 \right) + \\
 & \frac{1}{21} \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right)^{2(-1+m)} \\
 & \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2} \right)^{-1+2m} \\
 & \sqrt{\frac{\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^3}{\left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right)^2}} \\
 & \left(63 \left(\frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \frac{1}{6} \right. \right. \\
 & \quad \left. \left(\frac{3}{2} - 2m \right) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) \right) / \\
 & \left(-3 \operatorname{AppellF1}\left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + 2 \left(4 m \operatorname{AppellF1}\left[\frac{3}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + (-3 + 4m) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
 & \left(49 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) /
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \Bigg) \Bigg) / \\
 & \left(11 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2} - 2m, 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & \quad 2 \left(4m \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{15}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-3 + 4m) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{5}{2} - 2m, 2m, \frac{15}{4}, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) - \\
 & \left(63 \operatorname{AppellF1}\left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
 & \quad \left(\left(4m \operatorname{AppellF1}\left[\frac{3}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-3 + 4m) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{5}{2} - 2m, \right. \right. \\
 & \quad \quad \left. \left. 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - 3 \left(\frac{1}{3} m \operatorname{AppellF1}\left[\frac{3}{4}, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{3}{2} - 2m, 1 + 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \frac{1}{6} \left(\frac{3}{2} - 2m \right) \operatorname{AppellF1}\left[\right. \right. \\
 & \quad \quad \left. \left. \frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) + 2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
 & \left(4m \left(-\frac{3}{14} (1 + 2m) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2} - 2m, 2 + 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - \right. \right. \right. \\
 & \quad \quad \left. \left. dx\right)\right] + \frac{3}{14} \left(\frac{3}{2} - 2m \right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{11}{4}, \tan\left[\frac{1}{4} \right. \right. \\
 & \quad \quad \left. \left. \left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) + (-3 + 4m) \left(-\frac{3}{7} m \operatorname{AppellF1}\left[\frac{7}{4}, \frac{5}{2} - 2m, \right. \right. \\
 & \quad \quad \left. \left. 1 + 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{3}{14} \left(\frac{5}{2} - 2m \right) \operatorname{AppellF1}\left[\right. \right. \\
 & \quad \quad \left. \left. \frac{7}{4}, \frac{7}{2} - 2m, 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \right. \\
 & \quad \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) \Bigg) \Bigg) /
 \end{aligned}$$

$$\begin{aligned}
 & \left(-3 \operatorname{AppellF1}\left[-\frac{1}{4}, \frac{3}{2} - 2m, 2m, \frac{3}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right], \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + 2 \left(4m \operatorname{AppellF1}\left[\frac{3}{4}, \frac{3}{2} - 2m, 1 + 2m, \right. \right. \\
 & \quad \left. \left. \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + \\
 & \quad (-3 + 4m) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right], \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 - \\
 & \left(98 \operatorname{AppellF1}\left[\frac{3}{4}, \frac{3}{2} - 2m, 2m, \frac{7}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \\
 & \quad \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \left(-\left(4m \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2} - 2m, 1 + 2m, \frac{11}{4}, \right. \right. \right. \\
 & \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + (-3 + 4m) \operatorname{AppellF1}\left[\right. \\
 & \quad \left. \frac{7}{4}, \frac{5}{2} - 2m, 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \\
 & \quad \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + 7 \left(-\frac{3}{7}m \operatorname{AppellF1}\left[\frac{7}{4}, \right. \right. \\
 & \quad \left. \left. \frac{3}{2} - 2m, 1 + 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \\
 & \quad \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{3}{14} \left(\frac{3}{2} - 2m \right) \operatorname{AppellF1}\left[\right. \\
 & \quad \left. \frac{7}{4}, \frac{5}{2} - 2m, 2m, \frac{11}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \\
 & \quad \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - 2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
 & \quad \left(4m \left(-\frac{7}{22} (1 + 2m) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{3}{2} - 2m, 2 + 2m, \frac{15}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right], \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \\
 & \quad \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{7}{22} \left(\frac{3}{2} - 2m \right) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{5}{2} - 2m, \right. \\
 & \quad \left. 1 + 2m, \frac{15}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \\
 & \quad \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + (-3 + 4m) \\
 & \quad \left(-\frac{7}{11}m \operatorname{AppellF1}\left[\frac{11}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{15}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right], \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
 & \quad \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{7}{22} \left(\frac{5}{2} - 2m \right) \operatorname{AppellF1}\left[\frac{11}{4}, \frac{7}{2} - 2m, \right. \\
 & \quad \left. 2m, \frac{15}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right], -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right] \right) \right) \left. \right) \left. \right) \left. \right) \left. \right) \left. \right) \left. \right) \left. \right) \left. \right) / \\
 & \left(7 \text{AppellF1} \left[\frac{3}{4}, \frac{3}{2} - 2 m, 2 m, \frac{7}{4}, \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] - \right. \\
 & \quad 2 \left(4 m \text{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2 m, 1 + 2 m, \frac{11}{4}, \right. \right. \\
 & \quad \quad \left. \left. \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] + \right. \\
 & \quad \quad \left. (-3 + 4 m) \text{AppellF1} \left[\frac{7}{4}, \frac{5}{2} - 2 m, 2 m, \frac{11}{4}, \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right)^2 - \\
 & \left. \left(33 \text{AppellF1} \left[\frac{7}{4}, \frac{3}{2} - 2 m, 2 m, \frac{11}{4}, \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \right. \\
 & \quad \left. \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^4 \left(-4 m \text{AppellF1} \left[\frac{11}{4}, \frac{3}{2} - 2 m, 1 + 2 m, \frac{15}{4}, \right. \right. \right. \\
 & \quad \quad \left. \left. \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] + (-3 + 4 m) \text{AppellF1} \left[\right. \right. \\
 & \quad \quad \left. \left. \frac{11}{4}, \frac{5}{2} - 2 m, 2 m, \frac{15}{4}, \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \right) \\
 & \quad \text{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right] + 11 \left(-\frac{7}{11} m \text{AppellF1} \left[\right. \right. \\
 & \quad \quad \left. \left. \frac{11}{4}, \frac{3}{2} - 2 m, 1 + 2 m, \frac{15}{4}, \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \\
 & \quad \text{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right] + \frac{7}{22} \left(\frac{3}{2} - 2 m \right) \text{AppellF1} \left[\right. \\
 & \quad \quad \left. \frac{11}{4}, \frac{5}{2} - 2 m, 2 m, \frac{15}{4}, \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \\
 & \quad \text{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right] - 2 \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \\
 & \left. \left(4 m \left(-\frac{11}{30} (1 + 2 m) \text{AppellF1} \left[\frac{15}{4}, \frac{3}{2} - 2 m, 2 + 2 m, \frac{19}{4}, \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right. \right. \\
 & \quad \left. \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right] + \frac{11}{30} \left(\frac{3}{2} - 2 m \right) \text{AppellF1} \left[\frac{15}{4}, \frac{5}{2} - 2 m, \right. \right. \\
 & \quad \quad \left. \left. 1 + 2 m, \frac{19}{4}, \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, -\text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \right) \\
 & \quad \text{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right] + (-3 + 4 m) \\
 & \quad \left. \left(-\frac{11}{15} m \text{AppellF1} \left[\frac{15}{4}, \frac{5}{2} - 2 m, 1 + 2 m, \frac{19}{4}, \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right] \text{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right]^2 \right. \\
 & \quad \left. \text{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - d x \right) \right] + \frac{11}{30} \left(\frac{5}{2} - 2 m \right) \text{AppellF1} \left[\frac{15}{4}, \frac{7}{2} - 2 m, \right. \right. \\
 \end{aligned}$$

$$\begin{aligned}
 & -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big/ \\
 & \left(\text{AppellF1}\left[-\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & \quad 2 \left(4m \text{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-5 + 4m) \text{AppellF1}\left[\frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) + \\
 & \left(11700 \text{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \Big/ \\
 & \left(5 \text{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & \quad 2 \left(4m \text{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-5 + 4m) \text{AppellF1}\left[\frac{5}{4}, \frac{7}{2} - 2m, 2m, \frac{9}{4}, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) + \\
 & \left(6318 \text{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \\
 & \quad \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big/ \\
 & \left(9 \text{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & \quad 2 \left(4m \text{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-5 + 4m) \text{AppellF1}\left[\frac{9}{4}, \frac{7}{2} - 2m, 2m, \frac{13}{4}, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) + \\
 & \left(3380 \text{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \\
 & \quad \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^4 \Big) \Big/ \\
 & \left(13 \text{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & \quad 2 \left(4m \text{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-5 + 4m) \text{AppellF1}\left[\frac{13}{4}, \frac{7}{2} - 2m, 2m, \frac{17}{4}, \right. \right. \\
 & \quad \quad \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) + \\
 & \left(765 \text{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \begin{aligned}
 & \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^6 \Big/ \\
 & \left(17 \text{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & 2\left(4m \text{AppellF1}\left[\frac{17}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{21}{4}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-5 + 4m) \text{AppellF1}\left[\frac{17}{4}, \frac{7}{2} - 2m, 2m, \frac{21}{4}, \right. \right. \\
 & \quad \left. \left. \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \Big/
 \end{aligned} \right) \\
 & \left(2340 d \left(e \text{Cos}[c + dx]\right)^{5/2} \left(-\frac{1}{4680} (-1 + 2m) \text{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right. \right. \\
 & \quad \left. \left. \left(1 - \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^{-3+2m} \left(\frac{1}{1 + \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2}\right)^{2m} \right. \right. \\
 & \quad \left. \sqrt{\frac{\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^3}{\left(1 + \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2}} \right. \\
 & \quad \left. - \left(\left(195 \text{AppellF1}\left[-\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \text{Cot}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \Big/ \left(\text{AppellF1}\left[-\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 2\left(4m \text{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{5}{4}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \right. \right. \\
 & \quad \left. \left. \left. (-5 + 4m) \text{AppellF1}\left[\frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \right) + \left(11700 \text{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \Big/ \\
 & \quad \left(5 \text{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & \quad \left. 2\left(4m \text{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{9}{4}, \text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
 & \quad \left. \left. -\text{Tan}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + (-5 + 4m) \text{AppellF1}\left[\frac{5}{4}, \frac{7}{2} - 2m, \right. \right.
 \end{aligned}
 \right)
 \end{aligned}$$

$$\begin{aligned}
 & 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) \\
 & \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) + \left(6318 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 2m, \frac{9}{4}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) / \\
 & \left(9 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] - \right. \\
 & \left. 2 \left(4m \operatorname{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + (-5 + 4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{7}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
 & \left(3380 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^4 \right) / \\
 & \left(13 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] - 2 \left(4m \operatorname{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{17}{4}, \right. \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + (-5 + 4m) \operatorname{AppellF1}\left[\right. \right. \\
 & \left. \left. \frac{13}{4}, \frac{7}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \right) \\
 & \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \Big) + \left(765 \operatorname{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^6 \right) / \\
 & \left(17 \operatorname{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] - 2 \left(4m \operatorname{AppellF1}\left[\frac{17}{4}, \frac{5}{2} - 2m, 1 + 2m, \right. \right. \right. \\
 & \left. \left. \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] + \right. \\
 & \left. (-5 + 4m) \operatorname{AppellF1}\left[\frac{17}{4}, \frac{7}{2} - 2m, 2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) \Big) - \\
 & \frac{1}{4680} (-3 + 2m) \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \\
 & \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^{-4+2m}
 \end{aligned}$$

$$\begin{aligned}
 & \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2} \right)^{-1+2m} \\
 & \sqrt{\frac{\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^3}{\left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2}} \\
 & - \left(\left(195 \operatorname{AppellF1}\left[-\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right], \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) / \left(\operatorname{AppellF1}\left[-\frac{3}{4}, \frac{5}{2} - 2m, \right. \right. \\
 & \quad \left. \left. 2m, \frac{1}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 2 \left(4m \operatorname{AppellF1}\left[\frac{1}{4}, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} - 2m, 1 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (-5 + 4m) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \left(11700 \operatorname{AppellF1}\left[\right. \right. \\
 & \quad \left. \left. \frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) / \\
 & \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & \quad \left. 2 \left(4m \operatorname{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-5 + 4m) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{7}{2} - 2m, 2m, \frac{9}{4}, \tan\left[\right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
 & \left(6318 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) / \\
 & \left(9 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - \right. \\
 & \quad \left. 2 \left(4m \operatorname{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-5 + 4m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{7}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\right. \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) + \\
 & \left(3380 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^4 \right) / \left(13 \operatorname{AppellF1}\left[\frac{9}{4}, \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \frac{5}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2] - \\
 & 2\left(4m \operatorname{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-5 + 4m) \operatorname{AppellF1}\left[\frac{13}{4}, \frac{7}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + \\
 & \left(765 \operatorname{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^6\right) / \\
 & \left(17 \operatorname{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 2\left(4m \operatorname{AppellF1}\left[\frac{17}{4}, \frac{5}{2} - 2m, 1 + 2m, \right. \right. \\
 & \quad \left. \left. \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
 & \quad \left. (-5 + 4m) \operatorname{AppellF1}\left[\frac{17}{4}, \frac{7}{2} - 2m, 2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + \\
 & \frac{1}{4680 \sqrt{\frac{\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^3}{\left(1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2}} \left(1 - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^{-3+2m} \\
 & \left(\frac{1}{1 + \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2}\right)^{-1+2m} \\
 & \left(-\left(\left(195 \operatorname{AppellF1}\left[-\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \cot\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) / \left(\operatorname{AppellF1}\left[-\frac{3}{4}, \frac{5}{2} - 2m, \right. \right. \right. \\
 & \quad \left. \left. 2m, \frac{1}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 2\left(4m \operatorname{AppellF1}\left[\frac{1}{4}, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} - 2m, 1 + 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
 & \quad \left. (-5 + 4m) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, \right. \\
 & \quad \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) + \left(11700 \operatorname{AppellF1}\left[\right. \right. \\
 & \quad \left. \left. \frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) / \\
 & \left(5 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] -
 \end{aligned}$$

$$\begin{aligned}
 & \left(\left(\frac{1}{4} \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 - \frac{3}{4} \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) / \right. \\
 & \quad \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2 - \\
 & \quad \left(\operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \left(\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^3 \right) \right) \right) / \left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^3 + \\
 & \frac{1}{2340} \left(1 - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^{-3+2m} \left(\frac{1}{1 + \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2} \right)^{-1+2m} \\
 & \sqrt{\frac{\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^3}{\left(1 + \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right)^2}} \\
 & \left(\left(195 \operatorname{AppellF1} \left[-\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \right. \\
 & \quad \left. \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \operatorname{Csc} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) / \\
 & \left(2 \left(\operatorname{AppellF1} \left[-\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - 2 \left(4m \operatorname{AppellF1} \left[\frac{1}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{5}{4}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-5 + 4m) \operatorname{AppellF1} \left[\right. \right. \\
 & \quad \left. \left. \frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \right) \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) \right) - \left(195 \operatorname{Cot} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right. \\
 & \quad \left(3m \operatorname{AppellF1} \left[\frac{1}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{5}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] - \right. \\
 & \quad \left. \frac{3}{2} \left(\frac{5}{2} - 2m \right) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \right) \right) \right) / \\
 & \left(\operatorname{AppellF1} \left[-\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
 & \quad \left. 2 \left(4m \operatorname{AppellF1} \left[\frac{1}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{5}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-5 + 4m) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \operatorname{Tan} \left[\right. \right. \right. \\
 & \quad \left. \left. \frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right) +
 \end{aligned}$$

$$\begin{aligned}
& -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)+ \\
& \left(765\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^6\left(-\frac{13}{17}m\operatorname{AppellF1}\left[\frac{17}{4},\frac{5}{2}-2m,1+2m,\frac{21}{4},\right.\right.\right. \\
& \quad \left.\left.\left.\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right.\right. \\
& \quad \left.\left.\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)+\right. \\
& \quad \left.\frac{13}{34}\left(\frac{5}{2}-2m\right)\operatorname{AppellF1}\left[\frac{17}{4},\frac{7}{2}-2m,2m,\frac{21}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right. \\
& \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)\right)/ \\
& \left(17\operatorname{AppellF1}\left[\frac{13}{4},\frac{5}{2}-2m,2m,\frac{17}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right. \\
& \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]-2\left(4m\operatorname{AppellF1}\left[\frac{17}{4},\frac{5}{2}-2m,1+2m,\right.\right. \\
& \quad \left.\left.\frac{21}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+ \right. \\
& \quad \left.(-5+4m)\operatorname{AppellF1}\left[\frac{17}{4},\frac{7}{2}-2m,2m,\frac{21}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right. \\
& \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\right)\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)+ \\
& \left(195\operatorname{AppellF1}\left[-\frac{3}{4},\frac{5}{2}-2m,2m,\frac{1}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right. \\
& \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\operatorname{Cot}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \\
& \quad \left(3m\operatorname{AppellF1}\left[\frac{1}{4},\frac{5}{2}-2m,1+2m,\frac{5}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right. \\
& \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]- \\
& \quad \frac{3}{2}\left(\frac{5}{2}-2m\right)\operatorname{AppellF1}\left[\frac{1}{4},\frac{7}{2}-2m,2m,\frac{5}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right. \\
& \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]- \\
& \quad \left(4m\operatorname{AppellF1}\left[\frac{1}{4},\frac{5}{2}-2m,1+2m,\frac{5}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right. \\
& \quad \left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+(-5+4m)\operatorname{AppellF1}\left[\frac{1}{4},\frac{7}{2}-2m,\right. \\
& \quad \left.2m,\frac{5}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)\right) \\
& \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]-2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \\
& \left(4m\left(-\frac{1}{10}(1+2m)\operatorname{AppellF1}\left[\frac{5}{4},\frac{5}{2}-2m,2+2m,\frac{9}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,\right.\right. \right. \\
& \quad \left.\left.-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)
\end{aligned}$$

$$\begin{aligned}
 & \left(\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{1}{10}\left(\frac{5}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{7}{2} - 2m, \right. \right. \\
 & \quad \left. \left. 1 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + (-5 + 4m) \right. \\
 & \quad \left. \left(-\frac{1}{5}m \operatorname{AppellF1}\left[\frac{5}{4}, \frac{7}{2} - 2m, 1 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \right. \\
 & \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{1}{10}\left(\frac{7}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{9}{2} - 2m, \right. \right. \\
 & \quad \left. \left. 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] \right) \right) \Big/ \\
 & \left(\operatorname{AppellF1}\left[-\frac{3}{4}, \frac{5}{2} - 2m, 2m, \frac{1}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 2\left(4m \operatorname{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 1 + 2m, \right. \right. \right. \\
 & \quad \quad \left. \left. \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \right. \\
 & \quad \left. \left. (-5 + 4m) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{7}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right) - \right. \\
 & \quad \left. \left(11700 \operatorname{AppellF1}\left[\frac{1}{4}, \frac{5}{2} - 2m, 2m, \frac{5}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \\
 & \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \left(-\left(4m \operatorname{AppellF1}\left[\frac{5}{4}, \frac{5}{2} - 2m, 1 + 2m, \frac{9}{4}, \right. \right. \right. \right. \\
 & \quad \quad \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-5 + 4m) \operatorname{AppellF1}\left[\right. \right. \\
 & \quad \quad \left. \left. \frac{5}{4}, \frac{7}{2} - 2m, 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + 5\left(-\frac{1}{5}m \operatorname{AppellF1}\left[\frac{5}{4}, \right. \right. \\
 & \quad \left. \frac{5}{2} - 2m, 1 + 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{1}{10}\left(\frac{5}{2} - 2m\right) \operatorname{AppellF1}\left[\right. \\
 & \quad \left. \frac{5}{4}, \frac{7}{2} - 2m, 2m, \frac{9}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \\
 & \quad \operatorname{Sec}\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - 2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
 & \quad \left. \left(4m\left(-\frac{5}{18}(1 + 2m) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 2 + 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, \right. \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \\
 & \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]+\frac{5}{18}\left(\frac{5}{2}-2m\right)\operatorname{AppellF1}\left[\frac{9}{4},\frac{7}{2}-2m, \right. \\
 & \left. 1+2m,\frac{13}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \\
 & \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]+(-5+4m) \\
 & \left(-\frac{5}{9}m\operatorname{AppellF1}\left[\frac{9}{4},\frac{7}{2}-2m,1+2m,\frac{13}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]+\frac{5}{18}\left(\frac{7}{2}-2m\right)\operatorname{AppellF1}\left[\frac{9}{4},\frac{9}{2}-2m, \right. \right. \\
 & \left. \left. 2m,\frac{13}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]\right)\right) \\
 & \left(5\operatorname{AppellF1}\left[\frac{1}{4},\frac{5}{2}-2m,2m,\frac{5}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]- \right. \\
 & \left. 2\left(4m\operatorname{AppellF1}\left[\frac{5}{4},\frac{5}{2}-2m,1+2m,\frac{9}{4}, \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+ \right. \\
 & \left. (-5+4m)\operatorname{AppellF1}\left[\frac{5}{4},\frac{7}{2}-2m,2m,\frac{9}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2, \right. \right. \\
 & \left. \left. -\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right)- \right. \\
 & \left. (6318\operatorname{AppellF1}\left[\frac{5}{4},\frac{5}{2}-2m,2m,\frac{9}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \\
 & \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\left(-\left(4m\operatorname{AppellF1}\left[\frac{9}{4},\frac{5}{2}-2m,1+2m,\frac{13}{4}, \right. \right. \right. \right. \\
 & \left. \left. \operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]+(-5+4m)\operatorname{AppellF1}\left[\right. \right. \\
 & \left. \left. \frac{9}{4},\frac{7}{2}-2m,2m,\frac{13}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right]\right) \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]+9\left(-\frac{5}{9}m\operatorname{AppellF1}\left[\frac{9}{4}, \right. \right. \right. \\
 & \left. \left. \frac{5}{2}-2m,1+2m,\frac{13}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]+\frac{5}{18}\left(\frac{5}{2}-2m\right)\operatorname{AppellF1}\left[\right. \right. \\
 & \left. \left. \frac{9}{4},\frac{7}{2}-2m,2m,\frac{13}{4},\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2,-\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\right] \right. \\
 & \left. \operatorname{Sec}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]-2\operatorname{Tan}\left[\frac{1}{4}\left(-c+\frac{\pi}{2}-dx\right)\right]^2 \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(4m \left(-\frac{9}{26} (1+2m) \operatorname{AppellF1} \left[\frac{13}{4}, \frac{5}{2} - 2m, 2+2m, \frac{17}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right. \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] + \frac{9}{26} \left(\frac{5}{2} - 2m \right) \operatorname{AppellF1} \left[\frac{13}{4}, \frac{7}{2} - 2m, \right. \right. \\
 & \quad \left. \left. 1+2m, \frac{17}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \right) + (-5+4m) \\
 & \left(-\frac{9}{13} m \operatorname{AppellF1} \left[\frac{13}{4}, \frac{7}{2} - 2m, 1+2m, \frac{17}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right. \\
 & \quad \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] + \frac{9}{26} \left(\frac{7}{2} - 2m \right) \operatorname{AppellF1} \left[\frac{13}{4}, \frac{9}{2} - 2m, \right. \right. \\
 & \quad \left. \left. 2m, \frac{17}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] \right) \right) \Big/ \\
 & \left(9 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{5}{2} - 2m, 2m, \frac{9}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] - \right. \\
 & \quad \left. 2 \left(4m \operatorname{AppellF1} \left[\frac{9}{4}, \frac{5}{2} - 2m, 1+2m, \frac{13}{4}, \right. \right. \right. \\
 & \quad \left. \left. \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + \right. \\
 & \quad \left. (-5+4m) \operatorname{AppellF1} \left[\frac{9}{4}, \frac{7}{2} - 2m, 2m, \frac{13}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 - \right. \\
 & \left. \left(3380 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^4 \right. \\
 & \quad \left. \left(- \left(4m \operatorname{AppellF1} \left[\frac{13}{4}, \frac{5}{2} - 2m, 1+2m, \frac{17}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. - \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] + (-5+4m) \operatorname{AppellF1} \left[\frac{13}{4}, \frac{7}{2} - 2m, \right. \right. \\
 & \quad \left. \left. 2m, \frac{17}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right) \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] + 13 \left(-\frac{9}{13} m \operatorname{AppellF1} \left[\frac{13}{4}, \right. \right. \right. \\
 & \quad \left. \left. \frac{5}{2} - 2m, 1+2m, \frac{17}{4}, \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2, -\operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right]^2 \operatorname{Tan} \left[\frac{1}{4} \left(-c + \frac{\pi}{2} - dx \right) \right] + \frac{9}{26} \left(\frac{5}{2} - 2m \right) \operatorname{AppellF1} \left[\right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \frac{13}{4}, \frac{7}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
& \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - 2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
& \left(4m \left(-\frac{13}{34}(1+2m) \operatorname{AppellF1}\left[\frac{17}{4}, \frac{5}{2} - 2m, 2+2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \right. \\
& \quad \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{13}{34}\left(\frac{5}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{17}{4}, \frac{7}{2} - 2m, \right. \\
& \quad \left. 1+2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \\
& \quad \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + (-5+4m) \right. \\
& \quad \left. \left(-\frac{13}{17}m \operatorname{AppellF1}\left[\frac{17}{4}, \frac{7}{2} - 2m, 1+2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \right. \\
& \quad \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{13}{34}\left(\frac{7}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{17}{4}, \frac{9}{2} - 2m, \right. \\
& \quad \left. 2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \\
& \quad \left. \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)\right) \Bigg/ \\
& \left(13 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{5}{2} - 2m, 2m, \frac{13}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, \right. \\
& \quad \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] - 2 \left(4m \operatorname{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 1+2m, \right. \right. \\
& \quad \left. \left. \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \\
& \quad \left. (-5+4m) \operatorname{AppellF1}\left[\frac{13}{4}, \frac{7}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right)^2 - \\
& \left(765 \operatorname{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, \right. \\
& \quad \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^6 \\
& \quad \left(-\left(4m \operatorname{AppellF1}\left[\frac{17}{4}, \frac{5}{2} - 2m, 1+2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right]^2, \right. \right. \\
& \quad \left. \left. -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + (-5+4m) \operatorname{AppellF1}\left[\frac{17}{4}, \frac{7}{2} - 2m, \right. \right. \\
& \quad \left. \left. 2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right) \\
& \quad \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + 17 \left(-\frac{13}{17}m \operatorname{AppellF1}\left[\frac{17}{4}, \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & \frac{5}{2} - 2m, 1 + 2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
 & \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{13}{34}\left(\frac{5}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{17}{4}, \frac{7}{2} - 2m, 2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \\
 & \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] - 2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \\
 & \left(4m\left(-\frac{17}{42}(1+2m) \operatorname{AppellF1}\left[\frac{21}{4}, \frac{5}{2} - 2m, 2+2m, \frac{25}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \\
 & \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{17}{42}\left(\frac{5}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{21}{4}, \frac{7}{2} - 2m, 1+2m, \frac{25}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
 & \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + (-5+4m) \left(-\frac{17}{21}m \operatorname{AppellF1}\left[\frac{21}{4}, \frac{7}{2} - 2m, 1+2m, \frac{25}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \right. \right. \\
 & \left. \left. \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right] + \frac{17}{42}\left(\frac{7}{2} - 2m\right) \operatorname{AppellF1}\left[\frac{21}{4}, \frac{9}{2} - 2m, 2m, \frac{25}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \right. \\
 & \left. \left. \sec\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]\right)\right) \Bigg/ \\
 & \left(17 \operatorname{AppellF1}\left[\frac{13}{4}, \frac{5}{2} - 2m, 2m, \frac{17}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \\
 & \left. - 2 \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2 - 2\left(4m \operatorname{AppellF1}\left[\frac{17}{4}, \frac{5}{2} - 2m, 1+2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] + \right. \right. \\
 & \left. \left. (-5+4m) \operatorname{AppellF1}\left[\frac{17}{4}, \frac{7}{2} - 2m, 2m, \frac{21}{4}, \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2, -\tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right] \right. \right. \\
 & \left. \left. - \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \tan\left[\frac{1}{4}\left(-c + \frac{\pi}{2} - dx\right)\right]^2\right) \Bigg) \Bigg) \Bigg) \Bigg) \Bigg)
 \end{aligned}$$

Problem 371: Result more than twice size of optimal antiderivative.

$$\int (e \cos [c + d x])^{-3-2m} (a + a \sin [c + d x])^m dx$$

Optimal (type 5, 70 leaves, 3 steps):

$$\frac{1}{4 a d e (1+m)}$$

$$(e \cos [c + d x])^{-2(1+m)} \text{Hypergeometric2F1}\left[2, -1-m, -m, \frac{1}{2}(1 - \sin [c + d x])\right] (a + a \sin [c + d x])^{1+m}$$

Result (type 5, 206 leaves):

$$\frac{1}{8 d e^3 m (-1+m^2)} (e \cos [c + d x])^{-2m} \left(\sec \left[\frac{1}{4} (2c - \pi + 2dx) \right]^2 \right)^{-m} (a (1 + \sin [c + d x]))^m$$

$$\left(2(-1+m^2) \text{Hypergeometric2F1}\left[-m, -m, 1-m, -\tan \left[\frac{1}{4} (2c - \pi + 2dx) \right]^2 \right] + \right.$$

$$\left. (-1+m) m \csc \left[\frac{1}{4} (2c - \pi + 2dx) \right]^2 \left(\sec \left[\frac{1}{4} (2c - \pi + 2dx) \right]^2 \right)^m + m(1+m) \right.$$

$$\left. \text{Hypergeometric2F1}\left[1-m, -m, 2-m, -\tan \left[\frac{1}{4} (2c - \pi + 2dx) \right]^2 \right] \tan \left[\frac{1}{4} (2c - \pi + 2dx) \right]^2 \right)$$

Problem 372: Result more than twice size of optimal antiderivative.

$$\int (e \cos [c + d x])^{4-2m} (a + a \sin [c + d x])^m dx$$

Optimal (type 5, 89 leaves, 4 steps):

$$\frac{1}{5 d e} 2^{\frac{5}{2}-m} (e \cos [c + d x])^{5-2m} \text{Hypergeometric2F1}\left[\frac{5}{2}, \frac{1}{2}(-3+2m), \frac{7}{2}, \frac{1}{2}(1 + \sin [c + d x])\right]$$

$$(1 - \sin [c + d x])^{-\frac{5}{2}-m} (a + a \sin [c + d x])^m$$

Result (type 5, 200 leaves):

$$-\frac{1}{d(-1+2m)}$$

$$32 e^4 (e \cos [c + d x])^{-2m} \left(\text{Hypergeometric2F1}\left[\frac{1}{2}-m, 3-m, \frac{3}{2}-m, -\tan \left[\frac{1}{4} (2c - \pi + 2dx) \right]^2 \right] - \right.$$

$$2 \text{Hypergeometric2F1}\left[\frac{1}{2}-m, 4-m, \frac{3}{2}-m, -\tan \left[\frac{1}{4} (2c - \pi + 2dx) \right]^2 \right] +$$

$$\left. \text{Hypergeometric2F1}\left[\frac{1}{2}-m, 5-m, \frac{3}{2}-m, -\tan \left[\frac{1}{4} (2c - \pi + 2dx) \right]^2 \right] \right)$$

$$\left(\sec \left[\frac{1}{4} (2c - \pi + 2dx) \right]^2 \right)^{-m} (a (1 + \sin [c + d x]))^m \tan \left[\frac{1}{4} (2c - \pi + 2dx) \right]$$

Problem 375: Result more than twice size of optimal antiderivative.

$$\int (e \cos [c + d x])^{-2-2m} (a + a \sin [c + d x])^m dx$$

Optimal (type 5, 87 leaves, 4 steps):

$$-\frac{1}{d e} 2^{-\frac{1}{2}-m} (e \cos [c+d x])^{-1-2 m} \text{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{1}{2}(3+2 m), \frac{1}{2}, \frac{1}{2}(1+\sin [c+d x])\right] \\ (1-\sin [c+d x])^{\frac{1}{2}+m} (a+a \sin [c+d x])^m$$

Result (type 5, 186 leaves):

$$\frac{1}{2 d e^2 (-1+4 m^2)} (e \cos [c+d x])^{-2 m} \cot \left[\frac{1}{4}(2 c+\pi+2 d x)\right] \left((-1+2 m) \cot \left[\frac{1}{4}(2 c-\pi+2 d x)\right]^2 \text{Hypergeometric2F1}\left[-\frac{1}{2}-m, -m, \frac{1}{2}-m, -\tan \left[\frac{1}{4}(2 c-\pi+2 d x)\right]^2\right] + (1+2 m) \text{Hypergeometric2F1}\left[\frac{1}{2}-m, -m, \frac{3}{2}-m, -\tan \left[\frac{1}{4}(2 c-\pi+2 d x)\right]^2\right]\right) \left(\sec \left[\frac{1}{4}(2 c-\pi+2 d x)\right]^2\right)^{-m} (a(1+\sin [c+d x]))^m$$

Problem 380: Result more than twice size of optimal antiderivative.

$$\int \sec [c+d x]^3 (a+b \sin [c+d x]) dx$$

Optimal (type 3, 41 leaves, 3 steps):

$$\frac{a \operatorname{ArcTanh}[\sin [c+d x]]}{2 d} + \frac{\sec [c+d x]^2 (b+a \sin [c+d x])}{2 d}$$

Result (type 3, 83 leaves):

$$\frac{1}{2 d} \left(a \left(-\log \left[\cos \left[\frac{1}{2}(c+d x) \right] - \sin \left[\frac{1}{2}(c+d x) \right] \right] + \log \left[\cos \left[\frac{1}{2}(c+d x) \right] + \sin \left[\frac{1}{2}(c+d x) \right] \right] \right) + b \sec [c+d x]^2 + a \sec [c+d x] \tan [c+d x] \right)$$

Problem 381: Result more than twice size of optimal antiderivative.

$$\int \sec [c+d x]^5 (a+b \sin [c+d x]) dx$$

Optimal (type 3, 61 leaves, 4 steps):

$$\frac{3 a \operatorname{ArcTanh}[\sin [c+d x]]}{8 d} + \frac{\sec [c+d x]^4 (b+a \sin [c+d x])}{4 d} + \frac{3 a \sec [c+d x] \tan [c+d x]}{8 d}$$

Result (type 3, 207 leaves):

$$\begin{aligned}
& - \frac{3 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \\
& \frac{3 a \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right]}{8 d} + \frac{b \operatorname{Sec}[c+d x]^4}{4 d} + \\
& \frac{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4}{a} + \frac{3 a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} - \\
& \frac{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^4}{a} - \frac{3 a}{16 d\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2}
\end{aligned}$$

Problem 389: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c+d x](a+b \operatorname{Sin}[c+d x])^2 dx$$

Optimal (type 3, 22 leaves, 2 steps):

$$\frac{(a+b \operatorname{Sin}[c+d x])^3}{3 b d}$$

Result (type 3, 46 leaves):

$$\frac{a^2 \operatorname{Sin}[c+d x]}{d} + \frac{a b \operatorname{Sin}[c+d x]^2}{d} + \frac{b^2 \operatorname{Sin}[c+d x]^3}{3 d}$$

Problem 391: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Sec}[c+d x]^3(a+b \operatorname{Sin}[c+d x])^2 dx$$

Optimal (type 3, 59 leaves, 3 steps):

$$\frac{(a^2-b^2) \operatorname{ArcTanh}[\operatorname{Sin}[c+d x]]}{2 d} + \frac{\operatorname{Sec}[c+d x]^2(b+a \operatorname{Sin}[c+d x])(a+b \operatorname{Sin}[c+d x])}{2 d}$$

Result (type 3, 139 leaves):

$$\begin{aligned}
& \frac{1}{4 d} \left(2(-a^2+b^2) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] + \right. \\
& 2(a^2-b^2) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right] + \\
& \left. \frac{(a+b)^2}{\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]-\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} - \frac{(a-b)^2}{\left(\operatorname{Cos}\left[\frac{1}{2}(c+d x)\right]+\operatorname{Sin}\left[\frac{1}{2}(c+d x)\right]\right)^2} \right)
\end{aligned}$$

Problem 392: Result more than twice size of optimal antiderivative.

$$\int \sec [c+d x]^5 (a+b \sin [c+d x])^2 d x$$

Optimal (type 3, 99 leaves, 4 steps):

$$\frac{(3 a^2 - b^2) \operatorname{ArcTanh}[\sin [c+d x]]}{8 d} + \frac{\sec [c+d x]^4 (b+a \sin [c+d x]) (a+b \sin [c+d x])}{4 d} + \frac{\sec [c+d x]^2 (2 a b + (3 a^2 - b^2) \sin [c+d x])}{8 d}$$

Result (type 3, 219 leaves):

$$\frac{1}{16 d} \left(2 (-3 a^2 + b^2) \operatorname{Log} \left[\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right] + 2 (3 a^2 - b^2) \operatorname{Log} \left[\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right] + \frac{(a+b)^2}{\left(\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right)^4} + \frac{3 a^2 + 2 a b - b^2}{\left(\cos \left[\frac{1}{2} (c+d x) \right] - \sin \left[\frac{1}{2} (c+d x) \right] \right)^2} - \frac{(a-b)^2}{\left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^4} + \frac{-3 a^2 + 2 a b + b^2}{\left(\cos \left[\frac{1}{2} (c+d x) \right] + \sin \left[\frac{1}{2} (c+d x) \right] \right)^2} \right)$$

Problem 402: Result more than twice size of optimal antiderivative.

$$\int \cos [c+d x] (a+b \sin [c+d x])^3 d x$$

Optimal (type 3, 22 leaves, 2 steps):

$$\frac{(a+b \sin [c+d x])^4}{4 b d}$$

Result (type 3, 67 leaves):

$$\frac{a^3 \sin [c+d x]}{d} + \frac{3 a^2 b \sin [c+d x]^2}{2 d} + \frac{a b^2 \sin [c+d x]^3}{d} + \frac{b^3 \sin [c+d x]^4}{4 d}$$

Problem 405: Result more than twice size of optimal antiderivative.

$$\int \sec [c+d x]^5 (a+b \sin [c+d x])^3 d x$$

Optimal (type 3, 94 leaves, 4 steps):

$$\frac{3 a (a^2 - b^2) \operatorname{ArcTanh}[\operatorname{Sin}[c + d x]]}{8 d} + \frac{3 a \operatorname{Sec}[c + d x]^2 (b + a \operatorname{Sin}[c + d x]) (a + b \operatorname{Sin}[c + d x])}{8 d} + \frac{\operatorname{Sec}[c + d x]^3 (a + b \operatorname{Sin}[c + d x])^3 \operatorname{Tan}[c + d x]}{4 d}$$

Result (type 3, 213 leaves):

$$\frac{1}{16 d} \left(-6 a (a^2 - b^2) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + 6 a (a^2 - b^2) \operatorname{Log}\left[\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right] + \frac{(a + b)^3}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} + \frac{3(a - b)(a + b)^2}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] - \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} - \frac{(a - b)^3}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^4} - \frac{3(a - b)^2(a + b)}{\left(\operatorname{Cos}\left[\frac{1}{2}(c + d x)\right] + \operatorname{Sin}\left[\frac{1}{2}(c + d x)\right]\right)^2} \right)$$

Problem 413: Result more than twice size of optimal antiderivative.

$$\int \operatorname{Cos}[c + d x]^5 (a + b \operatorname{Sin}[c + d x])^8 dx$$

Optimal (type 3, 144 leaves, 3 steps):

$$\frac{(a^2 - b^2)^2 (a + b \operatorname{Sin}[c + d x])^9}{9 b^5 d} - \frac{2 a (a^2 - b^2) (a + b \operatorname{Sin}[c + d x])^{10}}{5 b^5 d} + \frac{2 (3 a^2 - b^2) (a + b \operatorname{Sin}[c + d x])^{11}}{11 b^5 d} - \frac{a (a + b \operatorname{Sin}[c + d x])^{12}}{3 b^5 d} + \frac{(a + b \operatorname{Sin}[c + d x])^{13}}{13 b^5 d}$$

Result (type 3, 572 leaves):

$$\frac{1}{26357760 d} \left(-205920 (80 a^7 b + 168 a^5 b^3 + 70 a^3 b^5 + 5 a b^7) \operatorname{Cos}[2(c + d x)] - 25740 (256 a^7 b + 224 a^5 b^3 - 5 a b^7) \operatorname{Cos}[4(c + d x)] - 1098240 a^7 b \operatorname{Cos}[6(c + d x)] + 3843840 a^5 b^3 \operatorname{Cos}[6(c + d x)] + 2402400 a^3 b^5 \operatorname{Cos}[6(c + d x)] + 171600 a b^7 \operatorname{Cos}[6(c + d x)] + 1441440 a^5 b^3 \operatorname{Cos}[8(c + d x)] - 51480 a b^7 \operatorname{Cos}[8(c + d x)] - 288288 a^3 b^5 \operatorname{Cos}[10(c + d x)] - 20592 a b^7 \operatorname{Cos}[10(c + d x)] + 8580 a b^7 \operatorname{Cos}[12(c + d x)] + 16473600 a^8 \operatorname{Sin}[c + d x] + 57657600 a^6 b^2 \operatorname{Sin}[c + d x] + 43243200 a^4 b^4 \operatorname{Sin}[c + d x] + 7207200 a^2 b^6 \operatorname{Sin}[c + d x] + 128700 b^8 \operatorname{Sin}[c + d x] + 2745600 a^8 \operatorname{Sin}[3(c + d x)] - 3843840 a^6 b^2 \operatorname{Sin}[3(c + d x)] - 9609600 a^4 b^4 \operatorname{Sin}[3(c + d x)] - 2402400 a^2 b^6 \operatorname{Sin}[3(c + d x)] - 53625 b^8 \operatorname{Sin}[3(c + d x)] + 329472 a^8 \operatorname{Sin}[5(c + d x)] - 6918912 a^6 b^2 \operatorname{Sin}[5(c + d x)] - 5765760 a^4 b^4 \operatorname{Sin}[5(c + d x)] - 720720 a^2 b^6 \operatorname{Sin}[5(c + d x)] - 6435 b^8 \operatorname{Sin}[5(c + d x)] - 1647360 a^6 b^2 \operatorname{Sin}[7(c + d x)] + 1029600 a^4 b^4 \operatorname{Sin}[7(c + d x)] + 514800 a^2 b^6 \operatorname{Sin}[7(c + d x)] + 12870 b^8 \operatorname{Sin}[7(c + d x)] + 800800 a^4 b^4 \operatorname{Sin}[9(c + d x)] + 80080 a^2 b^6 \operatorname{Sin}[9(c + d x)] - 1430 b^8 \operatorname{Sin}[9(c + d x)] - 65520 a^2 b^6 \operatorname{Sin}[11(c + d x)] - 1755 b^8 \operatorname{Sin}[11(c + d x)] + 495 b^8 \operatorname{Sin}[13(c + d x)] \right)$$

Problem 414: Result more than twice size of optimal antiderivative.

$$\int \cos [c+d x]^3 (a+b \sin [c+d x])^8 d x$$

Optimal (type 3, 77 leaves, 3 steps):

$$-\frac{(a^2-b^2)(a+b \sin [c+d x])^9}{9 b^3 d} + \frac{a(a+b \sin [c+d x])^{10}}{5 b^3 d} - \frac{(a+b \sin [c+d x])^{11}}{11 b^3 d}$$

Result (type 3, 438 leaves):

$$\begin{aligned} & \frac{1}{506880 d} (-7920 (64 a^7 b + 168 a^5 b^3 + 84 a^3 b^5 + 7 a b^7) \cos [2(c+d x)] - \\ & 15840 (8 a^7 b - 7 a^3 b^5 - a b^7) \cos [4(c+d x)] + 147840 a^5 b^3 \cos [6(c+d x)] + \\ & 73920 a^3 b^5 \cos [6(c+d x)] + 3960 a b^7 \cos [6(c+d x)] - 27720 a^3 b^5 \cos [8(c+d x)] - \\ & 3960 a b^7 \cos [8(c+d x)] + 792 a b^7 \cos [10(c+d x)] + 380160 a^8 \sin [c+d x] + \\ & 1774080 a^6 b^2 \sin [c+d x] + 1663200 a^4 b^4 \sin [c+d x] + 332640 a^2 b^6 \sin [c+d x] + \\ & 6930 b^8 \sin [c+d x] + 42240 a^8 \sin [3(c+d x)] - 295680 a^6 b^2 \sin [3(c+d x)] - \\ & 554400 a^4 b^4 \sin [3(c+d x)] - 147840 a^2 b^6 \sin [3(c+d x)] - 3630 b^8 \sin [3(c+d x)] - \\ & 177408 a^6 b^2 \sin [5(c+d x)] - 110880 a^4 b^4 \sin [5(c+d x)] + 495 b^8 \sin [5(c+d x)] + \\ & 79200 a^4 b^4 \sin [7(c+d x)] + 23760 a^2 b^6 \sin [7(c+d x)] + 495 b^8 \sin [7(c+d x)] - \\ & 6160 a^2 b^6 \sin [9(c+d x)] - 275 b^8 \sin [9(c+d x)] + 45 b^8 \sin [11(c+d x)] \end{aligned}$$

Problem 465: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\sec [c+d x]}{(a+b \sin [c+d x])^8} d x$$

Optimal (type 3, 385 leaves, 4 steps):

$$\begin{aligned} & -\frac{\log [1-\sin [c+d x]]}{2(a+b)^8 d} + \frac{\log [1+\sin [c+d x]]}{2(a-b)^8 d} - \\ & \frac{8 a b\left(a^2+b^2\right)\left(a^4+6 a^2 b^2+b^4\right) \log [a+b \sin [c+d x]]}{\left(a^2-b^2\right)^8 d} + \frac{b}{7\left(a^2-b^2\right) d(a+b \sin [c+d x])^7} + \\ & \frac{a b}{3\left(a^2-b^2\right)^2 d(a+b \sin [c+d x])^6} + \frac{b\left(3 a^2+b^2\right)}{5\left(a^2-b^2\right)^3 d(a+b \sin [c+d x])^5} + \\ & \frac{a b\left(a^2+b^2\right)}{\left(a^2-b^2\right)^4 d(a+b \sin [c+d x])^4} + \frac{b\left(5 a^4+10 a^2 b^2+b^4\right)}{3\left(a^2-b^2\right)^5 d(a+b \sin [c+d x])^3} + \\ & \frac{a b\left(3 a^2+b^2\right)\left(a^2+3 b^2\right)}{\left(a^2-b^2\right)^6 d(a+b \sin [c+d x])^2} + \frac{b\left(7 a^6+35 a^4 b^2+21 a^2 b^4+b^6\right)}{\left(a^2-b^2\right)^7 d(a+b \sin [c+d x])} \end{aligned}$$

Result (type 3, 847 leaves):

$$\begin{aligned}
& \frac{16 i (a^7 b + 7 a^5 b^3 + 7 a^3 b^5 + a b^7) (c + d x)}{(a - b)^8 (a + b)^8 d} + \frac{1}{(a - b)^8 d} \\
& i \operatorname{ArcTan} \left[\operatorname{Csc}[c + d x] \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right) \right. \\
& \quad \left. \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) \right] - \frac{1}{(a + b)^8 d} i \operatorname{ArcTan} \left[\right. \\
& \quad \left. \operatorname{Csc}[c + d x] \left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right) \left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right) \right] - \\
& \frac{\operatorname{Log} \left[\left(\cos \left[\frac{1}{2} (c + d x) \right] - \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 \right]}{2 (a + b)^8 d} + \frac{\operatorname{Log} \left[\left(\cos \left[\frac{1}{2} (c + d x) \right] + \sin \left[\frac{1}{2} (c + d x) \right] \right)^2 \right]}{2 (a - b)^8 d} - \\
& \frac{8 (a^7 b + 7 a^5 b^3 + 7 a^3 b^5 + a b^7) \operatorname{Log}[a + b \operatorname{Sin}[c + d x]]}{(a^2 - b^2)^8 d} + \\
& \frac{1}{3360 (a^2 - b^2)^7 d (a + b \operatorname{Sin}[c + d x])^7} \\
& (46176 a^{12} b + 368176 a^{10} b^3 + 1198292 a^8 b^5 + 1066342 a^6 b^7 + 403302 a^4 b^9 + 20066 a^2 b^{11} + 2286 b^{13} - \\
& 249648 a^{10} b^3 \operatorname{Cos}[2(c + d x)] - 1190224 a^8 b^5 \operatorname{Cos}[2(c + d x)] - 1321089 a^6 b^7 \operatorname{Cos}[2(c + d x)] - \\
& 527429 a^4 b^9 \operatorname{Cos}[2(c + d x)] - 35539 a^2 b^{11} \operatorname{Cos}[2(c + d x)] - 2471 b^{13} \operatorname{Cos}[2(c + d x)] + \\
& 51100 a^8 b^5 \operatorname{Cos}[4(c + d x)] + 239610 a^6 b^7 \operatorname{Cos}[4(c + d x)] + 137690 a^4 b^9 \operatorname{Cos}[4(c + d x)] + \\
& 14350 a^2 b^{11} \operatorname{Cos}[4(c + d x)] + 770 b^{13} \operatorname{Cos}[4(c + d x)] - 735 a^6 b^7 \operatorname{Cos}[6(c + d x)] - \\
& 3675 a^4 b^9 \operatorname{Cos}[6(c + d x)] - 2205 a^2 b^{11} \operatorname{Cos}[6(c + d x)] - 105 b^{13} \operatorname{Cos}[6(c + d x)] + \\
& 229152 a^{11} b^2 \operatorname{Sin}[c + d x] + 1230376 a^9 b^4 \operatorname{Sin}[c + d x] + 2302916 a^7 b^6 \operatorname{Sin}[c + d x] + \\
& 1297156 a^5 b^8 \operatorname{Sin}[c + d x] + 255276 a^3 b^{10} \operatorname{Sin}[c + d x] + 7364 a b^{12} \operatorname{Sin}[c + d x] - \\
& 149240 a^9 b^4 \operatorname{Sin}[3(c + d x)] - 692370 a^7 b^6 \operatorname{Sin}[3(c + d x)] - 506170 a^5 b^8 \operatorname{Sin}[3(c + d x)] - \\
& 127190 a^3 b^{10} \operatorname{Sin}[3(c + d x)] - 3430 a b^{12} \operatorname{Sin}[3(c + d x)] + 9450 a^7 b^6 \operatorname{Sin}[5(c + d x)] + \\
& 45570 a^5 b^8 \operatorname{Sin}[5(c + d x)] + 24990 a^3 b^{10} \operatorname{Sin}[5(c + d x)] + 630 a b^{12} \operatorname{Sin}[5(c + d x)])
\end{aligned}$$

Problem 466: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \frac{\operatorname{Sec}[c + d x]^3}{(a + b \operatorname{Sin}[c + d x])^8} dx$$

Optimal (type 3, 527 leaves, 4 steps):

$$\begin{aligned}
 & - \frac{(a+9b) \operatorname{Log}[1-\operatorname{Sin}[c+dx]]}{4(a+b)^9 d} + \frac{(a-9b) \operatorname{Log}[1+\operatorname{Sin}[c+dx]]}{4(a-b)^9 d} + \\
 & \frac{8ab^3(15a^6+63a^4b^2+45a^2b^4+5b^6) \operatorname{Log}[a+b \operatorname{Sin}[c+dx]]}{(a^2-b^2)^9 d} - \\
 & \frac{b(7a^2+9b^2)}{14(a^2-b^2)^2 d(a+b \operatorname{Sin}[c+dx])^7} - \frac{\operatorname{Sec}[c+dx]^2(b-a \operatorname{Sin}[c+dx])}{2(a^2-b^2) d(a+b \operatorname{Sin}[c+dx])^7} - \\
 & \frac{ab(3a^2+13b^2)}{6(a^2-b^2)^3 d(a+b \operatorname{Sin}[c+dx])^6} - \frac{b(5a^4+50a^2b^2+9b^4)}{10(a^2-b^2)^4 d(a+b \operatorname{Sin}[c+dx])^5} - \\
 & \frac{ab(a^4+20a^2b^2+11b^4)}{2(a^2-b^2)^5 d(a+b \operatorname{Sin}[c+dx])^4} - \frac{b(3a^6+115a^4b^2+129a^2b^4+9b^6)}{6(a^2-b^2)^6 d(a+b \operatorname{Sin}[c+dx])^3} - \\
 & \frac{ab(a^6+77a^4b^2+147a^2b^4+31b^6)}{2(a^2-b^2)^7 d(a+b \operatorname{Sin}[c+dx])^2} - \frac{b(a^8+196a^6b^2+574a^4b^4+244a^2b^6+9b^8)}{2(a^2-b^2)^8 d(a+b \operatorname{Sin}[c+dx])}
 \end{aligned}$$

Result (type 3, 1237 leaves):

$$\begin{aligned}
& - \frac{16 i (15 a^7 b^3 + 63 a^5 b^5 + 45 a^3 b^7 + 5 a b^9) (c + d x)}{(a - b)^9 (a + b)^9 d} + \frac{1}{2 (a - b)^9 d} \\
& i (a - 9 b) \operatorname{ArcTan}\left[\operatorname{Csc}[c + d x] \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right)\right] \\
& \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right) + \frac{1}{2 (a + b)^9 d} i (-a - 9 b) \operatorname{ArcTan}\left[\right. \\
& \left. \operatorname{Csc}[c + d x] \left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right) \left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)\right] + \\
& \frac{(-a - 9 b) \operatorname{Log}\left[\left(\cos\left[\frac{1}{2}(c + d x)\right] - \sin\left[\frac{1}{2}(c + d x)\right]\right)^2\right]}{4 (a + b)^9 d} + \\
& \frac{(a - 9 b) \operatorname{Log}\left[\left(\cos\left[\frac{1}{2}(c + d x)\right] + \sin\left[\frac{1}{2}(c + d x)\right]\right)^2\right]}{4 (a - b)^9 d} + \\
& \frac{8 (15 a^7 b^3 + 63 a^5 b^5 + 45 a^3 b^7 + 5 a b^9) \operatorname{Log}[a + b \operatorname{Sin}[c + d x]]}{(a^2 - b^2)^9 d} + \\
& \frac{1}{26880 (a^2 - b^2)^8 d (a + b \operatorname{Sin}[c + d x])^7} \\
& \operatorname{Sec}[c + d x]^2 (-60480 a^{14} b - 2155120 a^{12} b^3 - 10531096 a^{10} b^5 - 18656885 a^8 b^7 - \\
& 11704100 a^6 b^9 - 2859110 a^4 b^{11} - 153820 a^2 b^{13} - 5469 b^{15} - 47040 a^{14} b \operatorname{Cos}[2(c + d x)] - \\
& 2190400 a^{12} b^3 \operatorname{Cos}[2(c + d x)] - 3544396 a^{10} b^5 \operatorname{Cos}[2(c + d x)] + \\
& 128224 a^8 b^7 \operatorname{Cos}[2(c + d x)] + 4162744 a^6 b^9 \operatorname{Cos}[2(c + d x)] + 1322704 a^4 b^{11} \operatorname{Cos}[2(c + d x)] + \\
& 171764 a^2 b^{13} \operatorname{Cos}[2(c + d x)] - 3600 b^{15} \operatorname{Cos}[2(c + d x)] + 58800 a^{12} b^3 \operatorname{Cos}[4(c + d x)] + \\
& 6695640 a^{10} b^5 \operatorname{Cos}[4(c + d x)] + 17845324 a^8 b^7 \operatorname{Cos}[4(c + d x)] + \\
& 11544064 a^6 b^9 \operatorname{Cos}[4(c + d x)] + 2887864 a^4 b^{11} \operatorname{Cos}[4(c + d x)] + \\
& 96264 a^2 b^{13} \operatorname{Cos}[4(c + d x)] + 9324 b^{15} \operatorname{Cos}[4(c + d x)] - 8820 a^{10} b^5 \operatorname{Cos}[6(c + d x)] - \\
& 1410080 a^8 b^7 \operatorname{Cos}[6(c + d x)] - 3831800 a^6 b^9 \operatorname{Cos}[6(c + d x)] - \\
& 1515920 a^4 b^{11} \operatorname{Cos}[6(c + d x)] - 109620 a^2 b^{13} \operatorname{Cos}[6(c + d x)] - 5040 b^{15} \operatorname{Cos}[6(c + d x)] + \\
& 105 a^8 b^7 \operatorname{Cos}[8(c + d x)] + 20580 a^6 b^9 \operatorname{Cos}[8(c + d x)] + 60270 a^4 b^{11} \operatorname{Cos}[8(c + d x)] + \\
& 25620 a^2 b^{13} \operatorname{Cos}[8(c + d x)] + 945 b^{15} \operatorname{Cos}[8(c + d x)] + 13440 a^{15} \operatorname{Sin}[c + d x] - \\
& 164640 a^{13} b^2 \operatorname{Sin}[c + d x] - 5702480 a^{11} b^4 \operatorname{Sin}[c + d x] - 20202406 a^9 b^6 \operatorname{Sin}[c + d x] - \\
& 24081736 a^7 b^8 \operatorname{Sin}[c + d x] - 9935716 a^5 b^{10} \operatorname{Sin}[c + d x] - 1391096 a^3 b^{12} \operatorname{Sin}[c + d x] - \\
& 36806 a b^{14} \operatorname{Sin}[c + d x] - 70560 a^{13} b^2 \operatorname{Sin}[3(c + d x)] - 5955320 a^{11} b^4 \operatorname{Sin}[3(c + d x)] - \\
& 15658566 a^9 b^6 \operatorname{Sin}[3(c + d x)] - 13417656 a^7 b^8 \operatorname{Sin}[3(c + d x)] - \\
& 3705156 a^5 b^{10} \operatorname{Sin}[3(c + d x)] - 326816 a^3 b^{12} \operatorname{Sin}[3(c + d x)] - 3206 a b^{14} \operatorname{Sin}[3(c + d x)] + \\
& 29400 a^{11} b^4 \operatorname{Sin}[5(c + d x)] + 4071970 a^9 b^6 \operatorname{Sin}[5(c + d x)] + 10871560 a^7 b^8 \operatorname{Sin}[5(c + d x)] + \\
& 5210380 a^5 b^{10} \operatorname{Sin}[5(c + d x)] + 875280 a^3 b^{12} \operatorname{Sin}[5(c + d x)] + \\
& 15330 a b^{14} \operatorname{Sin}[5(c + d x)] - 1470 a^9 b^6 \operatorname{Sin}[7(c + d x)] - 262920 a^7 b^8 \operatorname{Sin}[7(c + d x)] - \\
& 737940 a^5 b^{10} \operatorname{Sin}[7(c + d x)] - 283080 a^3 b^{12} \operatorname{Sin}[7(c + d x)] - 4830 a b^{14} \operatorname{Sin}[7(c + d x)])
\end{aligned}$$

Problem 495: Result more than twice size of optimal antiderivative.

$$\int \cos[c + d x]^3 (a + b \operatorname{Sin}[c + d x])^{5/2} dx$$

Optimal (type 3, 83 leaves, 3 steps):

$$-\frac{2(a^2 - b^2)(a + b \sin[c + dx])^{7/2}}{7b^3 d} + \frac{4a(a + b \sin[c + dx])^{9/2}}{9b^3 d} - \frac{2(a + b \sin[c + dx])^{11/2}}{11b^3 d}$$

Result (type 3, 198 leaves):

$$\left(-2a^2(64a^4 - 780a^2b^2 - 705b^4) \sqrt{1 + \frac{b \sin[c + dx]}{a}} \left(-1 + \sqrt{1 + \frac{b \sin[c + dx]}{a}} \right) + \right. \\ \left. b(a + b \sin[c + dx]) (8ab(3a^2 - 136b^2) \cos[2(c + dx)] - 322ab^3 \cos[4(c + dx)] + \right. \\ \left. 2(32a^4 + 1698a^2b^2 + 279b^4) \sin[c + dx] + b^2(452a^2 - 81b^2) \sin[3(c + dx)] - \right. \\ \left. 63b^4 \sin[5(c + dx)]) \right) / \left(5544b^3 d \sqrt{a + b \sin[c + dx]} \right)$$

Problem 497: Result more than twice size of optimal antiderivative.

$$\int \sec[c + dx] (a + b \sin[c + dx])^{5/2} dx$$

Optimal (type 3, 117 leaves, 7 steps):

$$-\frac{(a - b)^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a + b \sin[c + dx]}}{\sqrt{a - b}}\right]}{d} + \frac{(a + b)^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{a + b \sin[c + dx]}}{\sqrt{a + b}}\right]}{d} - \\ \frac{4ab\sqrt{a + b \sin[c + dx]}}{d} - \frac{2b(a + b \sin[c + dx])^{3/2}}{3d}$$

Result (type 3, 286 leaves):

$$\frac{1}{6d} \left(\frac{(6a^3 - 18a^2b + 11ab^2 - 6b^3) \operatorname{ArcTanh}\left[\frac{\sqrt{a + b \sin[c + dx]}}{\sqrt{a - b}}\right]}{\sqrt{a - b}} + \right. \\ \left(\sqrt{-a - b} \sqrt{-a + b} (6a^3 + 18a^2b + 11ab^2 + 6b^3) \operatorname{ArcTanh}\left[\frac{\sqrt{a + b \sin[c + dx]}}{\sqrt{a + b}}\right] - \right. \\ \left. b \left(7ab\sqrt{-a + b} \sqrt{a + b} \operatorname{ArcTan}\left[\frac{\sqrt{a + b \sin[c + dx]}}{\sqrt{-a - b}}\right] + \right. \right. \\ \left. \left. \sqrt{-(a + b)^2} \left(-7ab \operatorname{ArcTan}\left[\frac{\sqrt{a + b \sin[c + dx]}}{\sqrt{-a + b}}\right] + 4\sqrt{-a + b} \right. \right. \right. \\ \left. \left. \left. \sqrt{a + b \sin[c + dx]} (7a + b \sin[c + dx]) \right) \right) \right) / \left(\sqrt{-a + b} \sqrt{-(a + b)^2} \right)$$

Problem 574: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{11/2}}{a + b \sin [c + d x]} dx$$

Optimal (type 4, 531 leaves, 15 steps):

$$\begin{aligned} & - \frac{(-a^2 + b^2)^{9/4} e^{11/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{b^{11/2} d} - \frac{(-a^2 + b^2)^{9/4} e^{11/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{b^{11/2} d} + \\ & \frac{2 e (e \cos [c + d x])^{9/2}}{9 b d} + \left(2 a (21 a^4 - 49 a^2 b^2 + 33 b^4) e^6 \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right] \right) / \\ & \left(21 b^6 d \sqrt{e \cos [c + d x]} \right) - \frac{a (a^2 - b^2)^3 e^6 \sqrt{\cos [c + d x]} \operatorname{EllipticPi}\left[\frac{-2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{b^6 (a^2 - b (b - \sqrt{-a^2 + b^2})) d \sqrt{e \cos [c + d x]}} - \\ & \frac{a (a^2 - b^2)^3 e^6 \sqrt{\cos [c + d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{b^6 (a^2 - b (b + \sqrt{-a^2 + b^2})) d \sqrt{e \cos [c + d x]}} - \\ & \frac{2 e^3 (e \cos [c + d x])^{5/2} (7 (a^2 - b^2) - 5 a b \sin [c + d x])}{35 b^3 d} + \\ & \frac{2 e^5 \sqrt{e \cos [c + d x]} (21 (a^2 - b^2)^2 - a b (7 a^2 - 12 b^2) \sin [c + d x])}{21 b^5 d} \end{aligned}$$

Result (type 6, 2235 leaves):

$$\begin{aligned} & \frac{1}{1680 b^4 d \cos [c + d x]^{11/2}} \\ & (e \cos [c + d x])^{11/2} \left(- \frac{1}{\sqrt{1 - \cos [c + d x]^2} (a + b \sin [c + d x])} - 2 (280 a^4 - 636 a^2 b^2 + 721 b^4) \right. \\ & \left. (a + b \sqrt{1 - \cos [c + d x]^2}) \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \right. \\ & \left. \left. \left. \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2}\right] \sqrt{\cos [c + d x]} \right) / \left(\sqrt{1 - \cos [c + d x]^2} \right. \right. \\ & \left. \left. \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2}\right] - 2 \right. \right. \right. \\ & \left. \left. \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \right. \right. \right. \\ & \left. \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2}\right] \right) \cos [c + d x]^2 \right) \right. \\ & \left. (a^2 + b^2 (-1 + \cos [c + d x]^2)) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \end{aligned}$$

$$\left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] + \right. \\ \left. \operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] - \right. \\ \left. \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] \right)$$

$$\sin [c+d x] + \frac{1}{\sqrt{1-\cos [c+d x]^2} (-1+2 \cos [c+d x]^2) (a+b \sin [c+d x])}$$

$$(840 a^4 - 1764 a^2 b^2 + 959 b^4) \left(a + b \sqrt{1-\cos [c+d x]^2} \right)$$

$$\cos [2(c+d x)]$$

$$\left(\frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right]}{b^{3/2} (-a^2+b^2)^{3/4}} - \right.$$

$$\left. \frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right]}{b^{3/2} (-a^2+b^2)^{3/4}} + \frac{4 \sqrt{\cos [c+d x]}}{b} + \right.$$

$$\left(10 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \sqrt{\cos [c+d x]} \right) /$$

$$\left(\sqrt{1-\cos [c+d x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \cos [c+d x]^2 \right) (a^2+b^2 (-1+\cos [c+d x]^2)) \right) -$$

$$\left(36 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right.$$

$$\left. \cos [c+d x]^{5/2} \right) / \left(5 \sqrt{1-\cos [c+d x]^2} \right)$$

$$\left(9 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] - \right.$$

$$2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right.$$

$$\left. \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \cos [c+d x]^2$$

$$(a^2+b^2 (-1+\cos [c+d x]^2)) + \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[\sqrt{-a^2+b^2} - \right. \right.$$

$$\left. \left. (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] \right) / \left(b^{3/2} (-a^2+b^2)^{3/4} \right) -$$

$$\left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2a^2 + b^2) \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\operatorname{Cos}[c + dx]} + \right. \right. \\
 \left. \left. i b \operatorname{Cos}[c + dx] \right] \right) / \left(b^{3/2} (-a^2 + b^2)^{3/4} \right) \operatorname{Sin}[c + dx] - \\
 \frac{1}{(1 - \operatorname{Cos}[c + dx]^2) (a + b \operatorname{Sin}[c + dx])} 2 (-392 a^3 b + 722 a b^3) \\
 \left(a + b \sqrt{1 - \operatorname{Cos}[c + dx]^2} \right) \\
 \left(\left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[c + dx]^2, \frac{b^2 \operatorname{Cos}[c + dx]^2}{-a^2 + b^2} \right] \right. \right. \\
 \left. \left. \sqrt{\operatorname{Cos}[c + dx]} \sqrt{1 - \operatorname{Cos}[c + dx]^2} \right) / \right. \\
 \left(\left(-5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[c + dx]^2, \frac{b^2 \operatorname{Cos}[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\
 \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \operatorname{Cos}[c + dx]^2, \frac{b^2 \operatorname{Cos}[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\
 \left. \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Cos}[c + dx]^2, \frac{b^2 \operatorname{Cos}[c + dx]^2}{-a^2 + b^2} \right] \right) \right) \right. \\
 \left. \left. \operatorname{Cos}[c + dx]^2 \right) (a^2 + b^2 (-1 + \operatorname{Cos}[c + dx]^2)) \right) + \\
 \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[c + dx]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \\
 \left. \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[c + dx]} + b \operatorname{Cos}[c + dx] \right] + \right. \right. \\
 \left. \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[c + dx]} + b \operatorname{Cos}[c + dx] \right] \right) \right) / \\
 \left(4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \operatorname{Sin}[c + dx]^2 + \frac{1}{d} \\
 (e \operatorname{Cos}[c + dx])^{11/2} \operatorname{Sec}[c + dx]^5 \left(\frac{(-9 a^2 + 14 b^2) \operatorname{Cos}[2(c + dx)]}{45 b^3} + \right. \\
 \frac{\operatorname{Cos}[4(c + dx)]}{36 b} - \\
 \frac{a (28 a^2 - 51 b^2) \operatorname{Sin}[c + dx]}{42 b^4} + \\
 \left. \frac{a \operatorname{Sin}[3(c + dx)]}{14 b^2} \right)$$

Problem 575: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{9/2}}{a + b \sin [c + d x]} dx$$

Optimal (type 4, 446 leaves, 14 steps):

$$\begin{aligned} & \frac{(-a^2 + b^2)^{7/4} e^{9/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{b^{9/2} d} - \frac{(-a^2 + b^2)^{7/4} e^{9/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{b^{9/2} d} + \\ & \frac{2 e (e \cos [c + d x])^{7/2}}{7 b d} - \frac{2 a (5 a^2 - 8 b^2) e^4 \sqrt{e \cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{5 b^4 d \sqrt{\cos [c + d x]}} + \\ & \frac{a (a^2 - b^2)^2 e^5 \sqrt{\cos [c + d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{b^5 (b - \sqrt{-a^2 + b^2}) d \sqrt{e \cos [c + d x]}} + \\ & \frac{a (a^2 - b^2)^2 e^5 \sqrt{\cos [c + d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{b^5 (b + \sqrt{-a^2 + b^2}) d \sqrt{e \cos [c + d x]}} - \\ & \frac{2 e^3 (e \cos [c + d x])^{3/2} (5 (a^2 - b^2) - 3 a b \sin [c + d x])}{15 b^3 d} \end{aligned}$$

Result (type 6, 1228 leaves):

$$\begin{aligned} & - \frac{1}{5 b^3 d \cos [c + d x]^{9/2}} (e \cos [c + d x])^{9/2} \\ & \left(\frac{1}{12 \sqrt{1 - \cos [c + d x]^2} (a + b \sin [c + d x])} (2 a^2 b - 5 b^3) \left(a + b \sqrt{1 - \cos [c + d x]^2} \right) \right. \\ & \quad \left(- \left(\left(56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \right. \right. \right. \right. \\ & \quad \left. \left. \left. \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \cos [c + d x]^{3/2} \right) / \left(\sqrt{1 - \cos [c + d x]^2} \right) \right. \right. \\ & \quad \left. \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] - \right. \right. \\ & \quad \left. \left. 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\ & \quad \left. \left. \left. (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \right) \right) \\ & \quad \left. \left. \left. \cos [c + d x]^2 \right) (a^2 + b^2 (-1 + \cos [c + d x]^2)) \right) \right) \right) - \end{aligned}$$

$$\begin{aligned}
 & \left((3 + 3i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i)\sqrt{b}\sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[\right. \right. \right. \\
 & \quad \left. \left. \left. 1 + \frac{(1+i)\sqrt{b}\sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i)\sqrt{b}(-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos[c+dx]} + ib\cos[c+dx] \right] + \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i)\sqrt{b}(-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos[c+dx]} + ib\cos[c+dx] \right] \right) \right) / \left(\sqrt{b}(-a^2+b^2)^{1/4} \right) \sin[c+dx] - \\
 & \frac{1}{(1-\cos[c+dx]^2)(a+b\sin[c+dx])} 2(5a^3-8ab^2) \left(a+b\sqrt{1-\cos[c+dx]^2} \right) \\
 & \left(\left(7b(a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c+dx]^2, \frac{b^2\cos[c+dx]^2}{-a^2+b^2} \right] \right. \right. \\
 & \quad \left. \left. \cos[c+dx]^{3/2} \sqrt{1-\cos[c+dx]^2} \right) / \right. \\
 & \left(3 \left(-7(a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c+dx]^2, \frac{b^2\cos[c+dx]^2}{-a^2+b^2} \right] + 2 \right. \right. \\
 & \quad \left(2b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[c+dx]^2, \frac{b^2\cos[c+dx]^2}{-a^2+b^2} \right] + \right. \\
 & \quad \left. \left. (a^2-b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[c+dx]^2, \frac{b^2\cos[c+dx]^2}{-a^2+b^2} \right] \right) \right) \\
 & \quad \left. \cos[c+dx]^2 \right) (a^2+b^2(-1+\cos[c+dx]^2)) \Big) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2}\sqrt{b}\sqrt{\cos[c+dx]}}{(a^2-b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2}\sqrt{b}\sqrt{\cos[c+dx]}}{(a^2-b^2)^{1/4}} \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[\sqrt{a^2-b^2} - \sqrt{2}\sqrt{b}(a^2-b^2)^{1/4} \sqrt{\cos[c+dx]} + b\cos[c+dx] \right] - \operatorname{Log} \left[\right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{a^2-b^2} + \sqrt{2}\sqrt{b}(a^2-b^2)^{1/4} \sqrt{\cos[c+dx]} + b\cos[c+dx] \right] \right) \right) / \Big) \\
 & \left(4\sqrt{2}b^{3/2}(a^2-b^2)^{1/4} \right) \sin[c+dx]^2 \Big) + \frac{1}{d} \\
 & (e \cos[c+dx])^{9/2} \operatorname{Sec}[c+dx]^4 \left(\frac{(-28a^2+37b^2)\cos[c+dx]}{42b^3} + \right. \\
 & \quad \frac{\cos[3(c+dx)]}{14b} + \\
 & \quad \left. \frac{a \sin[2(c+dx)]}{5b^2} \right)
 \end{aligned}$$

Problem 576: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{7/2}}{a + b \sin [c + d x]} dx$$

Optimal (type 4, 461 leaves, 14 steps):

$$\begin{aligned} & - \frac{(-a^2 + b^2)^{5/4} e^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{b^{7/2} d} - \frac{(-a^2 + b^2)^{5/4} e^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{b^{7/2} d} + \\ & \frac{2 e (e \cos [c + d x])^{5/2}}{5 b d} - \frac{2 a (3 a^2 - 4 b^2) e^4 \sqrt{\cos [c + d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{3 b^4 d \sqrt{e \cos [c + d x]}} + \\ & \frac{a (a^2 - b^2)^2 e^4 \sqrt{\cos [c + d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{b^4 (a^2 - b (b - \sqrt{-a^2 + b^2})) d \sqrt{e \cos [c + d x]}} + \\ & \frac{a (a^2 - b^2)^2 e^4 \sqrt{\cos [c + d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{b^4 (a^2 - b (b + \sqrt{-a^2 + b^2})) d \sqrt{e \cos [c + d x]}} - \\ & \frac{2 e^3 \sqrt{e \cos [c + d x]} (3 (a^2 - b^2) - a b \sin [c + d x])}{3 b^3 d} \end{aligned}$$

Result (type 6, 2155 leaves):

$$\begin{aligned} & \frac{(e \cos [c + d x])^{7/2} \operatorname{Sec}[c + d x]^3 \left(\frac{\cos [2 (c + d x)]}{5 b} + \frac{2 a \sin [c + d x]}{3 b^2}\right)}{d} - \\ & \frac{1}{60 b^2 d \cos [c + d x]^{7/2}} (e \cos [c + d x])^{7/2} \\ & \left(- \frac{1}{\sqrt{1 - \cos [c + d x]^2} (a + b \sin [c + d x])} - 2 (10 a^2 - 27 b^2) (a + b \sqrt{1 - \cos [c + d x]^2}) \right. \\ & \left. \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2}\right] \sqrt{\cos [c + d x]} \right) / \right. \right. \\ & \left. \left(\sqrt{1 - \cos [c + d x]^2} \right. \right. \\ & \left. \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2}\right] - 2 \right. \right. \\ & \left. \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \right. \right. \\ & \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2}\right] \right) \cos [c + d x]^2 \right) \\ & \left. \left. (a^2 + b^2 (-1 + \cos [c + d x]^2)) \right) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8}\right) \sqrt{b} \end{aligned}$$

$$\begin{aligned}
 & \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] + \right. \\
 & \quad \left. \operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] - \right. \\
 & \quad \left. \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] \right) \\
 & \sin [c+d x] + \frac{1}{\sqrt{1-\cos [c+d x]^2} (-1+2 \cos [c+d x]^2) (a+b \sin [c+d x])} \\
 & (30 a^2 - 33 b^2) \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \cos [2(c+d x)] \\
 & \left(\frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right]}{b^{3/2} (-a^2+b^2)^{3/4}} - \right. \\
 & \quad \left. \frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right]}{b^{3/2} (-a^2+b^2)^{3/4}} + \frac{4 \sqrt{\cos [c+d x]}}{b} + \right. \\
 & \quad \left(10 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \sqrt{\cos [c+d x]} \right) / \\
 & \quad \left(\sqrt{1-\cos [c+d x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \right. \right. \right. \\
 & \quad \quad \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \right. \right. \right. \\
 & \quad \quad \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \right. \\
 & \quad \quad \left. \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \cos [c+d x]^2 \right) (a^2+b^2 (-1+\cos [c+d x]^2)) \right) - \\
 & (36 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \\
 & \quad \cos [c+d x]^{5/2} \right) / \left(5 \sqrt{1-\cos [c+d x]^2} \right. \\
 & \quad \left(9 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] - \right. \\
 & \quad \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \right. \\
 & \quad \quad \left. \left. \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \cos [c+d x]^2 \right) \\
 & \quad \left. (a^2+b^2 (-1+\cos [c+d x]^2)) \right) + \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[\sqrt{-a^2+b^2} - \right. \right. \\
 & \quad \left. \left. (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] \right) / \left(b^{3/2} (-a^2+b^2)^{3/4} \right) -
 \end{aligned}$$

$$\left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2a^2 + b^2) \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\operatorname{Cos}[c + dx]} + \right. \right. \\
 \left. \left. i b \operatorname{Cos}[c + dx] \right] \right) / \left(b^{3/2} (-a^2 + b^2)^{3/4} \right) \operatorname{Sin}[c + dx] + \\
 \frac{1}{(1 - \operatorname{Cos}[c + dx]^2) (a + b \operatorname{Sin}[c + dx])} 28 a b \left(a + b \sqrt{1 - \operatorname{Cos}[c + dx]^2} \right) \\
 \left(\left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[c + dx]^2, \frac{b^2 \operatorname{Cos}[c + dx]^2}{-a^2 + b^2} \right] \right. \right. \\
 \left. \left. \sqrt{\operatorname{Cos}[c + dx]} \sqrt{1 - \operatorname{Cos}[c + dx]^2} \right) / \right. \\
 \left(\left(-5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[c + dx]^2, \frac{b^2 \operatorname{Cos}[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \\
 \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \operatorname{Cos}[c + dx]^2, \frac{b^2 \operatorname{Cos}[c + dx]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\
 \left. \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Cos}[c + dx]^2, \frac{b^2 \operatorname{Cos}[c + dx]^2}{-a^2 + b^2} \right] \right) \right) \right. \\
 \left. \left. \operatorname{Cos}[c + dx]^2 (a^2 + b^2 (-1 + \operatorname{Cos}[c + dx]^2)) \right) \right) + \\
 \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[c + dx]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[c + dx]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \\
 \left. \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[c + dx]} + b \operatorname{Cos}[c + dx] \right] + \right. \right. \\
 \left. \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\operatorname{Cos}[c + dx]} + b \operatorname{Cos}[c + dx] \right] \right) \right) / \\
 \left(4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \operatorname{Sin}[c + dx]^2 \left. \right)$$

Problem 577: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \operatorname{Cos}[c + dx])^{5/2}}{a + b \operatorname{Sin}[c + dx]} dx$$

Optimal (type 4, 384 leaves, 13 steps):

$$\frac{(-a^2 + b^2)^{3/4} e^{5/2} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c+dx]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{b^{5/2} d} - \frac{(-a^2 + b^2)^{3/4} e^{5/2} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c+dx]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{b^{5/2} d} +$$

$$\frac{2 e (e \cos[c+dx])^{3/2}}{3 b d} + \frac{2 a e^2 \sqrt{e \cos[c+dx]} \text{EllipticE}\left[\frac{1}{2} (c+dx), 2\right]}{b^2 d \sqrt{\cos[c+dx]}} -$$

$$\frac{a (a^2 - b^2) e^3 \sqrt{\cos[c+dx]} \text{EllipticPi}\left[\frac{2b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+dx), 2\right]}{b^3 (b - \sqrt{-a^2+b^2}) d \sqrt{e \cos[c+dx]}} -$$

$$\frac{a (a^2 - b^2) e^3 \sqrt{\cos[c+dx]} \text{EllipticPi}\left[\frac{2b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+dx), 2\right]}{b^3 (b + \sqrt{-a^2+b^2}) d \sqrt{e \cos[c+dx]}}$$

Result (type 6, 1151 leaves):

$$\frac{2 (e \cos[c+dx])^{5/2} \text{Sec}[c+dx]}{3 b d} + \frac{1}{b d \cos[c+dx]^{5/2}}$$

$$(e \cos[c+dx])^{5/2} \left(\frac{1}{12 \sqrt{1 - \cos[c+dx]^2} (a + b \sin[c+dx])} b (a + b \sqrt{1 - \cos[c+dx]^2}) \right.$$

$$\left. - \left(\left(56 a (a^2 - b^2) \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2 + b^2}\right] \cos[c+dx]^{3/2} \right) / \right.$$

$$\left(\sqrt{1 - \cos[c+dx]^2} \left(7 (a^2 - b^2) \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2 + b^2}\right] - 2 \left(2 b^2 \text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \text{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2 + b^2}\right] \right) \cos[c+dx]^2 (a^2 + b^2 (-1 + \cos[c+dx]^2)) \right) \right) -$$

$$\left((3 + 3i) \left(2 \text{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos[c+dx]}}{(-a^2 + b^2)^{1/4}}\right] - 2 \text{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos[c+dx]}}{(-a^2 + b^2)^{1/4}}\right] - \text{Log}\left[\sqrt{-a^2 + b^2} - (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c+dx]} + i b \cos[c+dx]\right] + \text{Log}\left[\sqrt{-a^2 + b^2} + (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos[c+dx]} + i b \cos[c+dx]\right] \right) / \left(\sqrt{b} (-a^2 + b^2)^{1/4} \right) \right) \sin[c+dx] -$$

$$\frac{1}{(1 - \cos[c+dx]^2) (a + b \sin[c+dx])} 2 a (a + b \sqrt{1 - \cos[c+dx]^2})$$

$$\left(\left(7 b (a^2 - b^2) \text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2 + b^2}\right] \right.$$

$$\begin{aligned}
 & \left. \left(\cos [c+d x]^{3/2} \sqrt{1-\cos [c+d x]^2} \right) / \right. \\
 & \left(3 \left(-7 \left(a^2-b^2 \right) \operatorname{AppellF1}\left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \right. \right. \\
 & \quad 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4},-\frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \right. \\
 & \quad \left. \left. \left(a^2-b^2 \right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \right) \\
 & \left. \cos [c+d x]^2 \right) \left(a^2+b^2 \left(-1+\cos [c+d x]^2 \right) \right) \left. \right) + \\
 & \left(a \left(-2 \operatorname{ArcTan}\left[1-\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2 \right)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1+\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2 \right)^{1/4}}\right] \right) + \right. \\
 & \quad \operatorname{Log}\left[\sqrt{a^2-b^2}-\sqrt{2} \sqrt{b}\left(a^2-b^2 \right)^{1/4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right]- \\
 & \quad \left. \left. \operatorname{Log}\left[\sqrt{a^2-b^2}+\sqrt{2} \sqrt{b}\left(a^2-b^2 \right)^{1/4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right] \right) \right) / \right. \\
 & \left. \left(4 \sqrt{2} b^{3/2}\left(a^2-b^2 \right)^{1/4} \right) \sin [c+d x]^2 \right)
 \end{aligned}$$

Problem 578: Result unnecessarily involves higher level functions.

$$\int \frac{\left(e \cos [c+d x] \right)^{3/2}}{a+b \sin [c+d x]} dx$$

Optimal (type 4, 397 leaves, 13 steps):

$$\begin{aligned}
 & -\frac{\left(-a^2+b^2 \right)^{1/4} e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2 \right)^{1/4} \sqrt{e}}\right]}{b^{3/2} d} - \frac{\left(-a^2+b^2 \right)^{1/4} e^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2 \right)^{1/4} \sqrt{e}}\right]}{b^{3/2} d} + \\
 & \frac{2 e \sqrt{e \cos [c+d x]}}{b d} + \frac{2 a e^2 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{b^2 d \sqrt{e \cos [c+d x]}} - \\
 & \frac{a \left(a^2-b^2 \right) e^2 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{b^2 \left(a^2-b \left(b-\sqrt{-a^2+b^2} \right) \right) d \sqrt{e \cos [c+d x]}} - \\
 & \frac{a \left(a^2-b^2 \right) e^2 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{b^2 \left(a^2-b \left(b+\sqrt{-a^2+b^2} \right) \right) d \sqrt{e \cos [c+d x]}}
 \end{aligned}$$

Result (type 6, 624 leaves):

$$\begin{aligned}
 & \frac{1}{20 d \operatorname{Cos}[c+d x]^{3/2} \sqrt{1-\operatorname{Cos}[c+d x]^2} (a+b \operatorname{Sin}[c+d x])} \\
 & (e \operatorname{Cos}[c+d x])^{3/2} \left(a+b \sqrt{1-\operatorname{Cos}[c+d x]^2} \right) \\
 & \left(-\left(\left(72 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Cos}[c+d x]^2, \frac{b^2 \operatorname{Cos}[c+d x]^2}{-a^2+b^2}\right] \operatorname{Cos}[c+d x]^{5/2} \right) / \right. \right. \\
 & \left. \left(\sqrt{1-\operatorname{Cos}[c+d x]^2} \left(9 (a^2-b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Cos}[c+d x]^2, \frac{b^2 \operatorname{Cos}[c+d x]^2}{-a^2+b^2}\right] - \right. \right. \right. \\
 & \left. \left. 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \operatorname{Cos}[c+d x]^2, \frac{b^2 \operatorname{Cos}[c+d x]^2}{-a^2+b^2}\right] + \right. \right. \right. \\
 & \left. \left. \left. (-a^2+b^2) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \operatorname{Cos}[c+d x]^2, \frac{b^2 \operatorname{Cos}[c+d x]^2}{-a^2+b^2}\right] \right) \right) \right) \right) \left. \right) \left. \right) + \\
 & \frac{1}{b^{3/2}} (5-5 i) \left(2 (-a^2+b^2)^{1/4} \operatorname{ArcTan}\left[1-\frac{(1+i) \sqrt{b} \sqrt{\operatorname{Cos}[c+d x]}}{(-a^2+b^2)^{1/4}}\right] - 2 (-a^2+b^2)^{1/4} \right. \\
 & \left. \operatorname{ArcTan}\left[1+\frac{(1+i) \sqrt{b} \sqrt{\operatorname{Cos}[c+d x]}}{(-a^2+b^2)^{1/4}}\right] + (4+4 i) \sqrt{b} \sqrt{\operatorname{Cos}[c+d x]} + (-a^2+b^2)^{1/4} \right. \\
 & \left. \operatorname{Log}\left[\sqrt{-a^2+b^2}-(1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\operatorname{Cos}[c+d x]}+i b \operatorname{Cos}[c+d x]\right]-(-a^2+b^2)^{1/4} \right. \\
 & \left. \left. \operatorname{Log}\left[\sqrt{-a^2+b^2}+(1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\operatorname{Cos}[c+d x]}+i b \operatorname{Cos}[c+d x]\right] \right) \right) \operatorname{Sin}[c+d x]
 \end{aligned}$$

Problem 579: Result unnecessarily involves higher level functions.

$$\int \frac{\sqrt{e \operatorname{Cos}[c+d x]}}{a+b \operatorname{Sin}[c+d x]} dx$$

Optimal (type 4, 292 leaves, 9 steps):

$$\begin{aligned}
 & \frac{\sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \operatorname{Cos}[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{\sqrt{b} (-a^2+b^2)^{1/4} d} - \frac{\sqrt{e} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \operatorname{Cos}[c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{\sqrt{b} (-a^2+b^2)^{1/4} d} + \\
 & \frac{a e \sqrt{\operatorname{Cos}[c+d x]} \operatorname{EllipticPi}\left[\frac{-2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{b\left(b-\sqrt{-a^2+b^2}\right) d \sqrt{e \operatorname{Cos}[c+d x]}} + \\
 & \frac{a e \sqrt{\operatorname{Cos}[c+d x]} \operatorname{EllipticPi}\left[\frac{-2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{b\left(b+\sqrt{-a^2+b^2}\right) d \sqrt{e \operatorname{Cos}[c+d x]}}
 \end{aligned}$$

Result (type 6, 565 leaves):

$$\begin{aligned}
 & \frac{1}{12 d \sqrt{\cos [c+d x]} \sqrt{1-\cos [c+d x]^2} (a+b \sin [c+d x])} \\
 & \sqrt{e \cos [c+d x]} \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \\
 & \left(- \left(\left(56 a \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \cos [c+d x]^{3/2} \right) / \right. \right. \\
 & \quad \left(\sqrt{1-\cos [c+d x]^2} \left(7 \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] - \right. \right. \\
 & \quad \quad \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \right. \\
 & \quad \quad \left. \left. \left. \left(-a^2+b^2 \right) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \cos [c+d x]^2 \right) \right) \\
 & \quad \left. \left. \left. \left(a^2+b^2 \left(-1+\cos [c+d x]^2 \right) \right) \right) \right) - \left((3+3 i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2 \right)^{1/4}} \right] - \right. \right. \right. \\
 & \quad \left. \left. \left. 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2 \right)^{1/4}} \right] - \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} \left(-a^2+b^2 \right)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] + \right. \right. \right. \\
 & \quad \left. \left. \left. \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} \left(-a^2+b^2 \right)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] \right) \right) \right) / \\
 & \quad \left(\sqrt{b} \left(-a^2+b^2 \right)^{1/4} \right) \sin [c+d x]
 \end{aligned}$$

Problem 580: Result unnecessarily involves higher level functions.

$$\int \frac{1}{\sqrt{e \cos [c+d x]} (a+b \sin [c+d x])} dx$$

Optimal (type 4, 299 leaves, 9 steps):

$$\begin{aligned}
 & - \frac{\sqrt{b} \operatorname{ArcTan} \left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2 \right)^{1/4} \sqrt{e}} \right]}{\left(-a^2+b^2 \right)^{3/4} d \sqrt{e}} - \frac{\sqrt{b} \operatorname{ArcTanh} \left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2 \right)^{1/4} \sqrt{e}} \right]}{\left(-a^2+b^2 \right)^{3/4} d \sqrt{e}} + \\
 & \frac{a \sqrt{\cos [c+d x]} \operatorname{EllipticPi} \left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right]}{\left(a^2-b \left(b-\sqrt{-a^2+b^2} \right) \right) d \sqrt{e \cos [c+d x]}} + \\
 & \frac{a \sqrt{\cos [c+d x]} \operatorname{EllipticPi} \left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right]}{\left(a^2-b \left(b+\sqrt{-a^2+b^2} \right) \right) d \sqrt{e \cos [c+d x]}}
 \end{aligned}$$

Result (type 6, 567 leaves):

Result (type 6, 1186 leaves):

$$\begin{aligned}
 & \frac{2 \operatorname{Cos}[c + d x] (-b + a \operatorname{Sin}[c + d x])}{(a^2 - b^2) d (e \operatorname{Cos}[c + d x])^{3/2}} - \frac{1}{(a - b) (a + b) d (e \operatorname{Cos}[c + d x])^{3/2}} \\
 & \operatorname{Cos}[c + d x]^{3/2} \left(\frac{1}{12 \sqrt{1 - \operatorname{Cos}[c + d x]^2} (a + b \operatorname{Sin}[c + d x])} (a^2 + b^2) \left(a + b \sqrt{1 - \operatorname{Cos}[c + d x]^2} \right) \right. \\
 & \left. - \left(\left(56 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \operatorname{Cos}[c + d x]^2, \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2} \right] \operatorname{Cos}[c + d x]^{3/2} \right) / \right. \right. \\
 & \left. \left(\sqrt{1 - \operatorname{Cos}[c + d x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \operatorname{Cos}[c + d x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \operatorname{Cos}[c + d x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \operatorname{Cos}[c + d x]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2} \right] \right) \operatorname{Cos}[c + d x]^2 \left. \right) (a^2 + b^2 (-1 + \operatorname{Cos}[c + d x]^2)) \right) \left. \right) - \\
 & \left((3 + 3 i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1 + i) \sqrt{b} \sqrt{\operatorname{Cos}[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[\right. \right. \right. \\
 & \left. \left. 1 + \frac{(1 + i) \sqrt{b} \sqrt{\operatorname{Cos}[c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2 + b^2} - (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \\
 & \left. \left. \sqrt{\operatorname{Cos}[c + d x]} + i b \operatorname{Cos}[c + d x] \right] + \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \\
 & \left. \left. \sqrt{\operatorname{Cos}[c + d x]} + i b \operatorname{Cos}[c + d x] \right] \right) \left. \right) / \left(\sqrt{b} (-a^2 + b^2)^{1/4} \right) \operatorname{Sin}[c + d x] - \\
 & \frac{1}{(1 - \operatorname{Cos}[c + d x]^2) (a + b \operatorname{Sin}[c + d x])} 2 a b \left(a + b \sqrt{1 - \operatorname{Cos}[c + d x]^2} \right) \\
 & \left(\left(7 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \operatorname{Cos}[c + d x]^2, \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\
 & \left. \left. \operatorname{Cos}[c + d x]^{3/2} \sqrt{1 - \operatorname{Cos}[c + d x]^2} \right) \right) / \\
 & \left(3 \left(-7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \operatorname{Cos}[c + d x]^2, \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \left. \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \operatorname{Cos}[c + d x]^2, \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \operatorname{Cos}[c + d x]^2, \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2} \right] \right) \right. \\
 & \left. \left. \operatorname{Cos}[c + d x]^2 \right) (a^2 + b^2 (-1 + \operatorname{Cos}[c + d x]^2)) \right) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[c + d x]}}{(a^2 - b^2)^{1/4}} \right] \right) + \right.
 \end{aligned}$$

$$\left(\frac{\text{Log}\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[c + d x]} + b \text{Cos}[c + d x]\right] - \text{Log}\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[c + d x]} + b \text{Cos}[c + d x]\right]}{4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4}} \right) \text{Sin}[c + d x]^2$$

Problem 582: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \text{Cos}[c + d x])^{5/2} (a + b \text{Sin}[c + d x])} dx$$

Optimal (type 4, 434 leaves, 13 steps):

$$\begin{aligned} & - \frac{b^{5/2} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \text{Cos}[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right] - b^{5/2} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \text{Cos}[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{(-a^2 + b^2)^{7/4} d e^{5/2}} + \\ & \frac{2 a \sqrt{\text{Cos}[c + d x]} \text{EllipticF}\left[\frac{1}{2} (c + d x), 2\right]}{3 (a^2 - b^2) d e^2 \sqrt{e \text{Cos}[c + d x]}} - \\ & \frac{a b^2 \sqrt{\text{Cos}[c + d x]} \text{EllipticPi}\left[\frac{-2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{(a^2 - b^2) (a^2 - b (b - \sqrt{-a^2 + b^2})) d e^2 \sqrt{e \text{Cos}[c + d x]}} - \\ & \frac{a b^2 \sqrt{\text{Cos}[c + d x]} \text{EllipticPi}\left[\frac{-2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{(a^2 - b^2) (a^2 - b (b + \sqrt{-a^2 + b^2})) d e^2 \sqrt{e \text{Cos}[c + d x]}} - \frac{2 (b - a \text{Sin}[c + d x])}{3 (a^2 - b^2) d e (e \text{Cos}[c + d x])^{3/2}} \end{aligned}$$

Result (type 6, 1192 leaves):

$$\begin{aligned} & \frac{2 \text{Cos}[c + d x] (-b + a \text{Sin}[c + d x])}{3 (a^2 - b^2) d (e \text{Cos}[c + d x])^{5/2}} + \\ & \frac{1}{3 (a - b) (a + b) d (e \text{Cos}[c + d x])^{5/2}} \text{Cos}[c + d x]^{5/2} \left(- \frac{1}{\sqrt{1 - \text{Cos}[c + d x]^2} (a + b \text{Sin}[c + d x])} \right. \\ & \left. 2 (a^2 - 3 b^2) (a + b \sqrt{1 - \text{Cos}[c + d x]^2}) \left(\left(5 a (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \right. \\ & \left. \left. \left. \text{Cos}[c + d x]^2, \frac{b^2 \text{Cos}[c + d x]^2}{-a^2 + b^2}\right] \sqrt{\text{Cos}[c + d x]} \right) / \left(\sqrt{1 - \text{Cos}[c + d x]^2} \right. \right. \\ & \left. \left. \left(5 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \text{Cos}[c + d x]^2, \frac{b^2 \text{Cos}[c + d x]^2}{-a^2 + b^2}\right] - 2 \right. \right. \right. \\ & \left. \left. \left. \left(2 b^2 \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \text{Cos}[c + d x]^2, \frac{b^2 \text{Cos}[c + d x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \right) \right) \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\text{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \cos [c+d x]^2 \right) \right. \\
 & \left. \left(a^2+b^2 (-1+\cos [c+d x]^2) \right) \right) - \frac{1}{(-a^2+b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
 & \left(2 \text{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \text{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] \right) + \\
 & \left(\text{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] - \right. \\
 & \left. \text{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] \right) \Bigg) \\
 & \sin [c+d x] - \frac{1}{(1-\cos [c+d x]^2) (a+b \sin [c+d x])} 2 a b \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \\
 & \left(\left(5 b (a^2-b^2) \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right. \right. \\
 & \left. \left. \sqrt{\cos [c+d x]} \sqrt{1-\cos [c+d x]^2} \right) \right) / \\
 & \left(\left(-5 (a^2-b^2) \text{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) + \right. \\
 & \left. 2 \left(2 b^2 \text{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
 & \left. \left. (a^2-b^2) \text{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \right) \\
 & \left. \cos [c+d x]^2 \right) \left(a^2+b^2 (-1+\cos [c+d x]^2) \right) \Bigg) + \\
 & \left(a \left(-2 \text{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{(a^2-b^2)^{1/4}} \right] + 2 \text{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{(a^2-b^2)^{1/4}} \right] \right) - \right. \\
 & \left. \text{Log} \left[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [c+d x]} + b \cos [c+d x] \right] + \right. \\
 & \left. \text{Log} \left[\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [c+d x]} + b \cos [c+d x] \right] \right) \Bigg) / \\
 & \left(4 \sqrt{2} \sqrt{b} (a^2-b^2)^{3/4} \right) \sin [c+d x]^2 \Bigg)
 \end{aligned}$$

Problem 583: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \cos [c+d x])^{7/2} (a+b \sin [c+d x])} dx$$

Optimal (type 4, 486 leaves, 14 steps):

$$\frac{b^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4} \sqrt{e}}\right]}{\left(-a^2+b^2\right)^{9/4} d e^{7/2}} - \frac{b^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4} \sqrt{e}}\right]}{\left(-a^2+b^2\right)^{9/4} d e^{7/2}} -$$

$$\frac{2 a\left(3 a^2-8 b^2\right) \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5\left(a^2-b^2\right)^2 d e^4 \sqrt{\cos [c+d x]}} +$$

$$\frac{a b^3 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{\left(a^2-b^2\right)^2\left(b-\sqrt{-a^2+b^2}\right) d e^3 \sqrt{e \cos [c+d x]}} +$$

$$\frac{a b^3 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{\left(a^2-b^2\right)^2\left(b+\sqrt{-a^2+b^2}\right) d e^3 \sqrt{e \cos [c+d x]}} -$$

$$\frac{2(b-a \sin [c+d x])}{5\left(a^2-b^2\right) d e\left(e \cos [c+d x]\right)^{5/2}} + \frac{2\left(5 b^3+a\left(3 a^2-8 b^2\right) \sin [c+d x]\right)}{5\left(a^2-b^2\right)^2 d e^3 \sqrt{e \cos [c+d x]}}$$

Result (type 6, 1275 leaves):

$$-\frac{1}{5(a-b)^2(a+b)^2 d(e \cos [c+d x])^{7/2}}$$

$$\cos [c+d x]^{7/2} \left(\frac{1}{12 \sqrt{1-\cos [c+d x]^2} (a+b \sin [c+d x])} (3 a^4-8 a^2 b^2-5 b^4) \right.$$

$$\left. \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \left(-\left(\left(56 a\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right)^2 \right. \right.$$

$$\left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right) \cos [c+d x]^{3/2} \right) / \left(\sqrt{1-\cos [c+d x]^2} \right.$$

$$\left. \left(7\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] - \right. \right.$$

$$\left. \left. 2\left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \right. \right.$$

$$\left. \left. \left(-a^2+b^2\right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \right)$$

$$\cos [c+d x]^2 \left(a^2+b^2(-1+\cos [c+d x]^2) \right) \left. \right) \left. \right) -$$

$$\left((3+3 i) \left(2 \operatorname{ArcTan}\left[1-\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[\right. \right. \right.$$

$$\left. \left. 1+\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4}}\right] - \operatorname{Log}\left[\sqrt{-a^2+b^2}-(1+i) \sqrt{b}(-a^2+b^2)^{1/4} \right. \right.$$

$$\left. \left. \sqrt{\cos [c+d x]}+i b \cos [c+d x]\right] + \operatorname{Log}\left[\sqrt{-a^2+b^2}+(1+i) \sqrt{b}(-a^2+b^2)^{1/4} \right. \right.$$

$$\left. \left. \left. \left. \left. \frac{\sqrt{\cos [c + d x]} + i b \cos [c + d x]}{\left(\sqrt{b} (-a^2 + b^2)^{1/4}\right)} \right) \sin [c + d x] - \right. \right. \right. \right. \\
 \left. \frac{1}{(1 - \cos [c + d x]^2) (a + b \sin [c + d x])} 2 (3 a^3 b - 8 a b^3) (a + b \sqrt{1 - \cos [c + d x]^2}) \right. \\
 \left. \left(\left(7 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \right. \right. \\
 \left. \left. \cos [c + d x]^{3/2} \sqrt{1 - \cos [c + d x]^2} \right) \right) / \\
 \left(3 \left(-7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + 2 \right. \right. \\
 \left. \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \right) \\
 \left. \cos [c + d x]^2 (a^2 + b^2 (-1 + \cos [c + d x]^2)) \right) + \\
 \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] \right) + \right. \\
 \left. \log [\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x]] - \right. \\
 \left. \log [\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + \right. \\
 \left. \left. b \cos [c + d x] \right] \right) / \left(4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin [c + d x]^2 \Bigg) + \\
 \left(\cos [c + d x]^4 \left(\frac{2 \operatorname{Sec} [c + d x]^3 (-b + a \sin [c + d x])}{5 (a^2 - b^2)} + \right. \right. \\
 \left. \left. \frac{2 \operatorname{Sec} [c + d x] (5 b^3 + 3 a^3 \sin [c + d x] - 8 a b^2 \sin [c + d x])}{5 (a^2 - b^2)^2} \right) \right) / \left(d \right. \\
 \left. (e \cos [c + d x])^{7/2} \right)$$

Problem 584: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{11/2}}{(a + b \sin [c + d x])^2} dx$$

Optimal (type 4, 543 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{9 a (-a^2 + b^2)^{5/4} e^{11/2} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 b^{11/2} d} - \frac{9 a (-a^2 + b^2)^{5/4} e^{11/2} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 b^{11/2} d} \\
 & + \frac{3 (21 a^4 - 28 a^2 b^2 + 5 b^4) e^6 \sqrt{\cos [c+d x]} \text{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{7 b^6 d \sqrt{e \cos [c+d x]}} \\
 & + \left(\frac{9 a^2 (a^2 - b^2)^2 e^6 \sqrt{\cos [c+d x]} \text{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 b^6 \left(a^2 - b \left(b - \sqrt{-a^2 + b^2}\right)\right) d \sqrt{e \cos [c+d x]}} \right) + \\
 & + \left(\frac{9 a^2 (a^2 - b^2)^2 e^6 \sqrt{\cos [c+d x]} \text{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 b^6 \left(a^2 - b \left(b + \sqrt{-a^2 + b^2}\right)\right) d \sqrt{e \cos [c+d x]}} \right) + \\
 & - \frac{9 e^3 (e \cos [c+d x])^{5/2} (7 a - 5 b \sin [c+d x])}{35 b^3 d} - \frac{e (e \cos [c+d x])^{9/2}}{b d (a + b \sin [c+d x])} \\
 & - \frac{3 e^5 \sqrt{e \cos [c+d x]} (21 a (a^2 - b^2) - b (7 a^2 - 5 b^2) \sin [c+d x])}{7 b^5 d}
 \end{aligned}$$

Result (type 6, 2230 leaves):

$$\begin{aligned}
 & - \frac{1}{70 b^5 d \cos [c+d x]^{11/2}} (e \cos [c+d x])^{11/2} \\
 & \left(- \frac{1}{\sqrt{1 - \cos [c+d x]^2} (a + b \sin [c+d x])} - 2 (70 a^3 b - 93 a b^3) (a + b \sqrt{1 - \cos [c+d x]^2}) \right. \\
 & \left. \left(\left(5 a (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2}\right] \sqrt{\cos [c+d x]} \right) / \right. \right. \\
 & \left. \left(\sqrt{1 - \cos [c+d x]^2} \left(5 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2}\right] - 2 \left(2 b^2 \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2}\right] \right. \right. \right. \right. \\
 & \left. \left. \left. + (-a^2 + b^2) \text{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2}\right] \right) \cos [c+d x]^2 \right) (a^2 + b^2 (-1 + \cos [c+d x]^2)) \right) \right) - \\
 & \frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \left(2 \text{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2 + b^2)^{1/4}}\right] - \right. \\
 & \left. 2 \text{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2 + b^2)^{1/4}}\right] + \text{Log}\left[\sqrt{-a^2 + b^2} - \right. \right. \\
 & \left. \left. (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] - \text{Log}\left[\sqrt{-a^2 + b^2} + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \left. (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+dx]} + i b \cos[c+dx] \right) \Bigg) \sin[c+dx] + \\
& \frac{1}{\sqrt{1-\cos[c+dx]}^2 (-1+2\cos[c+dx])^2 (a+b\sin[c+dx])} \\
& (140a^3b - 147ab^3) \\
& \left(a + b\sqrt{1-\cos[c+dx]} \right) \cos[2(c+dx)] \\
& \left(\frac{\frac{1}{2} - \frac{i}{2}}{b^{3/2} (-a^2+b^2)^{3/4}} (-2a^2+b^2) \operatorname{ArcTan} \left[1 - \frac{(1+i)\sqrt{b}\sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}} \right] \right. \\
& \left. \frac{\frac{1}{2} - \frac{i}{2}}{b^{3/2} (-a^2+b^2)^{3/4}} (-2a^2+b^2) \operatorname{ArcTan} \left[1 + \frac{(1+i)\sqrt{b}\sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}} \right] \right. + \frac{4\sqrt{\cos[c+dx]}}{b} + \\
& \left. \left(10a(a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] \sqrt{\cos[c+dx]} \right) / \right. \\
& \left. \left(\sqrt{1-\cos[c+dx]}^2 \left(5(a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+dx]^2, \right. \right. \right. \right. \\
& \left. \left. \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] - 2 \left(2b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c+dx]^2, \right. \right. \right. \right. \\
& \left. \left. \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+dx]^2, \right. \right. \right. \\
& \left. \left. \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] \right) \cos[c+dx]^2 (a^2+b^2(-1+\cos[c+dx]^2)) \Bigg) - \\
& \left(36a(a^2-b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] \right. \\
& \left. \cos[c+dx]^{5/2} \right) / \left(5\sqrt{1-\cos[c+dx]}^2 \right. \\
& \left. \left(9(a^2-b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] - 2 \right. \right. \\
& \left. \left. \left(2b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \right. \right. \\
& \left. \left. \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] \right) \cos[c+dx]^2 \right) \\
& \left. (a^2+b^2(-1+\cos[c+dx]^2)) \right) + \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2a^2+b^2) \operatorname{Log} \left[\sqrt{-a^2+b^2} - \right. \right. \\
& \left. \left. (1+i)\sqrt{b}(-a^2+b^2)^{1/4} \sqrt{\cos[c+dx]} + i b \cos[c+dx] \right] \right) / \left(b^{3/2} (-a^2+b^2)^{3/4} \right) - \\
& \left(\frac{1}{4} - \frac{i}{4} \right) (-2a^2+b^2) \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i)\sqrt{b}(-a^2+b^2)^{1/4} \sqrt{\cos[c+dx]} + \right.
\end{aligned}$$

$$\left. \left(\frac{b \cos [c + d x]}{b^{3/2} (-a^2 + b^2)^{3/4}} \right) \sin [c + d x] - \right.$$

$$\frac{1}{(1 - \cos [c + d x]^2) (a + b \sin [c + d x])} 2 (35 a^4 - 126 a^2 b^2 + 75 b^4)$$

$$\left(a + b \sqrt{1 - \cos [c + d x]^2} \right)$$

$$\left(\left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right. \right.$$

$$\left. \left. \sqrt{\cos [c + d x]} \sqrt{1 - \cos [c + d x]^2} \right) \right) /$$

$$\left(\left(-5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + 2 \right. \right.$$

$$\left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right.$$

$$\left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \right)$$

$$\cos [c + d x]^2 (a^2 + b^2 (-1 + \cos [c + d x]^2)) \left. \right) +$$

$$\left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right.$$

$$\left. \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] + \operatorname{Log} \left[\right. \right.$$

$$\left. \left. \sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] \right) \right) /$$

$$\left. \left(4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin [c + d x]^2 \right) + \frac{1}{d}$$

$$(e \cos [c + d x])^{11/2} \sec [c + d x]^5 \left(\frac{2 a \cos [2 (c + d x)]}{5 b^3} - \right.$$

$$\frac{(-28 a^2 + 17 b^2) \sin [c + d x]}{14 b^4} -$$

$$\frac{(-a^2 + b^2)^2}{b^5 (a + b \sin [c + d x])} -$$

$$\left. \frac{\sin [3 (c + d x)]}{14 b^2} \right)$$

Problem 585: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{9/2}}{(a + b \sin [c + d x])^2} dx$$

Optimal (type 4, 459 leaves, 14 steps):

$$\frac{7 a (-a^2 + b^2)^{3/4} e^{9/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{2 b^{9/2} d} - \frac{7 a (-a^2 + b^2)^{3/4} e^{9/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{2 b^{9/2} d} +$$

$$\frac{7 (5 a^2 - 3 b^2) e^4 \sqrt{e \cos [c + d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{5 b^4 d \sqrt{\cos [c + d x]}} -$$

$$\frac{7 a^2 (a^2 - b^2) e^5 \sqrt{\cos [c + d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{2 b^5 (b - \sqrt{-a^2 + b^2}) d \sqrt{e \cos [c + d x]}} -$$

$$\frac{7 a^2 (a^2 - b^2) e^5 \sqrt{\cos [c + d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{2 b^5 (b + \sqrt{-a^2 + b^2}) d \sqrt{e \cos [c + d x]}} +$$

$$\frac{7 e^3 (e \cos [c + d x])^{3/2} (5 a - 3 b \sin [c + d x])}{15 b^3 d} - \frac{e (e \cos [c + d x])^{7/2}}{b d (a + b \sin [c + d x])}$$

Result (type 6, 1229 leaves):

$$\frac{1}{10 b^3 d \cos [c + d x]^{9/2}}$$

$$7 (e \cos [c + d x])^{9/2} \left(\frac{1}{6 \sqrt{1 - \cos [c + d x]^2} (a + b \sin [c + d x])} a b \left(a + b \sqrt{1 - \cos [c + d x]^2} \right) \right.$$

$$\left(- \left(\left(56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2}\right] \cos [c + d x]^{3/2} \right) / \right. \right.$$

$$\left(\sqrt{1 - \cos [c + d x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2}\right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2}\right] \right) \cos [c + d x]^2 \right) (a^2 + b^2 (-1 + \cos [c + d x]^2)) \right) \right) -$$

$$\left((3 + 3 i) \left(2 \operatorname{ArcTan}\left[1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos [c + d x]}}{(-a^2 + b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1 + i) \sqrt{b} \sqrt{\cos [c + d x]}}{(-a^2 + b^2)^{1/4}}\right] - \operatorname{Log}\left[\sqrt{-a^2 + b^2} - (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4}\right] \right) \right)$$

$$\begin{aligned}
 & \left(\frac{\sqrt{\cos [c+d x]}+i b \cos [c+d x]}{\sqrt{\cos [c+d x]}+i b \cos [c+d x]}+\operatorname{Log}\left[\sqrt{-a^2+b^2}+(1+i) \sqrt{b}\left(-a^2+b^2\right)^{1 / 4}\right.\right. \\
 & \left.\left.\frac{\sqrt{\cos [c+d x]}+i b \cos [c+d x]}{\sqrt{\cos [c+d x]}+i b \cos [c+d x]}\right]\right) / \left(\sqrt{b}\left(-a^2+b^2\right)^{1 / 4}\right) \sin [c+d x]- \\
 & \frac{1}{\left(1-\cos [c+d x]^2\right)\left(a+b \sin [c+d x]\right)} 2\left(5 a^2-3 b^2\right)\left(a+b \sqrt{1-\cos [c+d x]^2}\right) \\
 & \left(\left(7 b\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]\right.\right. \\
 & \left.\left.\cos [c+d x]^{3 / 2} \sqrt{1-\cos [c+d x]^2}\right)\right) / \\
 & \left(3\left(-7\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]\right)+\right. \\
 & \left.2\left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4},-\frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]\right)+\right. \\
 & \left.\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]\right) \\
 & \left.\cos [c+d x]^2\right)\left(a^2+b^2\left(-1+\cos [c+d x]^2\right)\right)\right)+ \\
 & \left(a\left(-2 \operatorname{ArcTan}\left[1-\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1 / 4}}\right]+2 \operatorname{ArcTan}\left[1+\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1 / 4}}\right]\right)+\right. \\
 & \left.\operatorname{Log}\left[\sqrt{a^2-b^2}-\sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{1 / 4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right]-\right. \\
 & \left.\operatorname{Log}\left[\sqrt{a^2-b^2}+\sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{1 / 4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right]\right)\right) / \\
 & \left.\left(4 \sqrt{2} b^{3 / 2}\left(a^2-b^2\right)^{1 / 4}\right) \sin [c+d x]^2\right)+\frac{1}{d} \\
 & \left(e \cos [c+d x]\right)^{9 / 2} \sec [c+d x]^4\left(\frac{4 a \cos [c+d x]}{3 b^3}+\right. \\
 & \frac{a^2 \cos [c+d x]-b^2 \cos [c+d x]}{b^3(a+b \sin [c+d x])}- \\
 & \left.\frac{\sin [2(c+d x)]}{5 b^2}\right)
 \end{aligned}$$

Problem 586: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\left(e \cos [c+d x]\right)^{7 / 2}}{\left(a+b \sin [c+d x]\right)^2} d x$$

Optimal (type 4, 473 leaves, 14 steps):

$$\begin{aligned}
 & \frac{5 a (-a^2 + b^2)^{1/4} e^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 b^{7/2} d} - \frac{5 a (-a^2 + b^2)^{1/4} e^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 b^{7/2} d} + \\
 & \frac{5 (3 a^2 - b^2) e^4 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{3 b^4 d \sqrt{e \cos [c+d x]}} - \\
 & \frac{5 a^2 (a^2 - b^2) e^4 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 b^4 (a^2 - b (b - \sqrt{-a^2+b^2})) d \sqrt{e \cos [c+d x]}} - \\
 & \frac{5 a^2 (a^2 - b^2) e^4 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{2 b^4 (a^2 - b (b + \sqrt{-a^2+b^2})) d \sqrt{e \cos [c+d x]}} + \\
 & \frac{5 e^3 \sqrt{e \cos [c+d x]} (3 a - b \sin [c+d x])}{3 b^3 d} - \frac{e (e \cos [c+d x])^{5/2}}{b d (a + b \sin [c+d x])}
 \end{aligned}$$

Result (type 6, 2156 leaves):

$$\begin{aligned}
 & \frac{(e \cos [c+d x])^{7/2} \operatorname{Sec}[c+d x]^3 \left(-\frac{2 \sin [c+d x]}{3 b^2} + \frac{a^2 - b^2}{b^3 (a + b \sin [c+d x])}\right)}{d} + \\
 & \frac{1}{6 b^3 d \cos [c+d x]^{7/2}} (e \cos [c+d x])^{7/2} \left(-\frac{1}{\sqrt{1 - \cos [c+d x]^2} (a + b \sin [c+d x])} \right. \\
 & 8 a b \left(a + b \sqrt{1 - \cos [c+d x]^2} \right) \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \\
 & \left. \left. \left. \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2} \right] \sqrt{\cos [c+d x]} \right) / \left(\sqrt{1 - \cos [c+d x]^2} \right. \right. \\
 & \left. \left. \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2} \right] - 2 \right. \right. \right. \\
 & \left. \left. \left. \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \right. \right. \right. \\
 & \left. \left. \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2} \right] \right) \cos [c+d x]^2 \right) \right. \right. \\
 & \left. \left. (a^2 + b^2 (-1 + \cos [c+d x]^2)) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \right. \\
 & \left. \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2 + b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2 + b^2)^{1/4}}\right] \right) + \right. \\
 & \left. \operatorname{Log}\left[\sqrt{-a^2 + b^2} - (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x]\right] - \right. \\
 & \left. \operatorname{Log}\left[\sqrt{-a^2 + b^2} + (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x]\right] \right) \left. \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sin [c+d x] + \frac{1}{\sqrt{1-\cos [c+d x]^2}(-1+2 \cos [c+d x]^2)(a+b \sin [c+d x])} \\
 6 a b & \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \cos [2(c+d x)] \\
 & \left(\frac{\left(\frac{1}{2}-\frac{i}{2}\right)\left(-2 a^2+b^2\right) \operatorname{ArcTan}\left[1-\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2\right)^{1 / 4}}\right]}{b^{3 / 2}\left(-a^2+b^2\right)^{3 / 4}} - \right. \\
 & \frac{\left(\frac{1}{2}-\frac{i}{2}\right)\left(-2 a^2+b^2\right) \operatorname{ArcTan}\left[1+\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2\right)^{1 / 4}}\right]}{b^{3 / 2}\left(-a^2+b^2\right)^{3 / 4}} + \frac{4 \sqrt{\cos [c+d x]}}{b} + \\
 & \left. \left(10 a\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \sqrt{\cos [c+d x]} \right) / \right. \\
 & \left. \left(\sqrt{1-\cos [c+d x]^2} \left(5\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \left(-a^2+b^2\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \cos [c+d x]^2 \right) \left(a^2+b^2(-1+\cos [c+d x]^2)\right) \right) - \right. \\
 & \left. \left(36 a\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \cos [c+d x]^{5 / 2} \right) / \left(5 \sqrt{1-\cos [c+d x]^2} \right) \right. \\
 & \left. \left(9\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \left(-a^2+b^2\right) \operatorname{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \cos [c+d x]^2 \right) \right. \\
 & \left. \left(a^2+b^2(-1+\cos [c+d x]^2) \right) \right) + \left(\left(\frac{1}{4}-\frac{i}{4}\right)\left(-2 a^2+b^2\right) \operatorname{Log}\left[\sqrt{-a^2+b^2} - \right. \right. \\
 & \left. \left. (1+i) \sqrt{b}\left(-a^2+b^2\right)^{1 / 4} \sqrt{\cos [c+d x]} + i b \cos [c+d x]\right] \right) / \left(b^{3 / 2}\left(-a^2+b^2\right)^{3 / 4} \right) - \\
 & \left. \left(\left(\frac{1}{4}-\frac{i}{4}\right)\left(-2 a^2+b^2\right) \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b}\left(-a^2+b^2\right)^{1 / 4} \sqrt{\cos [c+d x]} + \right. \right. \right. \\
 & \left. \left. i b \cos [c+d x]\right] \right) / \left(b^{3 / 2}\left(-a^2+b^2\right)^{3 / 4} \right) \right) \sin [c+d x] -
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{(1 - \cos [c + d x]^2) (a + b \sin [c + d x])} 2 (3 a^2 - 5 b^2) \left(a + b \sqrt{1 - \cos [c + d x]^2} \right) \\
 & \left(\left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\
 & \quad \left. \left. \sqrt{\cos [c + d x]} \sqrt{1 - \cos [c + d x]^2} \right) / \right. \\
 & \left(\left(-5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \quad 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \\
 & \quad \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \right. \\
 & \quad \left. \cos [c + d x]^2 \right) (a^2 + b^2 (-1 + \cos [c + d x]^2)) \Big) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] + \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] \right) \right) / \\
 & \left. \left(4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin [c + d x]^2 \right)
 \end{aligned}$$

Problem 587: Result unnecessarily involves higher level functions.

$$\int \frac{(e \cos [c + d x])^{5/2}}{(a + b \sin [c + d x])^2} dx$$

Optimal (type 4, 390 leaves, 13 steps):

$$\frac{3 a e^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4} \sqrt{e}}\right]}{2 b^{5/2}\left(-a^2+b^2\right)^{1/4} d}-\frac{3 a e^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4} \sqrt{e}}\right]}{2 b^{5/2}\left(-a^2+b^2\right)^{1/4} d}-\frac{3 e^2 \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{b^2 d \sqrt{\cos [c+d x]}}+\frac{3 a^2 e^3 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{2 b^3\left(b-\sqrt{-a^2+b^2}\right) d \sqrt{e \cos [c+d x]}}+\frac{3 a^2 e^3 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{2 b^3\left(b+\sqrt{-a^2+b^2}\right) d \sqrt{e \cos [c+d x]}}-\frac{e(e \cos [c+d x])^{3/2}}{b d(a+b \sin [c+d x])}$$

Result(type 6, 617 leaves):

$$-\frac{(e \cos [c+d x])^{5/2} \operatorname{Sec}[c+d x]}{b d(a+b \sin [c+d x])}+\frac{1}{b d \cos [c+d x]^{5/2}\left(1-\cos [c+d x]^2\right)(a+b \sin [c+d x])} 3(e \cos [c+d x])^{5/2}\left(a+b \sqrt{1-\cos [c+d x]^2}\right)\left(\left(7 b\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \operatorname{Cos}[c+d x]^{3/2} \sqrt{1-\cos [c+d x]^2}\right) / \left(3\left(-7\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]+2\left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4},-\frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]+\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]\right) \operatorname{Cos}[c+d x]^2\right)\left(a^2+b^2(-1+\cos [c+d x]^2)\right)\right)+\left(a\left(-2 \operatorname{ArcTan}\left[1-\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1/4}}\right]+2 \operatorname{ArcTan}\left[1+\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1/4}}\right]\right)+\operatorname{Log}\left[\sqrt{a^2-b^2}-\sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{1/4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right]-\operatorname{Log}\left[\sqrt{a^2-b^2}+\sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{1/4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right]\right) / \left(4 \sqrt{2} b^{3/2}\left(a^2-b^2\right)^{1/4}\right) \sin [c+d x]^2$$

Problem 588: Result unnecessarily involves higher level functions.

$$\int \frac{(e \cos [c + d x])^{3/2}}{(a + b \sin [c + d x])^2} dx$$

Optimal (type 4, 404 leaves, 13 steps):

$$\begin{aligned} & - \frac{a e^{3/2} \operatorname{ArcTan} \left[\frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{2 b^{3/2} (-a^2 + b^2)^{3/4} d} - \\ & \frac{a e^{3/2} \operatorname{ArcTanh} \left[\frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{2 b^{3/2} (-a^2 + b^2)^{3/4} d} - \frac{e^2 \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[\frac{1}{2} (c + d x), 2 \right]}{b^2 d \sqrt{e \cos [c + d x]}} + \\ & \frac{a^2 e^2 \sqrt{\cos [c + d x]} \operatorname{EllipticPi} \left[\frac{2b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right]}{2 b^2 (a^2 - b (b - \sqrt{-a^2 + b^2})) d \sqrt{e \cos [c + d x]}} + \\ & \frac{a^2 e^2 \sqrt{\cos [c + d x]} \operatorname{EllipticPi} \left[\frac{2b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right]}{2 b^2 (a^2 - b (b + \sqrt{-a^2 + b^2})) d \sqrt{e \cos [c + d x]}} - \frac{e \sqrt{e \cos [c + d x]}}{b d (a + b \sin [c + d x])} \end{aligned}$$

Result (type 6, 614 leaves):

$$\begin{aligned}
& - \frac{(e \cos [c + d x])^{3/2} \operatorname{Sec}[c + d x]}{b d (a + b \sin [c + d x])} + \\
& \frac{1}{b d \cos [c + d x]^{3/2} (1 - \cos [c + d x]^2) (a + b \sin [c + d x])} (e \cos [c + d x])^{3/2} \\
& \left((a + b \sqrt{1 - \cos [c + d x]^2}) \left(\left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \right. \right. \right. \right. \\
& \left. \left. \left. \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \sqrt{\cos [c + d x]} \sqrt{1 - \cos [c + d x]^2} \right) / \right. \\
& \left(\left(-5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
& \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\
& \left. \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \right) \right. \\
& \left. \cos [c + d x]^2 \right) (a^2 + b^2 (-1 + \cos [c + d x]^2)) \Big) + \\
& \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \\
& \left. \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] + \right. \right. \\
& \left. \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] \right) \right) / \\
& \left(4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin [c + d x]^2
\end{aligned}$$

Problem 589: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{e \cos [c + d x]}}{(a + b \sin [c + d x])^2} dx$$

Optimal (type 4, 422 leaves, 13 steps):

$$\begin{aligned}
 & - \frac{a \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 \sqrt{b} (-a^2+b^2)^{5/4} d} + \\
 & \frac{a \sqrt{e} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2 \sqrt{b} (-a^2+b^2)^{5/4} d} + \frac{\sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{(a^2-b^2) d \sqrt{\cos [c+d x]}} + \\
 & \frac{a^2 e \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{-2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{2 b (a^2-b^2) (b-\sqrt{-a^2+b^2}) d \sqrt{e \cos [c+d x]}} + \\
 & \frac{a^2 e \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{-2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{2 b (a^2-b^2) (b+\sqrt{-a^2+b^2}) d \sqrt{e \cos [c+d x]}} + \frac{b (e \cos [c+d x])^{3/2}}{(a^2-b^2) d e (a+b \sin [c+d x])}
 \end{aligned}$$

Result (type 6, 1182 leaves):

$$\begin{aligned}
 & - \frac{b \cos [c+d x] \sqrt{e \cos [c+d x]}}{(-a^2+b^2) d (a+b \sin [c+d x])} + \frac{1}{2 (a-b) (a+b) d \sqrt{\cos [c+d x]}} \\
 & \sqrt{e \cos [c+d x]} \left(\frac{1}{6 \sqrt{1-\cos [c+d x]^2} (a+b \sin [c+d x])} a \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \right. \\
 & \left. \left(- \left(\left(56 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \cos [c+d x]^{3/2} \right) / \right. \right. \right. \\
 & \left. \left(\sqrt{1-\cos [c+d x]^2} \left(7 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \right. \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \right. \right. \right. \\
 & \left. \left. \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \cos [c+d x]^2 \right) (a^2+b^2 (-1+\cos [c+d x]^2)) \right) \left. \right) - \\
 & \left((3+3 i) \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[\right. \right. \right. \\
 & \left. \left. \left. 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] + \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \left. \left. \left. \left. \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] \right) \right) / \left(\sqrt{b} (-a^2+b^2)^{1/4} \right) \sin [c+d x] - \\
 & \frac{1}{(1-\cos [c+d x]^2) (a+b \sin [c+d x])} 2 b \left(a+b \sqrt{1-\cos [c+d x]^2} \right)
 \end{aligned}$$

$$\left(\left(7 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\ \left. \left. \cos [c + d x]^{3/2} \sqrt{1 - \cos [c + d x]^2} \right) / \right. \\ \left(3 \left(-7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\ \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\ \left. \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \right) \right. \\ \left. \cos [c + d x]^2 \right) (a^2 + b^2 (-1 + \cos [c + d x]^2)) \Big) + \\ \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] \right) + \right. \\ \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] - \right. \\ \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] \right) \Big) / \\ \left(4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin [c + d x]^2 \Big)$$

Problem 590: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{e \cos [c + d x]} (a + b \sin [c + d x])^2} dx$$

Optimal (type 4, 429 leaves, 13 steps):

$$\frac{3 a \sqrt{b} \operatorname{ArcTan} \left[\frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{2 (-a^2 + b^2)^{7/4} d \sqrt{e}} + \\ \frac{3 a \sqrt{b} \operatorname{ArcTanh} \left[\frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{2 (-a^2 + b^2)^{7/4} d \sqrt{e}} - \frac{\sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[\frac{1}{2} (c + d x), 2 \right]}{(a^2 - b^2) d \sqrt{e \cos [c + d x]}} + \\ \frac{3 a^2 \sqrt{\cos [c + d x]} \operatorname{EllipticPi} \left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right]}{2 (a^2 - b^2) (a^2 - b (b - \sqrt{-a^2 + b^2})) d \sqrt{e \cos [c + d x]}} + \\ \frac{3 a^2 \sqrt{\cos [c + d x]} \operatorname{EllipticPi} \left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right]}{2 (a^2 - b^2) (a^2 - b (b + \sqrt{-a^2 + b^2})) d \sqrt{e \cos [c + d x]}} + \frac{b \sqrt{e \cos [c + d x]}}{(a^2 - b^2) d e (a + b \sin [c + d x])}$$

Result (type 6, 1181 leaves):

$$\begin{aligned}
 & \frac{b \operatorname{Cos}[c + d x]}{(a^2 - b^2) d \sqrt{e \operatorname{Cos}[c + d x]} (a + b \operatorname{Sin}[c + d x])} + \\
 & \frac{1}{2(a-b)(a+b)d\sqrt{e \operatorname{Cos}[c + d x]}} \sqrt{\operatorname{Cos}[c + d x]} \left(-\frac{1}{\sqrt{1 - \operatorname{Cos}[c + d x]^2} (a + b \operatorname{Sin}[c + d x])} \right. \\
 & 4a \left(a + b \sqrt{1 - \operatorname{Cos}[c + d x]^2} \right) \left(\left(5a(a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \\
 & \left. \left. \left. \operatorname{Cos}[c + d x]^2, \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2}\right] \sqrt{\operatorname{Cos}[c + d x]} \right) / \left(\sqrt{1 - \operatorname{Cos}[c + d x]^2} \right. \right. \\
 & \left. \left(5(a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[c + d x]^2, \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2}\right] - 2 \right. \right. \\
 & \left. \left(2b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \operatorname{Cos}[c + d x]^2, \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \operatorname{Cos}[c + d x]^2, \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2}\right] \right) \operatorname{Cos}[c + d x]^2 \right) \\
 & \left. (a^2 + b^2(-1 + \operatorname{Cos}[c + d x]^2)) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
 & \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i)\sqrt{b}\sqrt{\operatorname{Cos}[c + d x]}}{(-a^2 + b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i)\sqrt{b}\sqrt{\operatorname{Cos}[c + d x]}}{(-a^2 + b^2)^{1/4}}\right] \right) + \\
 & \left. \left(\operatorname{Log}\left[\sqrt{-a^2 + b^2} - (1+i)\sqrt{b}(-a^2 + b^2)^{1/4}\sqrt{\operatorname{Cos}[c + d x]} + ib \operatorname{Cos}[c + d x]\right] - \right. \right. \\
 & \left. \left. \operatorname{Log}\left[\sqrt{-a^2 + b^2} + (1+i)\sqrt{b}(-a^2 + b^2)^{1/4}\sqrt{\operatorname{Cos}[c + d x]} + ib \operatorname{Cos}[c + d x]\right] \right) \right) \\
 & \operatorname{Sin}[c + d x] + \frac{1}{(1 - \operatorname{Cos}[c + d x]^2)(a + b \operatorname{Sin}[c + d x])} 2b \left(a + b \sqrt{1 - \operatorname{Cos}[c + d x]^2} \right) \\
 & \left(\left(5b(a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[c + d x]^2, \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2}\right] \right. \right. \\
 & \left. \left. \sqrt{\operatorname{Cos}[c + d x]} \sqrt{1 - \operatorname{Cos}[c + d x]^2} \right) / \right. \\
 & \left(\left(-5(a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[c + d x]^2, \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2}\right] + \right. \right. \\
 & \left. \left(2b^2 \operatorname{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \operatorname{Cos}[c + d x]^2, \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2}\right] + \right. \right. \\
 & \left. \left. (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Cos}[c + d x]^2, \frac{b^2 \operatorname{Cos}[c + d x]^2}{-a^2 + b^2}\right] \right) \right) \\
 & \left. \operatorname{Cos}[c + d x]^2 \right) (a^2 + b^2(-1 + \operatorname{Cos}[c + d x]^2)) \right) + \\
 & \left(a \left(-2 \operatorname{ArcTan}\left[1 - \frac{\sqrt{2}\sqrt{b}\sqrt{\operatorname{Cos}[c + d x]}}{(a^2 - b^2)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1 + \frac{\sqrt{2}\sqrt{b}\sqrt{\operatorname{Cos}[c + d x]}}{(a^2 - b^2)^{1/4}}\right] \right) - \right.
 \end{aligned}$$

$$\left(\frac{\text{Log}\left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[c + d x]} + b \text{Cos}[c + d x]\right] + \text{Log}\left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\text{Cos}[c + d x]} + b \text{Cos}[c + d x]\right]}{4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4}} \right) \text{Sin}[c + d x]^2$$

Problem 591: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \text{Cos}[c + d x])^{3/2} (a + b \text{Sin}[c + d x])^2} dx$$

Optimal (type 4, 492 leaves, 14 steps):

$$\begin{aligned} & - \frac{5 a b^{3/2} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \text{Cos}[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{2 (-a^2 + b^2)^{9/4} d e^{3/2}} + \frac{5 a b^{3/2} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \text{Cos}[c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}}\right]}{2 (-a^2 + b^2)^{9/4} d e^{3/2}} - \\ & \frac{(2 a^2 + 3 b^2) \sqrt{e \text{Cos}[c + d x]} \text{EllipticE}\left[\frac{1}{2} (c + d x), 2\right]}{(a^2 - b^2)^2 d e^2 \sqrt{\text{Cos}[c + d x]}} - \\ & \frac{5 a^2 b \sqrt{\text{Cos}[c + d x]} \text{EllipticPi}\left[\frac{-2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{2 (a^2 - b^2)^2 (b - \sqrt{-a^2 + b^2}) d e \sqrt{e \text{Cos}[c + d x]}} - \\ & \frac{5 a^2 b \sqrt{\text{Cos}[c + d x]} \text{EllipticPi}\left[\frac{-2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2\right]}{2 (a^2 - b^2)^2 (b + \sqrt{-a^2 + b^2}) d e \sqrt{e \text{Cos}[c + d x]}} + \\ & \frac{b}{(a^2 - b^2) d e \sqrt{e \text{Cos}[c + d x]} (a + b \text{Sin}[c + d x])} - \frac{5 a b - (2 a^2 + 3 b^2) \text{Sin}[c + d x]}{(a^2 - b^2)^2 d e \sqrt{e \text{Cos}[c + d x]}} \end{aligned}$$

Result (type 6, 1260 leaves):

$$\begin{aligned} & - \frac{1}{2 (a - b)^2 (a + b)^2 d (e \text{Cos}[c + d x])^{3/2}} \\ & \text{Cos}[c + d x]^{3/2} \left(\frac{1}{12 \sqrt{1 - \text{Cos}[c + d x]^2} (a + b \text{Sin}[c + d x])} (2 a^3 + 8 a b^2) \right. \\ & \left. (a + b \sqrt{1 - \text{Cos}[c + d x]^2}) \left(- \left(\left(56 a (a^2 - b^2) \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \text{Cos}[c + d x]^2, \right. \right. \right. \right. \right. \right. \\ & \left. \left. \left. \frac{b^2 \text{Cos}[c + d x]^2}{-a^2 + b^2} \right) \text{Cos}[c + d x]^{3/2} \right) / \left(\sqrt{1 - \text{Cos}[c + d x]^2} \right) \right. \right. \\ & \left. \left. \left(7 (a^2 - b^2) \text{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \text{Cos}[c + d x]^2, \frac{b^2 \text{Cos}[c + d x]^2}{-a^2 + b^2} \right] \right) - \right. \right. \end{aligned}$$

$$\begin{aligned}
 & 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \\
 & \quad \left. (-a^2+b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \\
 & \quad \cos [c+d x]^2 \left(a^2+b^2 (-1+\cos [c+d x]^2) \right) \Big) - \\
 & \left((3+3 i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[\right. \right. \right. \\
 & \quad \left. \left. \left. 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] + \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] \right) \right) / \left(\sqrt{b} (-a^2+b^2)^{1/4} \right) \Big) \sin [c+d x] - \\
 & \frac{1}{(1-\cos [c+d x]^2) (a+b \sin [c+d x])} 2 (2 a^2 b+3 b^3) \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \\
 & \left(\left(7 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right. \right. \\
 & \quad \left. \left. \cos [c+d x]^{3/2} \sqrt{1-\cos [c+d x]^2} \right) \right) / \\
 & \left(3 \left(-7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + 2 \right. \right. \\
 & \quad \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \\
 & \quad \left. \left. (a^2-b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \right) \\
 & \quad \cos [c+d x]^2 \left(a^2+b^2 (-1+\cos [c+d x]^2) \right) \Big) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{(a^2-b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{(a^2-b^2)^{1/4}} \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Log} \left[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [c+d x]} + b \cos [c+d x] \right] - \operatorname{Log} \left[\right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [c+d x]} + b \cos [c+d x] \right] \right) \right) / \\
 & \left(4 \sqrt{2} b^{3/2} (a^2-b^2)^{1/4} \right) \Big) \sin [c+d x]^2 + \left(\cos [c+d x]^2 \right. \\
 & \left. \left(-\frac{b^3 \cos [c+d x]}{(a^2-b^2)^2 (a+b \sin [c+d x])} + \frac{2 \sec [c+d x] (-2 a b+a^2 \sin [c+d x]+b^2 \sin [c+d x])}{(a^2-b^2)^2} \right) \right) \Big) / \\
 & (d
 \end{aligned}$$

$$(e \cos [c + d x])^{3/2}$$

Problem 592: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \cos [c + d x])^{5/2} (a + b \sin [c + d x])^2} dx$$

Optimal (type 4, 514 leaves, 14 steps):

$$\frac{7 a b^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2\left(-a^2+b^2\right)^{11/4} d e^{5/2}} + \frac{7 a b^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2\left(-a^2+b^2\right)^{11/4} d e^{5/2}} +$$

$$\frac{\left(2 a^2+5 b^2\right) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{3\left(a^2-b^2\right)^2 d e^2 \sqrt{e \cos [c+d x]}} -$$

$$\frac{7 a^2 b^2 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{2\left(a^2-b^2\right)^2\left(a^2-b\left(b-\sqrt{-a^2+b^2}\right)\right) d e^2 \sqrt{e \cos [c+d x]}} -$$

$$\frac{7 a^2 b^2 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{2\left(a^2-b^2\right)^2\left(a^2-b\left(b+\sqrt{-a^2+b^2}\right)\right) d e^2 \sqrt{e \cos [c+d x]}} +$$

$$\frac{b}{\left(a^2-b^2\right) d e\left(e \cos [c+d x]\right)^{3/2}\left(a+b \sin [c+d x]\right)} - \frac{7 a b-\left(2 a^2+5 b^2\right) \sin [c+d x]}{3\left(a^2-b^2\right)^2 d e\left(e \cos [c+d x]\right)^{3/2}}$$

Result (type 6, 1258 leaves):

$$\frac{1}{6(a-b)^2(a+b)^2 d (e \cos [c+d x])^{5/2}} \cos [c+d x]^{5/2}$$

$$\left(-\frac{1}{\sqrt{1-\cos [c+d x]^2} (a+b \sin [c+d x])} 2\left(2 a^3-16 a b^2\right)\left(a+b \sqrt{1-\cos [c+d x]^2}\right) \right.$$

$$\left. \left(\left(5 a\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \sqrt{\cos [c+d x]}\right) / \right. \right.$$

$$\left. \left(\sqrt{1-\cos [c+d x]^2} \right. \right.$$

$$\left. \left(5\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] - 2 \right. \right.$$

$$\left. \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \left(-a^2+b^2\right) \right. \right.$$

$$\left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \cos [c+d x]^2 \right)$$

$$\begin{aligned}
 & \left. \left(a^2 + b^2 (-1 + \cos [c + d x]^2) \right) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
 & \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] \right) + \\
 & \left(\operatorname{Log} \left[\sqrt{-a^2 + b^2} - (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [c + d x]} + i b \cos [c + d x] \right] - \right. \\
 & \left. \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [c + d x]} + i b \cos [c + d x] \right] \right) \\
 & \sin [c + d x] - \frac{1}{(1 - \cos [c + d x]^2) (a + b \sin [c + d x])} \\
 & 2 (2 a^2 b + 5 b^3) \left(a + b \sqrt{1 - \cos [c + d x]^2} \right) \\
 & \left(\left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\
 & \left. \left. \sqrt{\cos [c + d x]} \sqrt{1 - \cos [c + d x]^2} \right) / \right. \\
 & \left(\left(-5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\
 & \left. \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \right) \right. \\
 & \left. \cos [c + d x]^2 \right) (a^2 + b^2 (-1 + \cos [c + d x]^2)) \left. \right) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] \right) - \right. \\
 & \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] + \right. \\
 & \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] \right) / \left. \right) \\
 & \left(4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin [c + d x]^2 \left. \right) + \\
 & \left(\cos [c + d x]^3 \left(-\frac{b^3}{(a^2 - b^2)^2 (a + b \sin [c + d x])} + \right. \right. \\
 & \left. \left. \frac{2 \sec [c + d x]^2 (-2 a b + a^2 \sin [c + d x] + b^2 \sin [c + d x])}{3 (a^2 - b^2)^2} \right) \right) / (d \\
 & (e \cos [c + d x])^{5/2})
 \end{aligned}$$

Problem 593: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{1}{(e \cos [c + d x])^{7/2} (a + b \sin [c + d x])^2} dx$$

Optimal (type 4, 574 leaves, 15 steps):

$$\begin{aligned} & - \frac{9 a b^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2(-a^2+b^2)^{13/4} d e^{7/2}} + \frac{9 a b^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{2(-a^2+b^2)^{13/4} d e^{7/2}} - \\ & \frac{3(2 a^4 - 10 a^2 b^2 - 7 b^4) \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{5(a^2-b^2)^3 d e^4 \sqrt{\cos [c+d x]}} + \\ & \frac{9 a^2 b^3 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{2(a^2-b^2)^3 (b-\sqrt{-a^2+b^2}) d e^3 \sqrt{e \cos [c+d x]}} + \\ & \frac{9 a^2 b^3 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{2(a^2-b^2)^3 (b+\sqrt{-a^2+b^2}) d e^3 \sqrt{e \cos [c+d x]}} + \\ & \frac{b}{(a^2-b^2) d e (e \cos [c+d x])^{5/2} (a+b \sin [c+d x])} - \\ & \frac{9 a b - (2 a^2 + 7 b^2) \sin [c+d x]}{5(a^2-b^2)^2 d e (e \cos [c+d x])^{5/2}} + \frac{3(15 a b^3 + (2 a^4 - 10 a^2 b^2 - 7 b^4) \sin [c+d x])}{5(a^2-b^2)^3 d e^3 \sqrt{e \cos [c+d x]}} \end{aligned}$$

Result (type 6, 1343 leaves):

$$\begin{aligned} & - \frac{1}{10(a-b)^3 (a+b)^3 d (e \cos [c+d x])^{7/2}} \\ & 3 \cos [c+d x]^{7/2} \left(\frac{1}{12 \sqrt{1-\cos [c+d x]^2} (a+b \sin [c+d x])} \right. \\ & \quad \left. (2 a^5 - 10 a^3 b^2 - 22 a b^4) (a+b \sqrt{1-\cos [c+d x]^2}) \left(- \left(\left(56 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \right. \right. \right. \right. \right. \right. \\ & \quad \left. \left. \left. \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \cos [c+d x]^{3/2} \right) / \left(\sqrt{1-\cos [c+d x]^2} \right. \right. \right. \\ & \quad \left. \left. \left. \left(7 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] - \right. \right. \right. \right. \right. \\ & \quad \left. \left. \left. 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \right. \right. \right. \right. \right. \\ & \quad \left. \left. \left. (-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \right) \right) \right) \left. \right) \cos [c+d x]^2 \left(a^2+b^2 (-1+\cos [c+d x]^2) \right) \right) \right) - \end{aligned}$$

$$\begin{aligned}
 & \left((3 + 3i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+dx]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[\right. \right. \right. \\
 & \quad \left. \left. \left. 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+dx]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos [c+dx]} + i b \cos [c+dx] \right] + \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos [c+dx]} + i b \cos [c+dx] \right] \right) \right) / \left(\sqrt{b} (-a^2+b^2)^{1/4} \right) \sin [c+dx] - \\
 & \frac{1}{(1-\cos [c+dx]^2) (a+b \sin [c+dx])} 2 (2 a^4 b - 10 a^2 b^3 - 7 b^5) \\
 & \left(a + b \sqrt{1-\cos [c+dx]^2} \right) \\
 & \left(\left(7 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c+dx]^2, \frac{b^2 \cos [c+dx]^2}{-a^2+b^2} \right] \right. \right. \\
 & \quad \left. \left. \cos [c+dx]^{3/2} \sqrt{1-\cos [c+dx]^2} \right) \right) / \\
 & \left(3 \left(-7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c+dx]^2, \frac{b^2 \cos [c+dx]^2}{-a^2+b^2} \right] + 2 \right. \right. \\
 & \quad \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos [c+dx]^2, \frac{b^2 \cos [c+dx]^2}{-a^2+b^2} \right] + \right. \\
 & \quad \left. \left. (a^2-b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c+dx]^2, \frac{b^2 \cos [c+dx]^2}{-a^2+b^2} \right] \right) \right) \\
 & \quad \left. \cos [c+dx]^2 \right) (a^2+b^2 (-1+\cos [c+dx]^2)) \Big) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+dx]}}{(a^2-b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+dx]}}{(a^2-b^2)^{1/4}} \right] \right) + \right. \\
 & \quad \left. \operatorname{Log} \left[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [c+dx]} + b \cos [c+dx] \right] - \operatorname{Log} \left[\right. \right. \\
 & \quad \left. \left. \sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [c+dx]} + b \cos [c+dx] \right] \right) \Big) / \\
 & \left(4 \sqrt{2} b^{3/2} (a^2-b^2)^{1/4} \right) \sin [c+dx]^2 \Big) + \left(\cos [c+dx]^4 \right. \\
 & \left. \frac{b^5 \cos [c+dx]}{(a^2-b^2)^3 (a+b \sin [c+dx])} + \frac{2 \operatorname{Sec} [c+dx]^3 (-2 a b + a^2 \sin [c+dx] + b^2 \sin [c+dx])}{5 (a^2-b^2)^2} + \right. \\
 & \frac{1}{5 (a^2-b^2)^3} \\
 & 2 \\
 & \operatorname{Sec} [c+dx] \\
 & \left. (20 a b^3 + 3 a^4 \sin [c+dx] - 15 a^2 b^2 \sin [c+dx] - \right.
 \end{aligned}$$

$$8 b^4 \operatorname{Sin}[c+d x] \Big) \Big) \Big) / \left(d \left(e \operatorname{Cos}[c+d x] \right)^{7/2} \right)$$

Problem 594: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\left(e \operatorname{Cos}[c+d x] \right)^{13/2}}{\left(a+b \operatorname{Sin}[c+d x] \right)^3} dx$$

Optimal (type 4, 575 leaves, 15 steps):

$$\begin{aligned} & \frac{11 \left(9 a^4 - 11 a^2 b^2 + 2 b^4 \right) e^{13/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \operatorname{Cos}[c+d x]}}{\left(-a^2+b^2 \right)^{1/4} \sqrt{e}} \right]}{8 b^{13/2} \left(-a^2+b^2 \right)^{1/4} d} + \\ & \frac{11 \left(9 a^4 - 11 a^2 b^2 + 2 b^4 \right) e^{13/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \operatorname{Cos}[c+d x]}}{\left(-a^2+b^2 \right)^{1/4} \sqrt{e}} \right]}{8 b^{13/2} \left(-a^2+b^2 \right)^{1/4} d} + \\ & \frac{11 a \left(45 a^2 - 37 b^2 \right) e^6 \sqrt{e \operatorname{Cos}[c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), 2 \right]}{20 b^6 d \sqrt{\operatorname{Cos}[c+d x]}} - \\ & \left(\frac{11 a \left(9 a^4 - 11 a^2 b^2 + 2 b^4 \right) e^7 \sqrt{\operatorname{Cos}[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right]}{8 b^7 \left(b - \sqrt{-a^2+b^2} \right) d \sqrt{e \operatorname{Cos}[c+d x]}} \right) / \\ & \left(\frac{11 a \left(9 a^4 - 11 a^2 b^2 + 2 b^4 \right) e^7 \sqrt{\operatorname{Cos}[c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right]}{8 b^7 \left(b + \sqrt{-a^2+b^2} \right) d \sqrt{e \operatorname{Cos}[c+d x]}} \right) - \\ & \frac{e \left(e \operatorname{Cos}[c+d x] \right)^{11/2}}{2 b d \left(a+b \operatorname{Sin}[c+d x] \right)^2} - \frac{11 e^3 \left(e \operatorname{Cos}[c+d x] \right)^{7/2} \left(9 a+2 b \operatorname{Sin}[c+d x] \right)}{28 b^3 d \left(a+b \operatorname{Sin}[c+d x] \right)} + \\ & \frac{11 e^5 \left(e \operatorname{Cos}[c+d x] \right)^{3/2} \left(5 \left(9 a^2 - 2 b^2 \right) - 27 a b \operatorname{Sin}[c+d x] \right)}{60 b^5 d} \end{aligned}$$

Result (type 6, 1326 leaves):

$$\begin{aligned} & \frac{1}{40 b^5 d \operatorname{Cos}[c+d x]^{13/2}} 11 \left(e \operatorname{Cos}[c+d x] \right)^{13/2} \\ & \left(\frac{1}{12 \sqrt{1 - \operatorname{Cos}[c+d x]^2} \left(a+b \operatorname{Sin}[c+d x] \right)} \left(18 a^2 b - 10 b^3 \right) \left(a+b \sqrt{1 - \operatorname{Cos}[c+d x]^2} \right) \right. \\ & \left. - \left(\left(56 a \left(a^2 - b^2 \right) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \operatorname{Cos}[c+d x]^2, \frac{b^2 \operatorname{Cos}[c+d x]^2}{-a^2+b^2} \right] \operatorname{Cos}[c+d x]^{3/2} \right) / \right. \right. \\ & \left. \left. \left(\sqrt{1 - \operatorname{Cos}[c+d x]^2} \left(7 \left(a^2 - b^2 \right) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \operatorname{Cos}[c+d x]^2, \right. \right. \right. \right. \right. \right. \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right) - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \cos [c+d x]^2 \right) (a^2+b^2 (-1+\cos [c+d x]^2)) \Big) - \\
 & \left((3+3 i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[\right. \right. \right. \\
 & \left. \left. 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \\
 & \left. \left. \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] + \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} \right. \right. \\
 & \left. \left. (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] \right) \Big) / \left(\sqrt{b} (-a^2+b^2)^{1/4} \right) \\
 & \sin [c+d x] - \frac{1}{(1-\cos [c+d x]^2)(a+b \sin [c+d x])} 2(45 a^3-37 a b^2) \\
 & \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \\
 & \left(\left(7 b\left(a^2-b^2\right) \operatorname{AppellF1} \left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right. \right. \\
 & \left. \left. \cos [c+d x]^{3 / 2} \sqrt{1-\cos [c+d x]^2} \right) \Big) / \right. \\
 & \left(3 \left(-7\left(a^2-b^2\right) \operatorname{AppellF1} \left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
 & \left. \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4},-\frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
 & \left. \left. \left(a^2-b^2\right) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \right) \\
 & \left. \cos [c+d x]^2\right)\left(a^2+b^2(-1+\cos [c+d x]^2)\right) \Big) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1 / 4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1 / 4}} \right] \right) + \right. \\
 & \left. \operatorname{Log} \left[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} \left(a^2-b^2\right)^{1 / 4} \sqrt{\cos [c+d x]} + b \cos [c+d x] \right] - \right. \\
 & \left. \operatorname{Log} \left[\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} \left(a^2-b^2\right)^{1 / 4} \sqrt{\cos [c+d x]} + b \cos [c+d x] \right] \right) \Big) / \right. \\
 & \left. \left(4 \sqrt{2} b^{3 / 2} \left(a^2-b^2\right)^{1 / 4} \right) \sin [c+d x]^2 \right) + \frac{1}{d} \\
 & \left(e \cos [c+d x] \right)^{13 / 2} \sec [c+d x]^6 \left(-\frac{\left(-168 a^2+65 b^2\right) \cos [c+d x]}{42 b^5} - \right.
 \end{aligned}$$

$$\frac{\cos[3(c+dx)]}{14b^3} + \frac{-a^4 \cos[c+dx] + 2a^2b^2 \cos[c+dx] - b^4 \cos[c+dx]}{2b^5(a+b \sin[c+dx])^2} + \frac{19(a^3 \cos[c+dx] - ab^2 \cos[c+dx])}{4b^5(a+b \sin[c+dx])} - \frac{3a \sin[2(c+dx)]}{5b^4}$$

Problem 595: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c+dx])^{11/2}}{(a+b \sin[c+dx])^3} dx$$

Optimal (type 4, 589 leaves, 15 steps):

$$\frac{9(7a^4 - 9a^2b^2 + 2b^4) e^{11/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos[c+dx]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8b^{11/2} (-a^2+b^2)^{3/4} d} + \frac{9(7a^4 - 9a^2b^2 + 2b^4) e^{11/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos[c+dx]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8b^{11/2} (-a^2+b^2)^{3/4} d} + \frac{3a(21a^2 - 13b^2) e^6 \sqrt{\cos[c+dx]} \operatorname{EllipticF}\left[\frac{1}{2}(c+dx), 2\right]}{4b^6 d \sqrt{e \cos[c+dx]}} - \left(9a(7a^4 - 9a^2b^2 + 2b^4) e^6 \sqrt{\cos[c+dx]} \operatorname{EllipticPi}\left[\frac{2b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2}(c+dx), 2\right]\right) / \left(8b^6(a^2 - b(b - \sqrt{-a^2+b^2})) d \sqrt{e \cos[c+dx]}\right) - \left(9a(7a^4 - 9a^2b^2 + 2b^4) e^6 \sqrt{\cos[c+dx]} \operatorname{EllipticPi}\left[\frac{2b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2}(c+dx), 2\right]\right) / \left(8b^6(a^2 - b(b + \sqrt{-a^2+b^2})) d \sqrt{e \cos[c+dx]}\right) - \frac{e(e \cos[c+dx])^{9/2}}{2bd(a+b \sin[c+dx])^2} - \frac{9e^3(e \cos[c+dx])^{5/2}(7a+2b \sin[c+dx])}{20b^3d(a+b \sin[c+dx])} + \frac{3e^5 \sqrt{e \cos[c+dx]}(3(7a^2 - 2b^2) - 7ab \sin[c+dx])}{4b^5d}$$

Result (type 6, 2224 leaves):

$$\frac{1}{d} (e \cos[c+dx])^{11/2} \sec[c+dx]^5$$

$$\begin{aligned}
 & \left(-\frac{\cos[2(c+dx)]}{5b^3} - \frac{2a \sin[c+dx]}{b^4} - \frac{(-a^2+b^2)^2}{2b^5(a+b \sin[c+dx])^2} + \frac{17a(a^2-b^2)}{4b^5(a+b \sin[c+dx])} \right) + \\
 & \frac{1}{40b^5 d \cos[c+dx]^{11/2}} 3 (e \cos[c+dx])^{11/2} \\
 & \left(-\frac{1}{\sqrt{1-\cos[c+dx]^2} (a+b \sin[c+dx])} 2 (30a^2b - 16b^3) (a+b \sqrt{1-\cos[c+dx]^2}) \right. \\
 & \left. \left(\left(5a(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2}\right] \sqrt{\cos[c+dx]} \right) / \right. \right. \\
 & \left. \left(\sqrt{1-\cos[c+dx]^2} \right. \right. \\
 & \left. \left(5(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2}\right] - 2 \right. \right. \\
 & \left. \left(2b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2}\right] + (-a^2+b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2}\right] \right) \cos[c+dx]^2 \right) \\
 & \left. (a^2+b^2(-1+\cos[c+dx]^2)) \right) - \frac{1}{(-a^2+b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
 & \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i)\sqrt{b}\sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i)\sqrt{b}\sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}}\right] \right) + \\
 & \left. \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i)\sqrt{b}(-a^2+b^2)^{1/4}\sqrt{\cos[c+dx]} + ib \cos[c+dx]\right] - \right. \\
 & \left. \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i)\sqrt{b}(-a^2+b^2)^{1/4}\sqrt{\cos[c+dx]} + ib \cos[c+dx]\right] \right) \Bigg) \\
 & \sin[c+dx] + \frac{1}{\sqrt{1-\cos[c+dx]^2} (-1+2\cos[c+dx]^2) (a+b \sin[c+dx])} \\
 & (40a^2b - 14b^3) (a+b \sqrt{1-\cos[c+dx]^2}) \cos[2(c+dx)] \\
 & \left(\frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2a^2+b^2) \operatorname{ArcTan}\left[1 - \frac{(1+i)\sqrt{b}\sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}}\right]}{b^{3/2} (-a^2+b^2)^{3/4}} - \right. \\
 & \left. \frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2a^2+b^2) \operatorname{ArcTan}\left[1 + \frac{(1+i)\sqrt{b}\sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}}\right]}{b^{3/2} (-a^2+b^2)^{3/4}} + \frac{4\sqrt{\cos[c+dx]}}{b} + \right. \\
 & \left. \left(10a(a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2}\right] \sqrt{\cos[c+dx]} \right) / \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(\sqrt{1 - \cos [c + d x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c + d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c + d x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \cos [c + d x]^2 \left(a^2 + b^2 (-1 + \cos [c + d x]^2) \right) \Big) - \\
 & \left(36 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right. \\
 & \quad \left. \cos [c + d x]^{5/2} \right) / \left(5 \sqrt{1 - \cos [c + d x]^2} \right. \\
 & \quad \left(9 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] - \right. \\
 & \quad \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \cos [c + d x]^2 \right) \\
 & \quad \left(a^2 + b^2 (-1 + \cos [c + d x]^2) \right) \Big) + \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[\sqrt{-a^2 + b^2} - \right. \right. \\
 & \quad \left. \left. (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [c + d x]} + i b \cos [c + d x] \right] \right) / \left(b^{3/2} (-a^2 + b^2)^{3/4} \right) - \\
 & \quad \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [c + d x]} + \right. \right. \\
 & \quad \left. \left. i b \cos [c + d x] \right] \right) / \left(b^{3/2} (-a^2 + b^2)^{3/4} \right) \Big) \sin [c + d x] - \\
 & \frac{1}{(1 - \cos [c + d x]^2) (a + b \sin [c + d x])} 2 (25 a^3 - 37 a b^2) \left(a + b \sqrt{1 - \cos [c + d x]^2} \right) \\
 & \quad \left(\left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\
 & \quad \left. \left. \sqrt{\cos [c + d x]} \sqrt{1 - \cos [c + d x]^2} \right) \right) / \\
 & \quad \left(\left(-5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \quad \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\
 & \quad \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \right) \\
 & \quad \left. \cos [c + d x]^2 \left(a^2 + b^2 (-1 + \cos [c + d x]^2) \right) \right) +
 \end{aligned}$$

$$\left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{(a^2 - b^2)^{1/4}} \right] - \right. \right. \\ \left. \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c+d x]} + b \cos [c+d x] \right] + \right. \right. \\ \left. \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c+d x]} + b \cos [c+d x] \right] \right) \right) / \\ \left(4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \operatorname{Sin} [c+d x]^2 \Bigg)$$

Problem 596: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c+d x])^{9/2}}{(a+b \sin [c+d x])^3} dx$$

Optimal (type 4, 483 leaves, 14 steps):

$$\frac{7 (5 a^2 - 2 b^2) e^{9/2} \operatorname{ArcTan} \left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{8 b^{9/2} (-a^2 + b^2)^{1/4} d} - \\ \frac{7 (5 a^2 - 2 b^2) e^{9/2} \operatorname{ArcTanh} \left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{8 b^{9/2} (-a^2 + b^2)^{1/4} d} - \frac{35 a e^4 \sqrt{e \cos [c+d x]} \operatorname{EllipticE} \left[\frac{1}{2} (c+d x), 2 \right]}{4 b^4 d \sqrt{\cos [c+d x]}} + \\ \left(7 a (5 a^2 - 2 b^2) e^5 \sqrt{\cos [c+d x]} \operatorname{EllipticPi} \left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c+d x), 2 \right] \right) / \\ \left(8 b^5 (b - \sqrt{-a^2 + b^2}) d \sqrt{e \cos [c+d x]} \right) + \\ \left(7 a (5 a^2 - 2 b^2) e^5 \sqrt{\cos [c+d x]} \operatorname{EllipticPi} \left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c+d x), 2 \right] \right) / \\ \left(8 b^5 (b + \sqrt{-a^2 + b^2}) d \sqrt{e \cos [c+d x]} \right) - \\ \frac{e (e \cos [c+d x])^{7/2}}{2 b d (a+b \sin [c+d x])^2} - \frac{7 e^3 (e \cos [c+d x])^{3/2} (5 a + 2 b \sin [c+d x])}{12 b^3 d (a+b \sin [c+d x])}$$

Result (type 6, 1231 leaves):

$$\frac{1}{d} (e \cos [c+d x])^{9/2} \operatorname{Sec} [c+d x]^4 \\ \left(-\frac{2 \cos [c+d x]}{3 b^3} + \frac{a^2 \cos [c+d x] - b^2 \cos [c+d x]}{2 b^3 (a+b \sin [c+d x])^2} - \frac{11 a \cos [c+d x]}{4 b^3 (a+b \sin [c+d x])} \right) - \\ \frac{1}{8 b^3 d \cos [c+d x]^{9/2}} 7 (e \cos [c+d x])^{9/2}$$

$$\begin{aligned}
 & \left(\frac{1}{6 \sqrt{1 - \cos [c + d x]^2} (a + b \sin [c + d x])} b \left(a + b \sqrt{1 - \cos [c + d x]^2} \right) \right. \\
 & \left. - \left(\left(56 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \cos [c + d x]^{3/2} \right) / \right. \right. \\
 & \quad \left(\sqrt{1 - \cos [c + d x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \right. \right. \right. \\
 & \quad \quad \left. \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c + d x]^2, \right. \right. \\
 & \quad \quad \left. \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c + d x]^2, \right. \\
 & \quad \quad \left. \left. \left. \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \cos [c + d x]^2 \left(a^2 + b^2 (-1 + \cos [c + d x]^2) \right) \right) \right) - \\
 & \quad \left((3 + 3 i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[\right. \right. \right. \\
 & \quad \left. \left. 1 + \frac{(1 + i) \sqrt{b} \sqrt{\cos [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2 + b^2} - (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \\
 & \quad \left. \left. \sqrt{\cos [c + d x]} + i b \cos [c + d x] \right] + \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \\
 & \quad \left. \left. \left. \left. \sqrt{\cos [c + d x]} + i b \cos [c + d x] \right] \right) \right) / \left(\sqrt{b} (-a^2 + b^2)^{1/4} \right) \right) \sin [c + d x] - \\
 & \frac{1}{(1 - \cos [c + d x]^2) (a + b \sin [c + d x])} 10 a \left(a + b \sqrt{1 - \cos [c + d x]^2} \right) \\
 & \left(\left(7 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\
 & \quad \left. \left. \cos [c + d x]^{3/2} \sqrt{1 - \cos [c + d x]^2} \right) / \right. \\
 & \quad \left(3 \left(-7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \quad \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \quad \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \right) \\
 & \quad \left. \cos [c + d x]^2 \left(a^2 + b^2 (-1 + \cos [c + d x]^2) \right) \right) + \\
 & \quad \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] + \right. \right. \\
 & \quad \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] - \right. \\
 & \quad \left. \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] \right) \right) / \right)
 \end{aligned}$$

$$\left(4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \left(\sin [c + d x]^2 \right)$$

Problem 597: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{7/2}}{(a + b \sin [c + d x])^3} dx$$

Optimal (type 4, 497 leaves, 14 steps):

$$\begin{aligned} & \frac{5 (3 a^2 - 2 b^2) e^{7/2} \operatorname{ArcTan} \left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{8 b^{7/2} (-a^2 + b^2)^{3/4} d} - \\ & \frac{5 (3 a^2 - 2 b^2) e^{7/2} \operatorname{ArcTanh} \left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{8 b^{7/2} (-a^2 + b^2)^{3/4} d} - \frac{15 a e^4 \sqrt{\cos [c + d x]} \operatorname{EllipticF} \left[\frac{1}{2} (c + d x), 2 \right]}{4 b^4 d \sqrt{e \cos [c + d x]}} + \\ & \left(5 a (3 a^2 - 2 b^2) e^4 \sqrt{\cos [c + d x]} \operatorname{EllipticPi} \left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right] \right) / \\ & \left(8 b^4 \left(a^2 - b \left(b - \sqrt{-a^2 + b^2} \right) \right) d \sqrt{e \cos [c + d x]} \right) + \\ & \left(5 a (3 a^2 - 2 b^2) e^4 \sqrt{\cos [c + d x]} \operatorname{EllipticPi} \left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right] \right) / \\ & \left(8 b^4 \left(a^2 - b \left(b + \sqrt{-a^2 + b^2} \right) \right) d \sqrt{e \cos [c + d x]} \right) - \\ & \frac{e (e \cos [c + d x])^{5/2}}{2 b d (a + b \sin [c + d x])^2} - \frac{5 e^3 \sqrt{e \cos [c + d x]} (3 a + 2 b \sin [c + d x])}{4 b^3 d (a + b \sin [c + d x])} \end{aligned}$$

Result (type 6, 2154 leaves):

$$\begin{aligned} & \frac{(e \cos [c + d x])^{7/2} \operatorname{Sec} [c + d x]^3 \left(\frac{a^2 - b^2}{2 b^3 (a + b \sin [c + d x])^2} - \frac{9 a}{4 b^3 (a + b \sin [c + d x])} \right)}{d} - \\ & \frac{1}{8 b^3 d \cos [c + d x]^{7/2}} (e \cos [c + d x])^{7/2} \left(- \frac{1}{\sqrt{1 - \cos [c + d x]^2} (a + b \sin [c + d x])} \right. \\ & \left. 12 b \left(a + b \sqrt{1 - \cos [c + d x]^2} \right) \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \right. \\ & \left. \left. \left. \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \sqrt{\cos [c + d x]} \right) / \left(\sqrt{1 - \cos [c + d x]^2} \right. \right. \\ & \left. \left. \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] - 2 \right) \right) \right) \end{aligned}$$

$$\begin{aligned}
 & \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + (-a^2+b^2) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \cos [c+d x]^2 \\
 & \quad \left. (a^2+b^2(-1+\cos [c+d x]^2))\right) - \frac{1}{(-a^2+b^2)^{3/4}}\left(\frac{1}{8}-\frac{i}{8}\right) \sqrt{b} \\
 & \quad \left(2 \operatorname{ArcTan}\left[1-\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1+\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}}\right] \right) + \\
 & \quad \left(\operatorname{Log}\left[\sqrt{-a^2+b^2}-(1+i) \sqrt{b}(-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]}+i b \cos [c+d x]\right] - \right. \\
 & \quad \left. \operatorname{Log}\left[\sqrt{-a^2+b^2}+(1+i) \sqrt{b}(-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]}+i b \cos [c+d x]\right] \right) \\
 & \quad \sin [c+d x] + \frac{1}{\sqrt{1-\cos [c+d x]^2}(-1+2 \cos [c+d x]^2)(a+b \sin [c+d x])} \\
 4 b & \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \cos [2(c+d x)] \\
 & \quad \left(\frac{\left(\frac{1}{2}-\frac{i}{2}\right)\left(-2 a^2+b^2\right) \operatorname{ArcTan}\left[1-\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}}\right]}{b^{3/2}\left(-a^2+b^2\right)^{3/4}} - \right. \\
 & \quad \left. \frac{\left(\frac{1}{2}-\frac{i}{2}\right)\left(-2 a^2+b^2\right) \operatorname{ArcTan}\left[1+\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}}\right]}{b^{3/2}\left(-a^2+b^2\right)^{3/4}} + \frac{4 \sqrt{\cos [c+d x]}}{b} + \right. \\
 & \quad \left. \left(10 a\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \sqrt{\cos [c+d x]} \right) \right) / \\
 & \quad \left(\sqrt{1-\cos [c+d x]^2} \left(5\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] - 2\left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \left(-a^2+b^2\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \cos [c+d x]^2 \left. \right) \left. \left(a^2+b^2(-1+\cos [c+d x]^2) \right) \right) - \\
 & \quad \left(36 a\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right. \\
 & \quad \left. \cos [c+d x]^{5/2} \right) / \left(5 \sqrt{1-\cos [c+d x]^2} \right. \\
 & \quad \left(9\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] - \right. \\
 & \quad \left. 2\left(2 b^2 \operatorname{AppellF1}\left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \left(-a^2+b^2\right) \right) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left. \text{AppellF1}\left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2}\right] \cos[c+dx]^2 \right. \\
 & \left. (a^2+b^2(-1+\cos[c+dx]^2))\right) + \left(\left(\frac{1}{4}-\frac{i}{4}\right)(-2a^2+b^2) \log\left[\sqrt{-a^2+b^2}-\right.\right. \\
 & \left.\left.(1+i)\sqrt{b}(-a^2+b^2)^{1/4}\sqrt{\cos[c+dx]}+ib\cos[c+dx]\right]\right) / \left(b^{3/2}(-a^2+b^2)^{3/4}-\right. \\
 & \left.\left(\left(\frac{1}{4}-\frac{i}{4}\right)(-2a^2+b^2) \log\left[\sqrt{-a^2+b^2}+(1+i)\sqrt{b}(-a^2+b^2)^{1/4}\sqrt{\cos[c+dx]}+\right.\right.\right. \\
 & \left.\left.\left. ib\cos[c+dx]\right]\right) / \left(b^{3/2}(-a^2+b^2)^{3/4}\right)\right) \sin[c+dx] - \\
 & \frac{1}{(1-\cos[c+dx]^2)(a+b\sin[c+dx])} 14a\left(a+b\sqrt{1-\cos[c+dx]^2}\right) \\
 & \left(\left(5b(a^2-b^2) \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2}\right] \right.\right. \\
 & \left.\left.\sqrt{\cos[c+dx]}\sqrt{1-\cos[c+dx]^2}\right) / \right. \\
 & \left(\left(-5(a^2-b^2) \text{AppellF1}\left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2}\right] +\right.\right. \\
 & \left.2\left(2b^2 \text{AppellF1}\left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2}\right] +\right.\right. \\
 & \left.\left.(a^2-b^2) \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2}\right]\right) \right. \\
 & \left.\cos[c+dx]^2(a^2+b^2(-1+\cos[c+dx]^2))\right) + \\
 & \left(a\left(-2 \operatorname{ArcTan}\left[1-\frac{\sqrt{2}\sqrt{b}\sqrt{\cos[c+dx]}}{(a^2-b^2)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1+\frac{\sqrt{2}\sqrt{b}\sqrt{\cos[c+dx]}}{(a^2-b^2)^{1/4}}\right] -\right.\right. \\
 & \left.\log\left[\sqrt{a^2-b^2}-\sqrt{2}\sqrt{b}(a^2-b^2)^{1/4}\sqrt{\cos[c+dx]}+b\cos[c+dx]\right] +\right. \\
 & \left.\log\left[\sqrt{a^2-b^2}+\sqrt{2}\sqrt{b}(a^2-b^2)^{1/4}\sqrt{\cos[c+dx]}+b\cos[c+dx]\right]\right) / \right. \\
 & \left.\left(4\sqrt{2}\sqrt{b}(a^2-b^2)^{3/4}\right)\right) \sin[c+dx]^2 \Bigg)
 \end{aligned}$$

Problem 598: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c+dx])^{5/2}}{(a+b \sin[c+dx])^3} dx$$

Optimal (type 4, 505 leaves, 14 steps):

$$\frac{3 (a^2 - 2 b^2) e^{5/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 b^{5/2} (-a^2+b^2)^{5/4} d} -$$

$$\frac{3 (a^2 - 2 b^2) e^{5/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 b^{5/2} (-a^2+b^2)^{5/4} d} + \frac{3 a e^2 \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), 2\right]}{4 b^2 (a^2 - b^2) d \sqrt{\cos [c+d x]}} -$$

$$\left(3 a (a^2 - 2 b^2) e^3 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]\right) /$$

$$\left(8 b^3 (a^2 - b^2) (b - \sqrt{-a^2+b^2}) d \sqrt{e \cos [c+d x]}\right) -$$

$$\left(3 a (a^2 - 2 b^2) e^3 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]\right) /$$

$$\left(8 b^3 (a^2 - b^2) (b + \sqrt{-a^2+b^2}) d \sqrt{e \cos [c+d x]}\right) -$$

$$\frac{e (e \cos [c+d x])^{3/2}}{2 b d (a+b \sin [c+d x])^2} + \frac{3 a e (e \cos [c+d x])^{3/2}}{4 b (a^2 - b^2) d (a+b \sin [c+d x])}$$

Result (type 6, 1225 leaves):

$$\frac{1}{d} (e \cos [c+d x])^{5/2} \operatorname{Sec}[c+d x]^2 \left(-\frac{\cos [c+d x]}{2 b (a+b \sin [c+d x])^2} - \frac{3 a \cos [c+d x]}{4 b (-a^2+b^2) (a+b \sin [c+d x])}\right) +$$

$$\frac{1}{8 (a-b) b (a+b) d \cos [c+d x]^{5/2}}$$

$$3 (e \cos [c+d x])^{5/2} \left(\frac{1}{6 \sqrt{1 - \cos [c+d x]^2} (a+b \sin [c+d x])} b (a+b \sqrt{1 - \cos [c+d x]^2})\right.$$

$$\left(-\left(\left(56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \cos [c+d x]^{3/2}\right) / \right.\right.$$

$$\left(\sqrt{1 - \cos [c+d x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + (-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]\right) \cos [c+d x]^2\right) (a^2 + b^2 (-1 + \cos [c+d x]^2))\right) \right) -$$

$$\left((3 + 3 i) \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}}\right] - \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4}\right]\right)\right)$$

$$\begin{aligned}
 & \left(\sqrt{\cos [c+d x]} + i b \cos [c+d x] \right) + \log \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \\
 & \left. \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] \Bigg) / \left(\sqrt{b} (-a^2+b^2)^{1/4} \right) \sin [c+d x] - \\
 & \frac{1}{(1-\cos [c+d x]^2) (a+b \sin [c+d x])} 2 a \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \\
 & \left(\left(7 b \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right. \right. \\
 & \left. \left. \cos [c+d x]^{3/2} \sqrt{1-\cos [c+d x]^2} \right) \Bigg) / \right. \\
 & \left(3 \left(-7 \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
 & \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \right. \\
 & \left. \left. \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \right) \\
 & \left. \cos [c+d x]^2 \right) \left(a^2+b^2 \left(-1+\cos [c+d x]^2 \right) \right) \Bigg) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2 \right)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2 \right)^{1/4}} \right] \right) + \right. \\
 & \left. \log \left[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} \left(a^2-b^2 \right)^{1/4} \sqrt{\cos [c+d x]} + b \cos [c+d x] \right] - \right. \\
 & \left. \log \left[\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} \left(a^2-b^2 \right)^{1/4} \sqrt{\cos [c+d x]} + b \cos [c+d x] \right] \right) \Bigg) / \\
 & \left(4 \sqrt{2} b^{3/2} \left(a^2-b^2 \right)^{1/4} \right) \sin [c+d x]^2 \Bigg)
 \end{aligned}$$

Problem 599: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c+d x])^{3/2}}{(a+b \sin [c+d x])^3} dx$$

Optimal (type 4, 519 leaves, 14 steps):

$$\frac{(a^2 + 2 b^2) e^{3/2} \text{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 b^{3/2} (-a^2 + b^2)^{7/4} d} +$$

$$\frac{(a^2 + 2 b^2) e^{3/2} \text{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 b^{3/2} (-a^2 + b^2)^{7/4} d} - \frac{a e^2 \sqrt{\cos [c+d x]} \text{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{4 b^2 (a^2 - b^2) d \sqrt{e \cos [c+d x]}} +$$

$$\frac{a (a^2 + 2 b^2) e^2 \sqrt{\cos [c+d x]} \text{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{8 b^2 (a^2 - b^2) (a^2 - b (b - \sqrt{-a^2+b^2})) d \sqrt{e \cos [c+d x]}} +$$

$$\frac{a (a^2 + 2 b^2) e^2 \sqrt{\cos [c+d x]} \text{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{8 b^2 (a^2 - b^2) (a^2 - b (b + \sqrt{-a^2+b^2})) d \sqrt{e \cos [c+d x]}} -$$

$$\frac{e \sqrt{e \cos [c+d x]}}{2 b d (a + b \sin [c+d x])^2} + \frac{a e \sqrt{e \cos [c+d x]}}{4 b (a^2 - b^2) d (a + b \sin [c+d x])}$$

Result (type 6, 1211 leaves):

$$\frac{1}{d} (e \cos [c+d x])^{3/2} \text{Sec}[c+d x] \left(-\frac{1}{2 b (a + b \sin [c+d x])^2} - \frac{a}{4 b (-a^2 + b^2) (a + b \sin [c+d x])} \right) -$$

$$\frac{1}{8 (a - b) b (a + b) d \cos [c+d x]^{3/2}}$$

$$(e \cos [c+d x])^{3/2} \left(\frac{1}{\sqrt{1 - \cos [c+d x]^2} (a + b \sin [c+d x])} - 4 b (a + b \sqrt{1 - \cos [c+d x]^2}) \right)$$

$$\left(\left(5 a (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2}\right] \sqrt{\cos [c+d x]} \right) / \right.$$

$$\left(\sqrt{1 - \cos [c+d x]^2} \left(5 (a^2 - b^2) \text{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2}\right] - 2 \left(2 b^2 \text{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \text{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2}\right] \right) \cos [c+d x]^2 \right) (a^2 + b^2 (-1 + \cos [c+d x]^2)) \right) \right) -$$

$$\frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \left(2 \text{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2 + b^2)^{1/4}}\right] - \right.$$

$$\left. 2 \text{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2 + b^2)^{1/4}}\right] \right) +$$

$$\text{Log}\left[\sqrt{-a^2 + b^2} - (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x]\right] -$$

$$\begin{aligned} & \left. \left(\log \left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [c + d x]} + i b \cos [c + d x] \right] \right) \right) \\ & \sin [c + d x] - \frac{1}{(1 - \cos [c + d x]^2) (a + b \sin [c + d x])} 2 a (a + b \sqrt{1 - \cos [c + d x]^2}) \\ & \left(\left(5 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\ & \left. \left. \sqrt{\cos [c + d x]} \sqrt{1 - \cos [c + d x]^2} \right) \right) / \\ & \left(\left(-5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\ & \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \right. \\ & \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \right) \\ & \left. \cos [c + d x]^2 (a^2 + b^2 (-1 + \cos [c + d x]^2)) \right) + \\ & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] \right) - \right. \\ & \left. \log \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] + \right. \\ & \left. \log \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] \right) \right) / \\ & \left(4 \sqrt{2} \sqrt{b} (a^2 - b^2)^{3/4} \right) \sin [c + d x]^2 \end{aligned}$$

Problem 600: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\sqrt{e \cos [c + d x]}}{(a + b \sin [c + d x])^3} dx$$

Optimal (type 4, 514 leaves, 14 steps):

$$\frac{(3 a^2 + 2 b^2) \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 \sqrt{b} (-a^2+b^2)^{9/4} d} -$$

$$\frac{(3 a^2 + 2 b^2) \sqrt{e} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 \sqrt{b} (-a^2+b^2)^{9/4} d} + \frac{5 a \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{4 (a^2-b^2)^2 d \sqrt{\cos [c+d x]}} +$$

$$\frac{a (3 a^2 + 2 b^2) e \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{8 b (a^2-b^2)^2 (b-\sqrt{-a^2+b^2}) d \sqrt{e \cos [c+d x]}} +$$

$$\frac{a (3 a^2 + 2 b^2) e \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{8 b (a^2-b^2)^2 (b+\sqrt{-a^2+b^2}) d \sqrt{e \cos [c+d x]}} +$$

$$\frac{b (e \cos [c+d x])^{3/2}}{2 (a^2-b^2) d e (a+b \sin [c+d x])^2} + \frac{5 a b (e \cos [c+d x])^{3/2}}{4 (a^2-b^2)^2 d e (a+b \sin [c+d x])}$$

Result (type 6, 1232 leaves):

$$\frac{\sqrt{e \cos [c+d x]} \left(\frac{b \cos [c+d x]}{2 (a^2-b^2) (a+b \sin [c+d x])^2} + \frac{5 a b \cos [c+d x]}{4 (a^2-b^2)^2 (a+b \sin [c+d x])} \right)}{d} +$$

$$\frac{1}{8 (a-b)^2 (a+b)^2 d \sqrt{\cos [c+d x]}} \sqrt{e \cos [c+d x]}$$

$$\left(\frac{1}{12 \sqrt{1-\cos [c+d x]^2} (a+b \sin [c+d x])} (8 a^2 + 2 b^2) \left(a + b \sqrt{1-\cos [c+d x]^2} \right) \right.$$

$$\left. - \left(\left(\left(56 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \cos [c+d x]^{3/2} \right) \right) / \right. \right.$$

$$\left. \left(\sqrt{1-\cos [c+d x]^2} \left(7 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + (-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \cos [c+d x]^2 \right) \right) \right) \left(a^2 + b^2 (-1 + \cos [c+d x]^2) \right) \right) -$$

$$\left((3+3 i) \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}}\right] - \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x]\right] + \operatorname{Log}\left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x]\right] \right) \right)$$

$$\begin{aligned}
 & \left. \left. \left. \left. \left. \sqrt{\cos [c+d x]}+i b \cos [c+d x]\right)\right)\right)\right)\right)\left/\left(\sqrt{b}\left(-a^2+b^2\right)^{1 / 4}\right)\right) \sin [c+d x]- \\
 & \frac{1}{\left(1-\cos [c+d x]^2\right)\left(a+b \sin [c+d x]\right)} 10 a b\left(a+b \sqrt{1-\cos [c+d x]^2}\right) \\
 & \left(\left(7 b\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]\right.\right. \\
 & \left.\left.\cos [c+d x]^{3 / 2} \sqrt{1-\cos [c+d x]^2}\right)\right)\left/\right. \\
 & \left(3\left(-7\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]+2\left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4},-\frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]+(a^2-b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]\right)\right)\right. \\
 & \left.\cos [c+d x]^2\right)\left(a^2+b^2\left(-1+\cos [c+d x]^2\right)\right)\right)+ \\
 & \left(a\left(-2 \operatorname{ArcTan}\left[1-\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1 / 4}}\right]+2 \operatorname{ArcTan}\left[1+\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1 / 4}}\right]\right)+\right. \\
 & \left.\log \left[\sqrt{a^2-b^2}-\sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{1 / 4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right]-\right. \\
 & \left.\log \left[\sqrt{a^2-b^2}+\sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{1 / 4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right]\right)\right)\left/\right. \\
 & \left.\left(4 \sqrt{2} b^{3 / 2}\left(a^2-b^2\right)^{1 / 4}\right)\right) \sin [c+d x]^2\right)
 \end{aligned}$$

Problem 601: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{e \cos [c+d x]}\left(a+b \sin [c+d x]\right)^3} d x$$

Optimal (type 4, 520 leaves, 14 steps):

$$\begin{aligned}
 & - \frac{3 \sqrt{b} (5 a^2 + 2 b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2\right)^{1 / 4} \sqrt{e}}\right]}{8\left(-a^2+b^2\right)^{11 / 4} d \sqrt{e}} - \\
 & \frac{3 \sqrt{b} (5 a^2 + 2 b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2\right)^{1 / 4} \sqrt{e}}\right]}{8\left(-a^2+b^2\right)^{11 / 4} d \sqrt{e}} - \frac{7 a \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{4\left(a^2-b^2\right)^2 d \sqrt{e \cos [c+d x]}} + \\
 & \frac{3 a\left(5 a^2+2 b^2\right) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{8\left(a^2-b^2\right)^2\left(a^2-b\left(b-\sqrt{-a^2+b^2}\right)\right) d \sqrt{e \cos [c+d x]}} + \\
 & \frac{3 a\left(5 a^2+2 b^2\right) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{8\left(a^2-b^2\right)^2\left(a^2-b\left(b+\sqrt{-a^2+b^2}\right)\right) d \sqrt{e \cos [c+d x]}} + \\
 & \frac{b \sqrt{e \cos [c+d x]}}{2\left(a^2-b^2\right) d e\left(a+b \sin [c+d x]\right)^2} + \frac{7 a b \sqrt{e \cos [c+d x]}}{4\left(a^2-b^2\right)^2 d e\left(a+b \sin [c+d x]\right)}
 \end{aligned}$$

Result (type 6, 1226 leaves):

$$\begin{aligned}
 & \frac{\cos [c+d x]\left(\frac{b}{2\left(a^2-b^2\right)\left(a+b \sin [c+d x]\right)^2}+\frac{7 a b}{4\left(a^2-b^2\right)^2\left(a+b \sin [c+d x]\right)}\right)}{d \sqrt{e \cos [c+d x]}} + \\
 & \frac{1}{8(a-b)^2(a+b)^2 d \sqrt{e \cos [c+d x]}} \sqrt{\cos [c+d x]}\left(-\frac{1}{\sqrt{1-\cos [c+d x]^2}\left(a+b \sin [c+d x]\right)}\right. \\
 & \left.2\left(8 a^2+6 b^2\right)\left(a+b \sqrt{1-\cos [c+d x]^2}\right)\left(\left(5 a\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4},\right.\right.\right. \right. \\
 & \left.\left.\left.\frac{\cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}}{\sqrt{\cos [c+d x]}}\right] / \left(\sqrt{1-\cos [c+d x]^2}\right)^2\right.\right. \\
 & \left.\left.\left(5\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]-2\right.\right.\right. \\
 & \left.\left.\left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]+(-a^2+b^2)\right.\right.\right. \\
 & \left.\left.\left.\operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]\right) \cos [c+d x]^2\right) \right) \\
 & \left.\left.\left(a^2+b^2(-1+\cos [c+d x]^2)\right)\right)-\frac{1}{\left(-a^2+b^2\right)^{3 / 4}}\left(\frac{1}{8}-\frac{i}{8}\right) \sqrt{b}\right. \\
 & \left.\left(2 \operatorname{ArcTan}\left[1-\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2\right)^{1 / 4}}\right]-2 \operatorname{ArcTan}\left[1+\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2\right)^{1 / 4}}\right]\right)+\right. \\
 & \left.\log \left[\sqrt{-a^2+b^2}-(1+i) \sqrt{b}\left(-a^2+b^2\right)^{1 / 4} \sqrt{\cos [c+d x]}+i b \cos [c+d x]\right]-\right. \\
 & \left.\log \left[\sqrt{-a^2+b^2}+(1+i) \sqrt{b}\left(-a^2+b^2\right)^{1 / 4} \sqrt{\cos [c+d x]}+i b \cos [c+d x]\right]\right)
 \end{aligned}$$

$$\begin{aligned}
 & \sin [c+d x] + \frac{1}{(1-\cos [c+d x])^2 (a+b \sin [c+d x])} 14 a b \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \\
 & \left(\left(5 b \left(a^2-b^2 \right) \operatorname{AppellF1}\left[\frac{1}{4},-\frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right. \right. \\
 & \quad \left. \left. \sqrt{\cos [c+d x]} \sqrt{1-\cos [c+d x]^2} \right) / \right. \\
 & \left(\left(-5 \left(a^2-b^2 \right) \operatorname{AppellF1}\left[\frac{1}{4},-\frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \right. \right. \\
 & \quad 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4},-\frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \right. \\
 & \quad \left. \left. \left(a^2-b^2 \right) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \right. \\
 & \quad \left. \left. \cos [c+d x]^2 \right) \left(a^2+b^2 \left(-1+\cos [c+d x]^2 \right) \right) \right) + \\
 & \left(a \left(-2 \operatorname{ArcTan}\left[1-\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2 \right)^{1 / 4}}\right] + 2 \operatorname{ArcTan}\left[1+\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2 \right)^{1 / 4}}\right] - \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[\sqrt{a^2-b^2}-\sqrt{2} \sqrt{b}\left(a^2-b^2 \right)^{1 / 4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right] + \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[\sqrt{a^2-b^2}+\sqrt{2} \sqrt{b}\left(a^2-b^2 \right)^{1 / 4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right] \right) \right) / \right. \\
 & \left. \left(4 \sqrt{2} \sqrt{b}\left(a^2-b^2 \right)^{3 / 4} \right) \sin [c+d x]^2 \right)
 \end{aligned}$$

Problem 602: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\left(e \cos [c+d x] \right)^{3 / 2} \left(a+b \sin [c+d x] \right)^3} d x$$

Optimal (type 4, 596 leaves, 15 steps):

$$\frac{5 b^{3/2} (7 a^2 + 2 b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right] - 5 b^{3/2} (7 a^2 + 2 b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 (-a^2+b^2)^{13/4} d e^{3/2}} - \frac{a (8 a^2 + 37 b^2) \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2} (c+d x), 2\right]}{4 (a^2-b^2)^3 d e^2 \sqrt{\cos [c+d x]}} - \left(\frac{5 a b (7 a^2 + 2 b^2) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{b-\sqrt{-a^2+b^2}} \right) / \left(\frac{8 (a^2-b^2)^3 (b-\sqrt{-a^2+b^2}) d e \sqrt{e \cos [c+d x]}}{b-\sqrt{-a^2+b^2}} \right) - \left(\frac{5 a b (7 a^2 + 2 b^2) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{b+\sqrt{-a^2+b^2}} \right) / \left(\frac{8 (a^2-b^2)^3 (b+\sqrt{-a^2+b^2}) d e \sqrt{e \cos [c+d x]}}{b+\sqrt{-a^2+b^2}} \right) + \frac{b}{2 (a^2-b^2) d e \sqrt{e \cos [c+d x]} (a+b \sin [c+d x])^2} + \frac{9 a b}{4 (a^2-b^2)^2 d e \sqrt{e \cos [c+d x]} (a+b \sin [c+d x])} - \frac{5 b (7 a^2 + 2 b^2) - a (8 a^2 + 37 b^2) \sin [c+d x]}{4 (a^2-b^2)^3 d e \sqrt{e \cos [c+d x]}}$$

Result (type 6, 1316 leaves):

$$\frac{1}{8 (a-b)^3 (a+b)^3 d (e \cos [c+d x])^{3/2}} \cos [c+d x]^{3/2} \left(\frac{1}{12 \sqrt{1-\cos [c+d x]^2} (a+b \sin [c+d x])} (8 a^4 + 72 a^2 b^2 + 10 b^4) \right. \\ \left. \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \left(- \left(\left(56 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \operatorname{Cos}[c+d x]^{3/2} \right) / \left(\sqrt{1-\cos [c+d x]^2} \right) \right. \right. \right. \\ \left. \left. \left(7 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] - \right. \right. \right. \\ \left. \left. \left(2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \right. \right. \right. \right. \\ \left. \left. \left. (-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \right) \right) \right) \\ \left. \left. \left. \cos [c+d x]^2 \right) (a^2+b^2 (-1+\cos [c+d x]^2)) \right) \right) \right) - \left((3+3 i) \left(2 \operatorname{ArcTan}\left[1-\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1+\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}}\right] - \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4}\right] \right) \right)$$

$$\begin{aligned}
 & \left(\frac{\sqrt{\cos [c+d x]} + i b \cos [c+d x]}{\sqrt{\cos [c+d x]} + i b \cos [c+d x]} + \log \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \\
 & \left. \left. \frac{\sqrt{\cos [c+d x]} + i b \cos [c+d x]}{\sqrt{\cos [c+d x]} + i b \cos [c+d x]} \right] \right) / \left(\sqrt{b} (-a^2+b^2)^{1/4} \right) \sin [c+d x] - \\
 & \frac{1}{(1-\cos [c+d x]^2) (a+b \sin [c+d x])^2} (8 a^3 b + 37 a b^3) \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \\
 & \left(\left(7 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right. \right. \\
 & \left. \left. \cos [c+d x]^{3/2} \sqrt{1-\cos [c+d x]^2} \right) / \right. \\
 & \left(3 \left(-7 (a^2-b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + 2 \right. \right. \\
 & \left. \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
 & \left. \left. (a^2-b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \right) \\
 & \left. \cos [c+d x]^2 \right) (a^2+b^2 (-1+\cos [c+d x]^2)) \left. \right) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{(a^2-b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{(a^2-b^2)^{1/4}} \right] \right) + \right. \\
 & \left. \log \left[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [c+d x]} + b \cos [c+d x] \right] - \right. \\
 & \left. \log \left[\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [c+d x]} + \right. \right. \\
 & \left. \left. b \cos [c+d x] \right] \right) / \left(4 \sqrt{2} b^{3/2} (a^2-b^2)^{1/4} \right) \sin [c+d x]^2 \left. \right) + \\
 & \left(\cos [c+d x]^2 \left(-\frac{b^3 \cos [c+d x]}{2 (a^2-b^2)^2 (a+b \sin [c+d x])^2} - \frac{13 a b^3 \cos [c+d x]}{4 (a^2-b^2)^3 (a+b \sin [c+d x])} + \right. \right. \\
 & \left. \frac{1}{(a^2-b^2)^3} \right. \\
 & 2 \\
 & \left. \sec [c+d x] \right. \\
 & \left. \left. (-3 a^2 b - b^3 + a^3 \sin [c+d x] + 3 a b^2 \sin [c+d x]) \right) \right) / \left(d (e \right. \\
 & \left. \cos [c+d x])^{3/2} \right)
 \end{aligned}$$

Problem 603: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \cos [c+d x])^{5/2} (a+b \sin [c+d x])^3} dx$$

Optimal (type 4, 614 leaves, 15 steps):

$$\begin{aligned}
& \frac{7 b^{5/2} (9 a^2 + 2 b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 (-a^2+b^2)^{15/4} d e^{5/2}} - \frac{7 b^{5/2} (9 a^2 + 2 b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{8 (-a^2+b^2)^{15/4} d e^{5/2}} + \\
& \frac{a (8 a^2 + 69 b^2) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{12 (a^2-b^2)^3 d e^2 \sqrt{e \cos [c+d x]}} - \\
& \left(\frac{7 a b^2 (9 a^2 + 2 b^2) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{b-\sqrt{-a^2+b^2}} \right) / \\
& \left(8 (a^2-b^2)^3 (a^2-b (b-\sqrt{-a^2+b^2})) d e^2 \sqrt{e \cos [c+d x]} \right) - \\
& \left(\frac{7 a b^2 (9 a^2 + 2 b^2) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{b+\sqrt{-a^2+b^2}} \right) / \\
& \left(8 (a^2-b^2)^3 (a^2-b (b+\sqrt{-a^2+b^2})) d e^2 \sqrt{e \cos [c+d x]} \right) + \\
& \frac{b}{2 (a^2-b^2) d e (e \cos [c+d x])^{3/2} (a+b \sin [c+d x])^2} + \\
& \frac{11 a b}{4 (a^2-b^2)^2 d e (e \cos [c+d x])^{3/2} (a+b \sin [c+d x])} - \\
& \frac{7 b (9 a^2 + 2 b^2) - a (8 a^2 + 69 b^2) \sin [c+d x]}{12 (a^2-b^2)^3 d e (e \cos [c+d x])^{3/2}}
\end{aligned}$$

Result (type 6, 1308 leaves):

$$\begin{aligned}
& \frac{1}{24 (a-b)^3 (a+b)^3 d (e \cos [c+d x])^{5/2}} \cos [c+d x]^{5/2} \\
& \left(- \frac{1}{\sqrt{1-\cos [c+d x]^2} (a+b \sin [c+d x])} - 2 (8 a^4 - 120 a^2 b^2 - 42 b^4) (a+b \sqrt{1-\cos [c+d x]^2}) \right) \\
& \left(\left(5 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \sqrt{\cos [c+d x]} \right) / \right. \\
& \left. \left(\sqrt{1-\cos [c+d x]^2} \right) \right) \\
& \left(5 (a^2-b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] - 2 \right. \\
& \left. \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + (-a^2+b^2) \right. \right. \\
& \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \cos [c+d x]^2 \right) \\
& \left. (a^2+b^2 (-1+\cos [c+d x]^2)) \right) - \frac{1}{(-a^2+b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b}
\end{aligned}$$

$$\left(\begin{aligned} &2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] + \\ &\operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] - \\ &\operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] \end{aligned} \right) \Bigg) \\ \sin [c+d x] - \frac{1}{(1-\cos [c+d x]^2)(a+b \sin [c+d x])} \\ 2(8 a^3 b+69 a b^3)\left(a+b \sqrt{1-\cos [c+d x]^2}\right) \\ \left(\left(5 b\left(a^2-b^2\right) \operatorname{AppellF1} \left[\frac{1}{4},-\frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right. \right. \\ \left. \left. \sqrt{\cos [c+d x]} \sqrt{1-\cos [c+d x]^2} \right) / \right. \\ \left(\left(-5\left(a^2-b^2\right) \operatorname{AppellF1} \left[\frac{1}{4},-\frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\ \left. \left. 2\left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4},-\frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \right. \\ \left. \left. \left. \left(a^2-b^2\right) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \right) \right. \\ \left. \cos [c+d x]^2\left(a^2+b^2(-1+\cos [c+d x]^2)\right) \right) + \\ \left(a\left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1/4}} \right] - \right. \\ \left. \operatorname{Log} \left[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} \left(a^2-b^2\right)^{1/4} \sqrt{\cos [c+d x]} + b \cos [c+d x] \right] + \right. \\ \left. \left. \operatorname{Log} \left[\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} \left(a^2-b^2\right)^{1/4} \sqrt{\cos [c+d x]} + b \cos [c+d x] \right] \right) \right) / \right. \\ \left. \left(4 \sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{3/4} \right) \sin [c+d x]^2 \right) + \\ \left(\cos [c+d x] \right)^3 \left(-\frac{b^3}{2\left(a^2-b^2\right)^2\left(a+b \sin [c+d x]\right)^2} - \right. \\ \frac{15 a b^3}{4\left(a^2-b^2\right)^3\left(a+b \sin [c+d x]\right)} + \\ \frac{1}{3\left(a^2-b^2\right)^3} \\ \left. \left. 2 \operatorname{Sec} [c+d x]^2 \right. \right. \\ \left. \left. \left(-3 a^2 b-b^3+a^3 \sin [c+d x]+3 a b^2 \sin [c+d x] \right) \right) \right) / \left(d\left(e \cos [c+d x]\right)^{5/2} \right) \end{aligned}$$

Problem 604: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\left(e \cos [c+d x]\right)^{7 / 2}\left(a+b \sin [c+d x]\right)^3} d x$$

Optimal (type 4, 685 leaves, 16 steps):

$$\frac{9 b^{7 / 2}\left(11 a^2+2 b^2\right) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2\right)^{1 / 4} \sqrt{e}}\right]}{8\left(-a^2+b^2\right)^{17 / 4} d e^{7 / 2}}-\frac{9 b^{7 / 2}\left(11 a^2+2 b^2\right) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2\right)^{1 / 4} \sqrt{e}}\right]}{8\left(-a^2+b^2\right)^{17 / 4} d e^{7 / 2}}-\frac{\left(3 a\left(8 a^4-64 a^2 b^2-139 b^4\right) \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]\right) / \left(20\left(a^2-b^2\right)^4 d e^4 \sqrt{\cos [c+d x]}\right)+\left(9 a b^3\left(11 a^2+2 b^2\right) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]\right) / \left(8\left(a^2-b^2\right)^4\left(b-\sqrt{-a^2+b^2}\right) d e^3 \sqrt{e \cos [c+d x]}\right)+\left(9 a b^3\left(11 a^2+2 b^2\right) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]\right) / \left(8\left(a^2-b^2\right)^4\left(b+\sqrt{-a^2+b^2}\right) d e^3 \sqrt{e \cos [c+d x]}\right)+\frac{b}{2\left(a^2-b^2\right) d e\left(e \cos [c+d x]\right)^{5 / 2}\left(a+b \sin [c+d x]\right)^2}+\frac{13 a b}{4\left(a^2-b^2\right)^2 d e\left(e \cos [c+d x]\right)^{5 / 2}\left(a+b \sin [c+d x]\right)}-\frac{9 b\left(11 a^2+2 b^2\right)-a\left(8 a^2+109 b^2\right) \sin [c+d x]}{20\left(a^2-b^2\right)^3 d e\left(e \cos [c+d x]\right)^{5 / 2}}+\frac{3\left(15 b^3\left(11 a^2+2 b^2\right)+a\left(8 a^4-64 a^2 b^2-139 b^4\right) \sin [c+d x]\right)}{20\left(a^2-b^2\right)^4 d e^3 \sqrt{e \cos [c+d x]}}$$

Result (type 6, 1408 leaves):

$$-\frac{1}{40(a-b)^4(a+b)^4 d\left(e \cos [c+d x]\right)^{7 / 2}}-3 \cos [c+d x]^{7 / 2}\left(\frac{1}{12 \sqrt{1-\cos [c+d x]^2}(a+b \sin [c+d x])}\right)-\left(8 a^6-64 a^4 b^2-304 a^2 b^4-30 b^6\right)\left(a+b \sqrt{1-\cos [c+d x]^2}\right)-\left(-\left(\left(56 a\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]\right)\right)\right)$$

$$\begin{aligned}
 & \left. \left(\cos [c+d x]^{3/2} \right) / \left(\sqrt{1-\cos [c+d x]^2} \left(7\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right. \right. \right. \\
 & \quad - 2\left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right. \\
 & \quad \left. \left. +\left(-a^2+b^2\right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \cos [c+d x]^2 \left(a^2+b^2\left(-1+\cos [c+d x]^2\right)\right) \right) \right) - \\
 & \left((3+3 i) \left(2 \operatorname{ArcTan}\left[1-\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[\right. \right. \right. \\
 & \quad \left. \left. \left. 1+\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4}}\right] - \operatorname{Log}\left[\sqrt{-a^2+b^2}-\left(1+i\right) \sqrt{b}\left(-a^2+b^2\right)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos [c+d x]}+i b \cos [c+d x]\right]+\operatorname{Log}\left[\sqrt{-a^2+b^2}+\left(1+i\right) \sqrt{b}\left(-a^2+b^2\right)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos [c+d x]}+i b \cos [c+d x]\right] \right) \right) / \left(\sqrt{b}\left(-a^2+b^2\right)^{1/4}\right) \sin [c+d x] - \\
 & \frac{1}{\left(1-\cos [c+d x]^2\right)\left(a+b \sin [c+d x]\right)} 2\left(8 a^5 b-64 a^3 b^3-139 a b^5\right) \\
 & \left(a+b \sqrt{1-\cos [c+d x]^2}\right) \\
 & \left(\left(7 b\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right. \right. \\
 & \quad \left. \left. \cos [c+d x]^{3/2} \sqrt{1-\cos [c+d x]^2}\right) / \right. \\
 & \left(3\left(-7\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]+2\right. \right. \\
 & \quad \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4},-\frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]+ \right. \\
 & \quad \left.\left.\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]\right) \right) \\
 & \quad \left.\left.\cos [c+d x]^2\right)\left(a^2+b^2\left(-1+\cos [c+d x]^2\right)\right)\right)+ \\
 & \left(a\left(-2 \operatorname{ArcTan}\left[1-\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1/4}}\right]+2 \operatorname{ArcTan}\left[1+\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1/4}}\right]\right)+ \right. \\
 & \quad \left. \operatorname{Log}\left[\sqrt{a^2-b^2}-\sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{1/4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right]- \right. \\
 & \quad \left. \operatorname{Log}\left[\sqrt{a^2-b^2}+\sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{1/4} \sqrt{\cos [c+d x]}+ \right. \right. \\
 & \quad \left. \left. b \cos [c+d x]\right]\right) / \left(4 \sqrt{2} b^{3/2}\left(a^2-b^2\right)^{1/4}\right) \sin [c+d x]^2 \right) +
 \end{aligned}$$

$$\left(\cos [c + d x]^4 \left(\frac{b^5 \cos [c + d x]}{2 (a^2 - b^2)^3 (a + b \sin [c + d x])^2} + \frac{21 a b^5 \cos [c + d x]}{4 (a^2 - b^2)^4 (a + b \sin [c + d x])} + \frac{1}{5 (a^2 - b^2)^3} \frac{\sec [c + d x]^3}{(-3 a^2 b - b^3 + a^3 \sin [c + d x] + 3 a b^2 \sin [c + d x])} + \frac{1}{5 (a^2 - b^2)^4} 2 \sec [c + d x] (50 a^2 b^3 + 10 b^5 + 3 a^5 \sin [c + d x] - 24 a^3 b^2 \sin [c + d x] - 39 a b^4 \sin [c + d x]) \right) \right) / (d (e \cos [c + d x])^{7/2})$$

Problem 605: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{15/2}}{(a + b \sin [c + d x])^4} dx$$

Optimal (type 4, 671 leaves, 16 steps):

$$\begin{aligned}
 & \frac{39 a (11 a^4 - 17 a^2 b^2 + 6 b^4) e^{15/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 b^{15/2} (-a^2+b^2)^{3/4} d} + \\
 & \frac{39 a (11 a^4 - 17 a^2 b^2 + 6 b^4) e^{15/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 b^{15/2} (-a^2+b^2)^{3/4} d} + \\
 & \left(\frac{13 (231 a^4 - 203 a^2 b^2 + 20 b^4) e^8 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2} (c+d x), 2\right]}{(56 b^8 d \sqrt{e \cos [c+d x]})} - \right. \\
 & \left. \frac{39 a^2 (11 a^4 - 17 a^2 b^2 + 6 b^4) e^8 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{(16 b^8 (a^2 - b (b - \sqrt{-a^2+b^2}))) d \sqrt{e \cos [c+d x]}} - \right. \\
 & \left. \frac{39 a^2 (11 a^4 - 17 a^2 b^2 + 6 b^4) e^8 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2\right]}{(16 b^8 (a^2 - b (b + \sqrt{-a^2+b^2}))) d \sqrt{e \cos [c+d x]}} - \right. \\
 & \frac{e (e \cos [c+d x])^{13/2}}{3 b d (a+b \sin [c+d x])^3} - \frac{13 e^3 (e \cos [c+d x])^{9/2} (11 a + 4 b \sin [c+d x])}{84 b^3 d (a+b \sin [c+d x])^2} - \\
 & \frac{39 e^5 (e \cos [c+d x])^{5/2} (77 a^2 - 20 b^2 + 22 a b \sin [c+d x])}{280 b^5 d (a+b \sin [c+d x])} + \frac{1}{56 b^7 d} \\
 & \left. 13 e^7 \sqrt{e \cos [c+d x]} (21 a (11 a^2 - 6 b^2) - b (77 a^2 - 20 b^2) \sin [c+d x]) \right)
 \end{aligned}$$

Result (type 6, 2302 leaves):

$$\begin{aligned}
 & \frac{1}{560 b^7 d \cos [c+d x]^{15/2}} (e \cos [c+d x])^{15/2} \\
 & \left(- \frac{1}{\sqrt{1 - \cos [c+d x]^2} (a+b \sin [c+d x])} - 2 (4410 a^3 b - 3418 a b^3) (a+b \sqrt{1 - \cos [c+d x]^2}) \right) \\
 & \left(\frac{5 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \sqrt{\cos [c+d x]}}{\sqrt{1 - \cos [c+d x]^2}} \right) / \\
 & \left(\frac{5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] - 2}{2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]} + (-a^2 + b^2) \right. \\
 & \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \cos [c+d x]^2
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(a^2 + b^2 (-1 + \cos [c + d x]^2) \right) \right) - \frac{1}{(-a^2 + b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
 & \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] \right) + \\
 & \left(\operatorname{Log} \left[\sqrt{-a^2 + b^2} - (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [c + d x]} + i b \cos [c + d x] \right] - \right. \\
 & \left. \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1+i) \sqrt{b} (-a^2 + b^2)^{1/4} \sqrt{\cos [c + d x]} + i b \cos [c + d x] \right] \right) \Bigg) \\
 & \sin [c + d x] + \frac{1}{\sqrt{1 - \cos [c + d x]^2} (-1 + 2 \cos [c + d x]^2) (a + b \sin [c + d x])} \\
 & (5600 a^3 b - 3472 a b^3) \left(a + b \sqrt{1 - \cos [c + d x]^2} \right) \cos [2 (c + d x)] \\
 & \left(\frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c + d x]}}{(-a^2 + b^2)^{1/4}} \right]}{b^{3/2} (-a^2 + b^2)^{3/4}} - \right. \\
 & \left. \frac{\left(\frac{1}{2} - \frac{i}{2} \right) (-2 a^2 + b^2) \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c + d x]}}{(-a^2 + b^2)^{1/4}} \right]}{b^{3/2} (-a^2 + b^2)^{3/4}} + \frac{4 \sqrt{\cos [c + d x]}}{b} + \right. \\
 & \left. \left(10 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \sqrt{\cos [c + d x]} \right) \right) / \\
 & \left(\sqrt{1 - \cos [c + d x]^2} \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c + d x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c + d x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c + d x]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \cos [c + d x]^2 \right) (a^2 + b^2 (-1 + \cos [c + d x]^2)) \Bigg) - \\
 & \left(36 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right. \\
 & \left. \cos [c + d x]^{5/2} \right) / \left(5 \sqrt{1 - \cos [c + d x]^2} \right. \\
 & \left(9 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] - \right. \\
 & \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \cos [c + d x]^2 \right) \\
 & \left. (a^2 + b^2 (-1 + \cos [c + d x]^2)) \right) + \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2 + b^2) \operatorname{Log} \left[\sqrt{-a^2 + b^2} - \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left((1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+dx]} + i b \cos[c+dx] \right) \right) / \left(b^{3/2} (-a^2+b^2)^{3/4} \right) - \\
 & \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2a^2+b^2) \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos[c+dx]} + \right. \right. \\
 & \left. \left. i b \cos[c+dx] \right] \right) / \left(b^{3/2} (-a^2+b^2)^{3/4} \right) \left. \right) \operatorname{Sin}[c+dx] - \\
 & \frac{1}{(1-\cos[c+dx]^2)(a+b\sin[c+dx])^2} (3815a^4 - 6251a^2b^2 + 1300b^4) \\
 & \left(a + b \sqrt{1-\cos[c+dx]^2} \right) \\
 & \left(\left(5b(a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] \right. \right. \\
 & \left. \left. \sqrt{\cos[c+dx]} \sqrt{1-\cos[c+dx]^2} \right) / \right. \\
 & \left(\left(-5(a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] + \right. \right. \\
 & \left. \left. 2 \left(2b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] + \right. \right. \right. \\
 & \left. \left. (a^2-b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] \right) \right. \\
 & \left. \left. \cos[c+dx]^2 \right) (a^2+b^2(-1+\cos[c+dx]^2)) \right) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c+dx]}}{(a^2-b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos[c+dx]}}{(a^2-b^2)^{1/4}} \right] - \right. \right. \\
 & \left. \left. \operatorname{Log} \left[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos[c+dx]} + b \cos[c+dx] \right] + \right. \right. \\
 & \left. \left. \operatorname{Log} \left[\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos[c+dx]} + b \cos[c+dx] \right] \right) \right) / \right. \\
 & \left. \left(4 \sqrt{2} \sqrt{b} (a^2-b^2)^{3/4} \right) \operatorname{Sin}[c+dx]^2 + \frac{1}{d} \right. \\
 & \left. (e \cos[c+dx])^{15/2} \operatorname{Sec}[c+dx]^7 \left(-\frac{4a \cos[2(c+dx)]}{5b^5} + \right. \right. \\
 & \left. \left. \frac{(-280a^2+79b^2) \operatorname{Sin}[c+dx]}{42b^6} - \right. \right. \\
 & \left. \left. \frac{(-a^2+b^2)^3}{3b^7(a+b\sin[c+dx])^3} - \right. \right.
 \end{aligned}$$

$$\frac{37 a (a^2 - b^2)^2}{12 b^7 (a + b \sin [c + d x])^2} + \frac{(-a^2 + b^2) (-393 a^2 + 76 b^2)}{24 b^7 (a + b \sin [c + d x])} + \frac{\sin [3 (c + d x)]}{14 b^4}$$

Problem 606: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^{13/2}}{(a + b \sin [c + d x])^4} dx$$

Optimal (type 4, 557 leaves, 15 steps):

$$\frac{77 a (3 a^2 - 2 b^2) e^{13/2} \operatorname{ArcTan} \left[\frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{16 b^{13/2} (-a^2 + b^2)^{1/4} d} - \frac{77 a (3 a^2 - 2 b^2) e^{13/2} \operatorname{ArcTanh} \left[\frac{\sqrt{b} \sqrt{e \cos [c + d x]}}{(-a^2 + b^2)^{1/4} \sqrt{e}} \right]}{16 b^{13/2} (-a^2 + b^2)^{1/4} d} - \frac{77 (15 a^2 - 4 b^2) e^6 \sqrt{e \cos [c + d x]} \operatorname{EllipticE} \left[\frac{1}{2} (c + d x), 2 \right]}{40 b^6 d \sqrt{\cos [c + d x]}} + \left(\frac{77 a^2 (3 a^2 - 2 b^2) e^7 \sqrt{\cos [c + d x]} \operatorname{EllipticPi} \left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right]}{16 b^7 (b - \sqrt{-a^2 + b^2}) d \sqrt{e \cos [c + d x]}} \right) + \left(\frac{77 a^2 (3 a^2 - 2 b^2) e^7 \sqrt{\cos [c + d x]} \operatorname{EllipticPi} \left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2} (c + d x), 2 \right]}{16 b^7 (b + \sqrt{-a^2 + b^2}) d \sqrt{e \cos [c + d x]}} \right) - \frac{e (e \cos [c + d x])^{11/2}}{3 b d (a + b \sin [c + d x])^3} - \frac{11 e^3 (e \cos [c + d x])^{7/2} (9 a + 4 b \sin [c + d x])}{60 b^3 d (a + b \sin [c + d x])^2} - \frac{77 e^5 (e \cos [c + d x])^{3/2} (15 a^2 - 4 b^2 + 6 a b \sin [c + d x])}{120 b^5 d (a + b \sin [c + d x])}$$

Result (type 6, 1331 leaves):

$$-\frac{1}{80 b^5 d \cos [c + d x]^{13/2}} - 77 (e \cos [c + d x])^{13/2} \left(\frac{1}{2 \sqrt{1 - \cos [c + d x]^2} (a + b \sin [c + d x])} a b (a + b \sqrt{1 - \cos [c + d x]^2}) - \left(\left(\left(56 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \right) \right)$$

$$\begin{aligned}
 & \left(\cos [c+d x]^{3/2} \right) / \left(\sqrt{1-\cos [c+d x]^2} \left(7\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right. \right. \\
 & \quad - 2\left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right. \\
 & \quad \left. \left. +\left(-a^2+b^2\right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \cos [c+d x]^2 \left(a^2+b^2\left(-1+\cos [c+d x]^2\right)\right) \right) - \\
 & \left((3+3 i) \left(2 \operatorname{ArcTan}\left[1-\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[\right. \right. \right. \\
 & \quad \left. \left. \left. 1+\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4}}\right] - \operatorname{Log}\left[\sqrt{-a^2+b^2}-(1+i) \sqrt{b}\left(-a^2+b^2\right)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos [c+d x]}+i b \cos [c+d x]\right]+\operatorname{Log}\left[\sqrt{-a^2+b^2}+(1+i) \sqrt{b}\left(-a^2+b^2\right)^{1/4} \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{\cos [c+d x]}+i b \cos [c+d x]\right] \right) \right) / \left(\sqrt{b}\left(-a^2+b^2\right)^{1/4} \right) \sin [c+d x] - \\
 & \frac{1}{\left(1-\cos [c+d x]^2\right)\left(a+b \sin [c+d x]\right)} 2\left(15 a^2-4 b^2\right)\left(a+b \sqrt{1-\cos [c+d x]^2}\right) \\
 & \left(\left(7 b\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right. \right. \\
 & \quad \left. \left. \cos [c+d x]^{3/2} \sqrt{1-\cos [c+d x]^2} \right) / \right. \\
 & \left(3\left(-7\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + 2 \right. \right. \\
 & \quad \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4},-\frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \right. \\
 & \quad \left. \left. \left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \right) \\
 & \quad \left. \cos [c+d x]^2\right)\left(a^2+b^2\left(-1+\cos [c+d x]^2\right)\right) \right) + \\
 & \left(a\left(-2 \operatorname{ArcTan}\left[1-\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1/4}}\right] + 2 \operatorname{ArcTan}\left[1+\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1/4}}\right] \right. \right. \\
 & \quad \left. \left. \operatorname{Log}\left[\sqrt{a^2-b^2}-\sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{1/4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right]-\operatorname{Log}\left[\right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{a^2-b^2}+\sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{1/4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right] \right) \right) / \right. \\
 & \quad \left. \left(4 \sqrt{2} b^{3/2}\left(a^2-b^2\right)^{1/4} \right) \sin [c+d x]^2 \right) + \frac{1}{d} \\
 & \left(e \cos [c+d x] \right)^{13/2} \operatorname{Sec}[c+d x]^6 \left(-\frac{8 a \cos [c+d x]}{3 b^5} + \right.
 \end{aligned}$$

$$\frac{-a^4 \cos [c+d x]+2 a^2 b^2 \cos [c+d x]-b^4 \cos [c+d x]}{3 b^5 (a+b \sin [c+d x])^3} +$$

$$\frac{9\left(a^3 \cos [c+d x]-a b^2 \cos [c+d x]\right)}{4 b^5 (a+b \sin [c+d x])^2} +$$

$$\frac{-71 a^2 \cos [c+d x]+20 b^2 \cos [c+d x]}{8 b^5 (a+b \sin [c+d x])} +$$

$$\frac{\sin [2(c+d x)]}{5 b^4}$$

Problem 607: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c+d x])^{11/2}}{(a+b \sin [c+d x])^4} dx$$

Optimal (type 4, 571 leaves, 15 steps):

$$\frac{15 a\left(7 a^2-6 b^2\right) e^{11/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4} \sqrt{e}}\right]}{16 b^{11/2}\left(-a^2+b^2\right)^{3/4} d}-\frac{15 a\left(7 a^2-6 b^2\right) e^{11/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4} \sqrt{e}}\right]}{16 b^{11/2}\left(-a^2+b^2\right)^{3/4} d}$$

$$+\frac{5\left(21 a^2-4 b^2\right) e^6 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{8 b^6 d \sqrt{e \cos [c+d x]}}$$

$$\left(\frac{15 a^2\left(7 a^2-6 b^2\right) e^6 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{\left(16 b^6\left(a^2-b\left(b-\sqrt{-a^2+b^2}\right)\right) d \sqrt{e \cos [c+d x]}\right)}+\right.$$

$$\left.\frac{15 a^2\left(7 a^2-6 b^2\right) e^6 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{\left(16 b^6\left(a^2-b\left(b+\sqrt{-a^2+b^2}\right)\right) d \sqrt{e \cos [c+d x]}\right)}-\right.$$

$$\frac{e\left(e \cos [c+d x]\right)^{9/2}}{3 b d(a+b \sin [c+d x])^3}-\frac{e^3\left(e \cos [c+d x]\right)^{5/2}(7 a+4 b \sin [c+d x])}{4 b^3 d(a+b \sin [c+d x])^2}$$

$$+\frac{5 e^5 \sqrt{e \cos [c+d x]}\left(21 a^2-4 b^2+14 a b \sin [c+d x]\right)}{8 b^5 d(a+b \sin [c+d x])}$$

Result (type 6, 2220 leaves):

$$\frac{1}{d}(e \cos [c+d x])^{11/2} \sec [c+d x]^5\left(\frac{2 \sin [c+d x]}{3 b^4}-\right.$$

$$\left.\frac{\left(-a^2+b^2\right)^2}{3 b^5(a+b \sin [c+d x])^3}+\frac{25 a\left(a^2-b^2\right)}{12 b^5(a+b \sin [c+d x])^2}+\frac{-165 a^2+52 b^2}{24 b^5(a+b \sin [c+d x])}\right)-$$

$$\begin{aligned}
 & \frac{1}{16 b^5 d \cos [c+d x]^{11/2}} (e \cos [c+d x])^{11/2} \left(-\frac{1}{\sqrt{1-\cos [c+d x]^2} (a+b \sin [c+d x])} \right. \\
 & 76 a b \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \left(\left(5 a \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \\
 & \quad \left. \left. \left. \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \sqrt{\cos [c+d x]} \right) / \left(\sqrt{1-\cos [c+d x]^2} \right) \right. \\
 & \quad \left(5 \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] - 2 \right. \\
 & \quad \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \left(-a^2+b^2 \right) \right. \\
 & \quad \left. \left. \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \cos [c+d x]^2 \right) \\
 & \quad \left. \left(a^2+b^2 \left(-1+\cos [c+d x]^2 \right) \right) \right) - \frac{1}{\left(-a^2+b^2 \right)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
 & \quad \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2 \right)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2 \right)^{1/4}} \right] \right) + \\
 & \quad \left(\operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} \left(-a^2+b^2 \right)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] - \right. \\
 & \quad \left. \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} \left(-a^2+b^2 \right)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] \right) \left. \right) \\
 & \sin [c+d x] + \frac{1}{\sqrt{1-\cos [c+d x]^2} (-1+2 \cos [c+d x]^2) (a+b \sin [c+d x])} \\
 & 32 a b \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \cos [2(c+d x)] \\
 & \left(\frac{\left(\frac{1}{2} - \frac{i}{2} \right) \left(-2 a^2+b^2 \right) \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2 \right)^{1/4}} \right]}{b^{3/2} \left(-a^2+b^2 \right)^{3/4}} - \right. \\
 & \quad \frac{\left(\frac{1}{2} - \frac{i}{2} \right) \left(-2 a^2+b^2 \right) \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2 \right)^{1/4}} \right]}{b^{3/2} \left(-a^2+b^2 \right)^{3/4}} + \frac{4 \sqrt{\cos [c+d x]}}{b} + \\
 & \quad \left(10 a \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \sqrt{\cos [c+d x]} \right) / \\
 & \quad \left(\sqrt{1-\cos [c+d x]^2} \left(5 \left(a^2-b^2 \right) \operatorname{AppellF1} \left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. \left(\frac{b^2 \operatorname{Cos}[c+dx]^2}{-a^2+b^2} \right) + (-a^2+b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \operatorname{Cos}[c+dx]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \operatorname{Cos}[c+dx]^2}{-a^2+b^2} \right] \operatorname{Cos}[c+dx]^2 \right) (a^2+b^2 (-1+\operatorname{Cos}[c+dx]^2)) \Bigg) - \\
 & \left(36 a (a^2-b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Cos}[c+dx]^2, \frac{b^2 \operatorname{Cos}[c+dx]^2}{-a^2+b^2} \right] \right. \\
 & \left. \operatorname{Cos}[c+dx]^{5/2} \right) / \left(5 \sqrt{1-\operatorname{Cos}[c+dx]^2} \right. \\
 & \left(9 (a^2-b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Cos}[c+dx]^2, \frac{b^2 \operatorname{Cos}[c+dx]^2}{-a^2+b^2} \right] - \right. \\
 & \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{9}{4}, \frac{1}{2}, 2, \frac{13}{4}, \operatorname{Cos}[c+dx]^2, \frac{b^2 \operatorname{Cos}[c+dx]^2}{-a^2+b^2} \right] + (-a^2+b^2) \right. \right. \\
 & \left. \left. \operatorname{AppellF1} \left[\frac{9}{4}, \frac{3}{2}, 1, \frac{13}{4}, \operatorname{Cos}[c+dx]^2, \frac{b^2 \operatorname{Cos}[c+dx]^2}{-a^2+b^2} \right] \right) \operatorname{Cos}[c+dx]^2 \right) \\
 & (a^2+b^2 (-1+\operatorname{Cos}[c+dx]^2)) \Bigg) + \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2+b^2) \operatorname{Log}[\sqrt{-a^2+b^2} - \right. \\
 & \left. (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\operatorname{Cos}[c+dx]} + i b \operatorname{Cos}[c+dx]] \right) / \left(b^{3/2} (-a^2+b^2)^{3/4} \right) - \\
 & \left(\left(\frac{1}{4} - \frac{i}{4} \right) (-2 a^2+b^2) \operatorname{Log}[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\operatorname{Cos}[c+dx]} + \right. \\
 & \left. i b \operatorname{Cos}[c+dx]] \right) / \left(b^{3/2} (-a^2+b^2)^{3/4} \right) \Bigg) \operatorname{Sin}[c+dx] - \\
 & \frac{1}{(1-\operatorname{Cos}[c+dx]^2) (a+b \operatorname{Sin}[c+dx])} 2 (41 a^2-20 b^2) \left(a+b \sqrt{1-\operatorname{Cos}[c+dx]^2} \right) \\
 & \left(\left(5 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[c+dx]^2, \frac{b^2 \operatorname{Cos}[c+dx]^2}{-a^2+b^2} \right] \right. \right. \\
 & \left. \left. \sqrt{\operatorname{Cos}[c+dx]} \sqrt{1-\operatorname{Cos}[c+dx]^2} \right) \right) / \\
 & \left(\left(-5 (a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \operatorname{Cos}[c+dx]^2, \frac{b^2 \operatorname{Cos}[c+dx]^2}{-a^2+b^2} \right] + \right. \right. \\
 & \left. \left. 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \operatorname{Cos}[c+dx]^2, \frac{b^2 \operatorname{Cos}[c+dx]^2}{-a^2+b^2} \right] + \right. \right. \right. \\
 & \left. \left. (a^2-b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \operatorname{Cos}[c+dx]^2, \frac{b^2 \operatorname{Cos}[c+dx]^2}{-a^2+b^2} \right] \right) \right) \\
 & \left. \operatorname{Cos}[c+dx]^2 \right) (a^2+b^2 (-1+\operatorname{Cos}[c+dx]^2)) \Bigg) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[c+dx]}}{(a^2-b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\operatorname{Cos}[c+dx]}}{(a^2-b^2)^{1/4}} \right] \right) - \right. \\
 & \left. \operatorname{Log}[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\operatorname{Cos}[c+dx]} + b \operatorname{Cos}[c+dx]] + \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(\sqrt{1 - \cos [c + d x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c + d x]^2, \right. \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c + d x]^2, \right. \right. \\
 & \quad \left. \left. \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \cos [c + d x]^2 \left(a^2 + b^2 (-1 + \cos [c + d x]^2) \right) \Big) - \\
 & \left((3 + 3 i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[\right. \right. \right. \\
 & \quad \left. \left. 1 + \frac{(1 + i) \sqrt{b} \sqrt{\cos [c + d x]}}{(-a^2 + b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2 + b^2} - (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \\
 & \quad \left. \left. \sqrt{\cos [c + d x]} + i b \cos [c + d x] \right] + \operatorname{Log} \left[\sqrt{-a^2 + b^2} + (1 + i) \sqrt{b} (-a^2 + b^2)^{1/4} \right. \right. \\
 & \quad \left. \left. \sqrt{\cos [c + d x]} + i b \cos [c + d x] \right] \right) \Big) / \left(\sqrt{b} (-a^2 + b^2)^{1/4} \right) \sin [c + d x] - \\
 & \frac{1}{(1 - \cos [c + d x]^2) (a + b \sin [c + d x])} 2 (5 a^2 - 4 b^2) \left(a + b \sqrt{1 - \cos [c + d x]^2} \right) \\
 & \left(\left(7 b (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right. \right. \\
 & \quad \left. \left. \cos [c + d x]^{3/2} \sqrt{1 - \cos [c + d x]^2} \right) \Big) / \right. \\
 & \left(3 \left(-7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \quad \left. \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] + \right. \right. \\
 & \quad \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c + d x]^2, \frac{b^2 \cos [c + d x]^2}{-a^2 + b^2} \right] \right) \right) \\
 & \quad \left. \cos [c + d x]^2 \left(a^2 + b^2 (-1 + \cos [c + d x]^2) \right) \right) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c + d x]}}{(a^2 - b^2)^{1/4}} \right] + \right. \right. \\
 & \quad \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] - \right. \\
 & \quad \left. \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2} \sqrt{b} (a^2 - b^2)^{1/4} \sqrt{\cos [c + d x]} + b \cos [c + d x] \right] \right) \right) \Big) / \\
 & \left(4 \sqrt{2} b^{3/2} (a^2 - b^2)^{1/4} \right) \sin [c + d x]^2 \Big)
 \end{aligned}$$

Problem 609: Result unnecessarily involves higher level functions and more

than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c+d x])^{7/2}}{(a+b \sin [c+d x])^4} dx$$

Optimal (type 4, 597 leaves, 15 steps):

$$\begin{aligned} & -\frac{5 a\left(a^2-2 b^2\right) e^{7/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4} \sqrt{e}}\right]}{16 b^{7/2}\left(-a^2+b^2\right)^{7/4} d}-\frac{5 a\left(a^2-2 b^2\right) e^{7/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4} \sqrt{e}}\right]}{16 b^{7/2}\left(-a^2+b^2\right)^{7/4} d}+ \\ & \frac{5\left(3 a^2-4 b^2\right) e^4 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{24 b^4\left(a^2-b^2\right) d \sqrt{e \cos [c+d x]}}- \\ & \left(5 a^2\left(a^2-2 b^2\right) e^4 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]\right) / \\ & \left(16 b^4\left(a^2-b^2\right)\left(a^2-b\left(b-\sqrt{-a^2+b^2}\right)\right) d \sqrt{e \cos [c+d x]}\right)- \\ & \left(5 a^2\left(a^2-2 b^2\right) e^4 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]\right) / \\ & \left(16 b^4\left(a^2-b^2\right)\left(a^2-b\left(b+\sqrt{-a^2+b^2}\right)\right) d \sqrt{e \cos [c+d x]}\right)-\frac{e\left(e \cos [c+d x]\right)^{5/2}}{3 b d\left(a+b \sin [c+d x]\right)^3}- \\ & \frac{5\left(3 a^2-4 b^2\right) e^3 \sqrt{e \cos [c+d x]}}{24 b^3\left(a^2-b^2\right) d\left(a+b \sin [c+d x]\right)}+\frac{5 e^3 \sqrt{e \cos [c+d x]}\left(3 a+4 b \sin [c+d x]\right)}{12 b^3 d\left(a+b \sin [c+d x]\right)^2} \end{aligned}$$

Result (type 6, 1263 leaves):

$$\begin{aligned} & \frac{1}{d}\left(e \cos [c+d x]\right)^{7/2} \sec [c+d x]^3 \\ & \left(\frac{a^2-b^2}{3 b^3\left(a+b \sin [c+d x]\right)^3}-\frac{13 a}{12 b^3\left(a+b \sin [c+d x]\right)^2}+\frac{-33 a^2+28 b^2}{24 b^3\left(-a^2+b^2\right)\left(a+b \sin [c+d x]\right)}\right)+ \\ & \frac{1}{48(a-b) b^3(a+b) d \cos [c+d x]^{7/2}} \\ & 5\left(e \cos [c+d x]\right)^{7/2}\left(-\frac{1}{\sqrt{1-\cos [c+d x]}^2(a+b \sin [c+d x])}-4 a b\left(a+b \sqrt{1-\cos [c+d x]^2}\right)\right) \\ & \left(\left(5 a\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \sqrt{\cos [c+d x]}\right) / \right. \\ & \left.\left(\sqrt{1-\cos [c+d x]^2}\left(5\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]-2\left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]+(-a^2+b^2) \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]\right)\right)\right) \right) \end{aligned}$$

$$\begin{aligned}
& \left. \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right) \cos [c+d x]^2 \left(a^2+b^2 \left(-1+\cos [c+d x]^2 \right) \right) \right) - \\
& \frac{1}{\left(-a^2+b^2\right)^{3/4}} \left(\frac{1}{8}-\frac{i}{8} \right) \sqrt{b} \left(2 \operatorname{ArcTan} \left[1-\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4}} \right] - \right. \\
& \left. 2 \operatorname{ArcTan} \left[1+\frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{\left(-a^2+b^2\right)^{1/4}} \right] + \operatorname{Log} \left[\sqrt{-a^2+b^2}-(1+i) \sqrt{b} \right. \right. \\
& \left. \left. \left(-a^2+b^2\right)^{1/4} \sqrt{\cos [c+d x]}+i b \cos [c+d x] \right] - \operatorname{Log} \left[\sqrt{-a^2+b^2}+(1+i) \right. \right. \\
& \left. \left. \sqrt{b} \left(-a^2+b^2\right)^{1/4} \sqrt{\cos [c+d x]}+i b \cos [c+d x] \right] \right) \right) \sin [c+d x] - \\
& \frac{1}{\left(1-\cos [c+d x]^2\right)\left(a+b \sin [c+d x]\right)} 2\left(3 a^2-4 b^2\right)\left(a+b \sqrt{1-\cos [c+d x]^2}\right) \\
& \left(\left(5 b\left(a^2-b^2\right) \operatorname{AppellF1} \left[\frac{1}{4},-\frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right. \right. \\
& \left. \left. \sqrt{\cos [c+d x]} \sqrt{1-\cos [c+d x]^2} \right) / \right. \\
& \left(\left(-5\left(a^2-b^2\right) \operatorname{AppellF1} \left[\frac{1}{4},-\frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
& \left. \left. 2\left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4},-\frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \right. \\
& \left. \left. \left. \left(a^2-b^2\right) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \right) \right. \\
& \left. \left. \cos [c+d x]^2 \left(a^2+b^2 \left(-1+\cos [c+d x]^2 \right) \right) \right) + \right. \\
& \left(a \left(-2 \operatorname{ArcTan} \left[1-\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1+\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1/4}} \right] - \right. \right. \\
& \left. \left. \operatorname{Log} \left[\sqrt{a^2-b^2}-\sqrt{2} \sqrt{b} \left(a^2-b^2\right)^{1/4} \sqrt{\cos [c+d x]}+b \cos [c+d x] \right] + \right. \right. \\
& \left. \left. \operatorname{Log} \left[\sqrt{a^2-b^2}+\sqrt{2} \sqrt{b} \left(a^2-b^2\right)^{1/4} \sqrt{\cos [c+d x]}+b \cos [c+d x] \right] \right) \right) / \right. \\
& \left. \left. \left. \left(4 \sqrt{2} \sqrt{b} \left(a^2-b^2\right)^{3/4} \right) \right) \sin [c+d x]^2 \right) \right)
\end{aligned}$$

Problem 610: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{\left(e \cos [c+d x]\right)^{5/2}}{\left(a+b \sin [c+d x]\right)^4} d x$$

Optimal (type 4, 574 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{a (a^2 - 6 b^2) e^{5/2} \operatorname{ArcTan} \left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{16 b^{5/2} (-a^2+b^2)^{9/4} d} + \frac{a (a^2 - 6 b^2) e^{5/2} \operatorname{ArcTanh} \left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}} \right]}{16 b^{5/2} (-a^2+b^2)^{9/4} d} + \\
 & \frac{(a^2 + 4 b^2) e^2 \sqrt{e \cos [c+d x]} \operatorname{EllipticE} \left[\frac{1}{2} (c+d x), 2 \right]}{8 b^2 (a^2 - b^2)^2 d \sqrt{\cos [c+d x]}} - \\
 & \frac{a^2 (a^2 - 6 b^2) e^3 \sqrt{\cos [c+d x]} \operatorname{EllipticPi} \left[\frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right]}{16 b^3 (a^2 - b^2)^2 (b - \sqrt{-a^2+b^2}) d \sqrt{e \cos [c+d x]}} - \\
 & \frac{a^2 (a^2 - 6 b^2) e^3 \sqrt{\cos [c+d x]} \operatorname{EllipticPi} \left[\frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2} (c+d x), 2 \right]}{16 b^3 (a^2 - b^2)^2 (b + \sqrt{-a^2+b^2}) d \sqrt{e \cos [c+d x]}} - \frac{e (e \cos [c+d x])^{3/2}}{3 b d (a+b \sin [c+d x])^3} + \\
 & \frac{a e (e \cos [c+d x])^{3/2}}{4 b (a^2 - b^2) d (a+b \sin [c+d x])^2} + \frac{(a^2 + 4 b^2) e (e \cos [c+d x])^{3/2}}{8 b (a^2 - b^2)^2 d (a+b \sin [c+d x])}
 \end{aligned}$$

Result (type 6, 1286 leaves):

$$\begin{aligned}
 & \frac{1}{d} (e \cos [c+d x])^{5/2} \operatorname{Sec} [c+d x]^2 \left(- \frac{\cos [c+d x]}{3 b (a+b \sin [c+d x])^3} - \frac{a \cos [c+d x]}{4 b (-a^2+b^2) (a+b \sin [c+d x])^2} + \right. \\
 & \left. \frac{a^2 \cos [c+d x] + 4 b^2 \cos [c+d x]}{8 b (-a^2+b^2)^2 (a+b \sin [c+d x])} \right) + \frac{1}{16 (a-b)^2 b (a+b)^2 d \cos [c+d x]^{5/2}} \\
 & (e \cos [c+d x])^{5/2} \left(\frac{1}{6 \sqrt{1 - \cos [c+d x]^2} (a+b \sin [c+d x])} - 5 a b (a+b \sqrt{1 - \cos [c+d x]^2}) \right. \\
 & \left(- \left(\left(56 a (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \cos [c+d x]^{3/2} \right) / \right. \right. \\
 & \left(\sqrt{1 - \cos [c+d x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] - 2 \left(2 b^2 \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \right. \right. \right. \\
 & \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + (-a^2+b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \right. \right. \\
 & \left. \left. \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \cos [c+d x]^2 \right) (a^2 + b^2 (-1 + \cos [c+d x]^2)) \left. \right) \left. \right) - \\
 & \left((3 + 3 i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[\right. \right. \right. \\
 & \left. \left. \left. 1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right. \\
 & \left. \left. \left. \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] + \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned} & \left. \left. \left. \left. \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right) \right) \right) / \left(\sqrt{b} \left(-a^2+b^2\right)^{1 / 4} \right) \sin [c+d x] - \\ & \frac{1}{\left(1-\cos [c+d x]\right)^2 (a+b \sin [c+d x])} 2\left(a^2+4 b^2\right)\left(a+b \sqrt{1-\cos [c+d x]^2}\right) \\ & \left(\left(7 b\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right. \right. \\ & \left. \left. \cos [c+d x]^{3 / 2} \sqrt{1-\cos [c+d x]^2} \right) / \right. \\ & \left(3\left(-7\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{4},-\frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \right. \right. \\ & \left. \left. 2\left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4},-\frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \right. \right. \right. \\ & \left. \left. \left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \right) \\ & \left. \cos [c+d x]^2\right)\left(a^2+b^2\left(-1+\cos [c+d x]^2\right)\right) \left. + \right. \\ & \left(a\left(-2 \operatorname{ArcTan}\left[1-\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1 / 4}}\right]+2 \operatorname{ArcTan}\left[1+\frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{\left(a^2-b^2\right)^{1 / 4}}\right] + \right. \right. \\ & \left. \left. \operatorname{Log}\left[\sqrt{a^2-b^2}-\sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{1 / 4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right]- \right. \right. \\ & \left. \left. \operatorname{Log}\left[\sqrt{a^2-b^2}+\sqrt{2} \sqrt{b}\left(a^2-b^2\right)^{1 / 4} \sqrt{\cos [c+d x]}+b \cos [c+d x]\right] \right) \right) \left. \right) / \\ & \left(4 \sqrt{2} b^{3 / 2}\left(a^2-b^2\right)^{1 / 4} \right) \sin [c+d x]^2 \end{aligned}$$

Problem 611: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c+d x])^{3 / 2}}{(a+b \sin [c+d x])^4} d x$$

Optimal (type 4, 592 leaves, 15 steps):

$$\begin{aligned}
 & - \frac{a (a^2 + 6 b^2) e^{3/2} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 b^{3/2} (-a^2+b^2)^{11/4} d} - \frac{a (a^2 + 6 b^2) e^{3/2} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 b^{3/2} (-a^2+b^2)^{11/4} d} \\
 & + \frac{(3 a^2 + 4 b^2) e^2 \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{24 b^2 (a^2 - b^2)^2 d \sqrt{e \cos [c+d x]}} \\
 & + \frac{a^2 (a^2 + 6 b^2) e^2 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{16 b^2 (a^2 - b^2)^2 (a^2 - b (b - \sqrt{-a^2+b^2})) d \sqrt{e \cos [c+d x]}} \\
 & + \frac{a^2 (a^2 + 6 b^2) e^2 \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{16 b^2 (a^2 - b^2)^2 (a^2 - b (b + \sqrt{-a^2+b^2})) d \sqrt{e \cos [c+d x]}} - \frac{e \sqrt{e \cos [c+d x]}}{3 b d (a + b \sin [c+d x])^3} \\
 & + \frac{a e \sqrt{e \cos [c+d x]}}{12 b (a^2 - b^2) d (a + b \sin [c+d x])^2} + \frac{(3 a^2 + 4 b^2) e \sqrt{e \cos [c+d x]}}{24 b (a^2 - b^2)^2 d (a + b \sin [c+d x])}
 \end{aligned}$$

Result (type 6, 1263 leaves):

$$\begin{aligned}
 & \frac{1}{d} (e \cos [c+d x])^{3/2} \sec [c+d x] \left(- \frac{1}{3 b (a + b \sin [c+d x])^3} - \right. \\
 & \left. \frac{a}{12 b (-a^2+b^2) (a + b \sin [c+d x])^2} + \frac{3 a^2 + 4 b^2}{24 b (-a^2+b^2)^2 (a + b \sin [c+d x])} \right) - \\
 & \frac{1}{48 (a-b)^2 b (a+b)^2 d \cos [c+d x]^{3/2}} (e \cos [c+d x])^{3/2} \left(\frac{1}{\sqrt{1 - \cos [c+d x]^2} (a + b \sin [c+d x])} \right. \\
 & \left. 28 a b (a + b \sqrt{1 - \cos [c+d x]^2}) \left(\left(5 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \right. \right. \right. \right. \\
 & \left. \left. \left. \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \sqrt{\cos [c+d x]} \right) / \left(\sqrt{1 - \cos [c+d x]^2} \right. \right. \\
 & \left. \left. \left(5 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] - \right. \right. \right. \\
 & \left. \left. \left. 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + (-a^2+b^2) \right. \right. \right. \right. \\
 & \left. \left. \left. \operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \right) \cos [c+d x]^2 \right) \right. \\
 & \left. (a^2 + b^2 (-1 + \cos [c+d x]^2)) \right) - \frac{1}{(-a^2+b^2)^{3/4}} \left(\frac{1}{8} - \frac{i}{8} \right) \sqrt{b} \\
 & \left(2 \operatorname{ArcTan}\left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}}\right] \right) + \\
 & \operatorname{Log}\left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x]\right] -
 \end{aligned}$$

$$\begin{aligned}
 & - \frac{5 a (a^2 + 2 b^2) \sqrt{e} \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 \sqrt{b} (-a^2+b^2)^{13/4} d} + \frac{5 a (a^2 + 2 b^2) \sqrt{e} \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 \sqrt{b} (-a^2+b^2)^{13/4} d} + \\
 & \frac{(11 a^2 + 4 b^2) \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{8 (a^2 - b^2)^3 d \sqrt{\cos [c+d x]}} + \\
 & \left(\frac{5 a^2 (a^2 + 2 b^2) e \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b - \sqrt{-a^2 + b^2}}, \frac{1}{2}(c+d x), 2\right]}{16 b (a^2 - b^2)^3 (b - \sqrt{-a^2 + b^2}) d \sqrt{e \cos [c+d x]}} \right) / \\
 & \left(\frac{5 a^2 (a^2 + 2 b^2) e \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b + \sqrt{-a^2 + b^2}}, \frac{1}{2}(c+d x), 2\right]}{16 b (a^2 - b^2)^3 (b + \sqrt{-a^2 + b^2}) d \sqrt{e \cos [c+d x]}} \right) + \\
 & \frac{b (e \cos [c+d x])^{3/2}}{3 (a^2 - b^2) d e (a + b \sin [c+d x])^3} + \\
 & \frac{3 a b (e \cos [c+d x])^{3/2}}{4 (a^2 - b^2)^2 d e (a + b \sin [c+d x])^2} + \frac{b (11 a^2 + 4 b^2) (e \cos [c+d x])^{3/2}}{8 (a^2 - b^2)^3 d e (a + b \sin [c+d x])}
 \end{aligned}$$

Result (type 6, 1294 leaves):

$$\begin{aligned}
 & \frac{1}{d} \sqrt{e \cos [c+d x]} \left(\frac{b \cos [c+d x]}{3 (a^2 - b^2) (a + b \sin [c+d x])^3} + \right. \\
 & \left. \frac{3 a b \cos [c+d x]}{4 (a^2 - b^2)^2 (a + b \sin [c+d x])^2} - \frac{-11 a^2 b \cos [c+d x] - 4 b^3 \cos [c+d x]}{8 (a^2 - b^2)^3 (a + b \sin [c+d x])} \right) + \\
 & \frac{1}{16 (a - b)^3 (a + b)^3 d \sqrt{\cos [c+d x]}} \sqrt{e \cos [c+d x]} \\
 & \left(\frac{1}{12 \sqrt{1 - \cos [c+d x]^2} (a + b \sin [c+d x])} (16 a^3 + 14 a b^2) (a + b \sqrt{1 - \cos [c+d x]^2}) \right. \\
 & \left. - \left(\left(56 a (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2}\right] \cos [c+d x]^{3/2} \right) / \right. \right. \\
 & \left. \left(\sqrt{1 - \cos [c+d x]^2} \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2}\right] - 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2}\right] + (-a^2 + b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2 + b^2}\right] \right) \cos [c+d x]^2 \right) (a^2 + b^2 (-1 + \cos [c+d x]^2)) \right) \right) - \\
 & \left. \left((3 + 3 i) \left(2 \operatorname{ArcTan}\left[1 - \frac{(1 + i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2 + b^2)^{1/4}}\right] - 2 \operatorname{ArcTan}\left[\right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left. 1 + \frac{(1+i)\sqrt{b}\sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}} \right] - \text{Log}\left[\sqrt{-a^2+b^2} - (1+i)\sqrt{b}(-a^2+b^2)^{1/4}\right. \\
 & \left. \sqrt{\cos[c+dx]} + ib\cos[c+dx]\right] + \text{Log}\left[\sqrt{-a^2+b^2} + (1+i)\sqrt{b}(-a^2+b^2)^{1/4}\right. \\
 & \left. \sqrt{\cos[c+dx]} + ib\cos[c+dx]\right] \Bigg) / \left(\sqrt{b}(-a^2+b^2)^{1/4}\right) \sin[c+dx] - \\
 & \frac{1}{(1-\cos[c+dx]^2)(a+b\sin[c+dx])^2} (11a^2b+4b^3) \left(a+b\sqrt{1-\cos[c+dx]^2}\right) \\
 & \left(\left(7b(a^2-b^2) \text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c+dx]^2, \frac{b^2\cos[c+dx]^2}{-a^2+b^2}\right] \right. \right. \\
 & \left. \left. \cos[c+dx]^{3/2}\sqrt{1-\cos[c+dx]^2} \right) / \right. \\
 & \left(3 \left(-7(a^2-b^2) \text{AppellF1}\left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c+dx]^2, \frac{b^2\cos[c+dx]^2}{-a^2+b^2}\right] + \right. \right. \\
 & \left. \left. 2 \left(2b^2 \text{AppellF1}\left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[c+dx]^2, \frac{b^2\cos[c+dx]^2}{-a^2+b^2}\right] + \right. \right. \right. \\
 & \left. \left. (a^2-b^2) \text{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[c+dx]^2, \frac{b^2\cos[c+dx]^2}{-a^2+b^2}\right] \right) \right) \\
 & \left. \cos[c+dx]^2 \right) (a^2+b^2(-1+\cos[c+dx]^2)) \Bigg) + \\
 & \left(a \left(-2 \text{ArcTan}\left[1 - \frac{\sqrt{2}\sqrt{b}\sqrt{\cos[c+dx]}}{(a^2-b^2)^{1/4}}\right] + 2 \text{ArcTan}\left[1 + \frac{\sqrt{2}\sqrt{b}\sqrt{\cos[c+dx]}}{(a^2-b^2)^{1/4}}\right] \right) + \right. \\
 & \left. \text{Log}\left[\sqrt{a^2-b^2} - \sqrt{2}\sqrt{b}(a^2-b^2)^{1/4}\sqrt{\cos[c+dx]} + b\cos[c+dx]\right] - \right. \\
 & \left. \text{Log}\left[\sqrt{a^2-b^2} + \sqrt{2}\sqrt{b}(a^2-b^2)^{1/4}\sqrt{\cos[c+dx]} + b\cos[c+dx]\right] \right) \Bigg) / \\
 & \left(4\sqrt{2}b^{3/2}(a^2-b^2)^{1/4} \right) \sin[c+dx]^2 \Bigg)
 \end{aligned}$$

Problem 613: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{e\cos[c+dx]}(a+b\sin[c+dx])^4} dx$$

Optimal (type 4, 593 leaves, 15 steps):

$$\begin{aligned}
 & \frac{7 a \sqrt{b} (5 a^2 + 6 b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2\right)^{1 / 4} \sqrt{e}}\right]}{16\left(-a^2+b^2\right)^{15 / 4} d \sqrt{e}} + \frac{7 a \sqrt{b} (5 a^2 + 6 b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{\left(-a^2+b^2\right)^{1 / 4} \sqrt{e}}\right]}{16\left(-a^2+b^2\right)^{15 / 4} d \sqrt{e}} - \\
 & \frac{\left(57 a^2 + 20 b^2\right) \sqrt{\cos [c+d x]} \operatorname{EllipticF}\left[\frac{1}{2}(c+d x), 2\right]}{24\left(a^2-b^2\right)^3 d \sqrt{e \cos [c+d x]}} + \\
 & \left(7 a^2 (5 a^2 + 6 b^2) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]\right) / \\
 & \left(16\left(a^2-b^2\right)^3\left(a^2-b\left(b-\sqrt{-a^2+b^2}\right)\right) d \sqrt{e \cos [c+d x]}\right) + \\
 & \left(7 a^2 (5 a^2 + 6 b^2) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]\right) / \\
 & \left(16\left(a^2-b^2\right)^3\left(a^2-b\left(b+\sqrt{-a^2+b^2}\right)\right) d \sqrt{e \cos [c+d x]}\right) + \frac{b \sqrt{e \cos [c+d x]}}{3\left(a^2-b^2\right) d e\left(a+b \sin [c+d x]\right)^3} + \\
 & \frac{11 a b \sqrt{e \cos [c+d x]}}{12\left(a^2-b^2\right)^2 d e\left(a+b \sin [c+d x]\right)^2} + \frac{b\left(57 a^2 + 20 b^2\right) \sqrt{e \cos [c+d x]}}{24\left(a^2-b^2\right)^3 d e\left(a+b \sin [c+d x]\right)}
 \end{aligned}$$

Result (type 6, 1276 leaves):

$$\begin{aligned}
 & \left(\cos [c+d x]\left(\frac{b}{3\left(a^2-b^2\right)\left(a+b \sin [c+d x]\right)^3} + \frac{11 a b}{12\left(a^2-b^2\right)^2\left(a+b \sin [c+d x]\right)^2} + \frac{b\left(57 a^2 + 20 b^2\right)}{24\left(a^2-b^2\right)^3\left(a+b \sin [c+d x]\right)}\right) / \\
 & \left(d \sqrt{e \cos [c+d x]}\right) + \frac{1}{48\left(a-b\right)^3\left(a+b\right)^3 d \sqrt{e \cos [c+d x]}} \sqrt{\cos [c+d x]} \\
 & \left(-\frac{1}{\sqrt{1-\cos [c+d x]^2}\left(a+b \sin [c+d x]\right)} - 2\left(48 a^3 + 106 a b^2\right)\left(a+b \sqrt{1-\cos [c+d x]^2}\right)\right. \\
 & \left.\left(\left(5 a\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] \sqrt{\cos [c+d x]}\right) / \right.\right. \\
 & \left.\left(\sqrt{1-\cos [c+d x]^2}\right)\right. \\
 & \left.\left(5\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{1}{4}, \frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] - 2\right.\right. \\
 & \left.\left(2 b^2 \operatorname{AppellF1}\left[\frac{5}{4}, \frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right] + \left(-a^2+b^2\right)\right.\right. \\
 & \left.\left.\operatorname{AppellF1}\left[\frac{5}{4}, \frac{3}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2}\right]\right) \cos [c+d x]^2\right) \\
 & \left.\left(a^2+b^2\left(-1+\cos [c+d x]^2\right)\right)\right) - \frac{1}{\left(-a^2+b^2\right)^{3 / 4}}\left(\frac{1}{8}-\frac{i}{8}\right) \sqrt{b}
 \end{aligned}$$

$$\begin{aligned}
& \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i) \sqrt{b} \sqrt{\cos [c+d x]}}{(-a^2+b^2)^{1/4}} \right] \right) + \\
& \left(\operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] - \right. \\
& \left. \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i) \sqrt{b} (-a^2+b^2)^{1/4} \sqrt{\cos [c+d x]} + i b \cos [c+d x] \right] \right) \\
& \operatorname{Sin} [c+d x] - \frac{1}{(1-\cos [c+d x]^2) (a+b \operatorname{Sin} [c+d x])} \\
& 2 (-57 a^2 b - 20 b^3) \left(a + b \sqrt{1-\cos [c+d x]^2} \right) \\
& \left(\left(5 b (a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right. \right. \\
& \left. \left. \sqrt{\cos [c+d x]} \sqrt{1-\cos [c+d x]^2} \right) / \right. \\
& \left(\left(-5 (a^2-b^2) \operatorname{AppellF1} \left[\frac{1}{4}, -\frac{1}{2}, 1, \frac{5}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
& \left. \left(2 b^2 \operatorname{AppellF1} \left[\frac{5}{4}, -\frac{1}{2}, 2, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \\
& \left. \left. (a^2-b^2) \operatorname{AppellF1} \left[\frac{5}{4}, \frac{1}{2}, 1, \frac{9}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \right) \\
& \left. \cos [c+d x]^2 \right) (a^2+b^2 (-1+\cos [c+d x]^2)) \left. \right) + \\
& \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{(a^2-b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2} \sqrt{b} \sqrt{\cos [c+d x]}}{(a^2-b^2)^{1/4}} \right] - \right. \right. \\
& \left. \operatorname{Log} \left[\sqrt{a^2-b^2} - \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [c+d x]} + b \cos [c+d x] \right] + \right. \\
& \left. \left. \operatorname{Log} \left[\sqrt{a^2-b^2} + \sqrt{2} \sqrt{b} (a^2-b^2)^{1/4} \sqrt{\cos [c+d x]} + b \cos [c+d x] \right] \right) \right) / \\
& \left(4 \sqrt{2} \sqrt{b} (a^2-b^2)^{3/4} \right) \operatorname{Sin} [c+d x]^2 \left. \right)
\end{aligned}$$

Problem 614: Result unnecessarily involves higher level functions and more than twice size of optimal antiderivative.

$$\int \frac{1}{(e \cos [c+d x])^{3/2} (a+b \operatorname{Sin} [c+d x])^4} dx$$

Optimal (type 4, 674 leaves, 16 steps):

$$\begin{aligned}
 & - \frac{15 a b^{3/2} (7 a^2 + 6 b^2) \operatorname{ArcTan}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 (-a^2+b^2)^{17/4} d e^{3/2}} + \frac{15 a b^{3/2} (7 a^2 + 6 b^2) \operatorname{ArcTanh}\left[\frac{\sqrt{b} \sqrt{e \cos [c+d x]}}{(-a^2+b^2)^{1/4} \sqrt{e}}\right]}{16 (-a^2+b^2)^{17/4} d e^{3/2}} \\
 & - \frac{(16 a^4 + 151 a^2 b^2 + 28 b^4) \sqrt{e \cos [c+d x]} \operatorname{EllipticE}\left[\frac{1}{2}(c+d x), 2\right]}{8 (a^2-b^2)^4 d e^2 \sqrt{\cos [c+d x]}} \\
 & \left(\frac{15 a^2 b (7 a^2 + 6 b^2) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b-\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{16 (a^2-b^2)^4 (b-\sqrt{-a^2+b^2}) d e \sqrt{e \cos [c+d x]}} \right) / \\
 & \left(\frac{15 a^2 b (7 a^2 + 6 b^2) \sqrt{\cos [c+d x]} \operatorname{EllipticPi}\left[\frac{2 b}{b+\sqrt{-a^2+b^2}}, \frac{1}{2}(c+d x), 2\right]}{16 (a^2-b^2)^4 (b+\sqrt{-a^2+b^2}) d e \sqrt{e \cos [c+d x]}} \right) / \\
 & \frac{b}{3 (a^2-b^2) d e \sqrt{e \cos [c+d x]} (a+b \sin [c+d x])^3} + \\
 & \frac{13 a b}{12 (a^2-b^2)^2 d e \sqrt{e \cos [c+d x]} (a+b \sin [c+d x])^2} + \\
 & \frac{b (89 a^2 + 28 b^2)}{24 (a^2-b^2)^3 d e \sqrt{e \cos [c+d x]} (a+b \sin [c+d x])} - \\
 & \frac{15 a b (7 a^2 + 6 b^2) - (16 a^4 + 151 a^2 b^2 + 28 b^4) \sin [c+d x]}{8 (a^2-b^2)^4 d e \sqrt{e \cos [c+d x]}}
 \end{aligned}$$

Result (type 6, 1390 leaves):

$$\begin{aligned}
 & - \frac{1}{16 (a-b)^4 (a+b)^4 d (e \cos [c+d x])^{3/2}} \\
 & \cos [c+d x]^{3/2} \left(\frac{1}{12 \sqrt{1-\cos [c+d x]^2} (a+b \sin [c+d x])} (16 a^5 + 256 a^3 b^2 + 118 a b^4) \right. \\
 & \left. \left(a+b \sqrt{1-\cos [c+d x]^2} \right) \left(- \left(\left(56 a (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \cos [c+d x]^{3/2} \right) / \left(\sqrt{1-\cos [c+d x]^2} \right) \right. \right. \\
 & \left. \left. \left(7 (a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{4}, \frac{1}{2}, 1, \frac{7}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] - \right. \right. \right. \\
 & \left. \left. \left. 2 \left(2 b^2 \operatorname{AppellF1}\left[\frac{7}{4}, \frac{1}{2}, 2, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] + \right. \right. \right. \right. \\
 & \left. \left. \left. (-a^2+b^2) \operatorname{AppellF1}\left[\frac{7}{4}, \frac{3}{2}, 1, \frac{11}{4}, \cos [c+d x]^2, \frac{b^2 \cos [c+d x]^2}{-a^2+b^2} \right] \right) \right) \right) \\
 & \left. \left. \left. \cos [c+d x]^2 \right) (a^2+b^2 (-1+\cos [c+d x]^2)) \right) \right) \right) -
 \end{aligned}$$

$$\begin{aligned}
 & \left((3 + 3i) \left(2 \operatorname{ArcTan} \left[1 - \frac{(1+i)\sqrt{b}\sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}} \right] - 2 \operatorname{ArcTan} \left[1 + \frac{(1+i)\sqrt{b}\sqrt{\cos[c+dx]}}{(-a^2+b^2)^{1/4}} \right] - \operatorname{Log} \left[\sqrt{-a^2+b^2} - (1+i)\sqrt{b}(-a^2+b^2)^{1/4} \sqrt{\cos[c+dx]} + i b \cos[c+dx] \right] + \operatorname{Log} \left[\sqrt{-a^2+b^2} + (1+i)\sqrt{b}(-a^2+b^2)^{1/4} \sqrt{\cos[c+dx]} + i b \cos[c+dx] \right] \right) \right) / \left(\sqrt{b}(-a^2+b^2)^{1/4} \right) \sin[c+dx] - \\
 & \frac{1}{(1 - \cos[c+dx]^2)(a+b\sin[c+dx])} 2(16a^4b + 151a^2b^3 + 28b^5) \\
 & \left(a + b\sqrt{1 - \cos[c+dx]^2} \right) \\
 & \left(\left(7b(a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] \right. \right. \\
 & \left. \left. \cos[c+dx]^{3/2} \sqrt{1 - \cos[c+dx]^2} \right) / \right. \\
 & \left(3 \left(-7(a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{4}, -\frac{1}{2}, 1, \frac{7}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] + 2 \right. \right. \\
 & \left. \left(2b^2 \operatorname{AppellF1} \left[\frac{7}{4}, -\frac{1}{2}, 2, \frac{11}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] + \right. \right. \\
 & \left. \left. (a^2 - b^2) \operatorname{AppellF1} \left[\frac{7}{4}, \frac{1}{2}, 1, \frac{11}{4}, \cos[c+dx]^2, \frac{b^2 \cos[c+dx]^2}{-a^2+b^2} \right] \right) \right) \\
 & \left. \cos[c+dx]^2 \right) (a^2 + b^2(-1 + \cos[c+dx]^2)) \Big) + \\
 & \left(a \left(-2 \operatorname{ArcTan} \left[1 - \frac{\sqrt{2}\sqrt{b}\sqrt{\cos[c+dx]}}{(a^2 - b^2)^{1/4}} \right] + 2 \operatorname{ArcTan} \left[1 + \frac{\sqrt{2}\sqrt{b}\sqrt{\cos[c+dx]}}{(a^2 - b^2)^{1/4}} \right] \right) + \right. \\
 & \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} - \sqrt{2}\sqrt{b}(a^2 - b^2)^{1/4} \sqrt{\cos[c+dx]} + b \cos[c+dx] \right] - \right. \\
 & \left. \operatorname{Log} \left[\sqrt{a^2 - b^2} + \sqrt{2}\sqrt{b}(a^2 - b^2)^{1/4} \sqrt{\cos[c+dx]} + \right. \right. \\
 & \left. \left. b \cos[c+dx] \right] \right) / \left(4\sqrt{2}b^{3/2}(a^2 - b^2)^{1/4} \right) \sin[c+dx]^2 \Big) + \\
 & \left(\cos[c+dx]^2 \left(-\frac{b^3 \cos[c+dx]}{3(a^2 - b^2)^2(a+b\sin[c+dx])^3} - \frac{7ab^3 \cos[c+dx]}{4(a^2 - b^2)^3(a+b\sin[c+dx])^2} + \right. \right. \\
 & \left. \left. \frac{-55a^2b^3 \cos[c+dx] - 12b^5 \cos[c+dx]}{8(a^2 - b^2)^4(a+b\sin[c+dx])} + \right. \right. \\
 & \frac{1}{(a^2 - b^2)^4} \\
 & 2 \\
 & \operatorname{Sec}[c+dx] \\
 & \left. (-4a^3b - 4ab^3 + a^4 \sin[c+dx] + 6a^2b^2 \sin[c+dx]) + \right.
 \end{aligned}$$

$$b^4 \sin[c + dx] \Big) \Big) \Big) / \left(d (e \cos[c + dx])^{3/2} \right)$$

Problem 615: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{\sqrt{c \cos[e + fx]} \sqrt{a + b \sin[e + fx]}} dx$$

Optimal (type 4, 183 leaves, 2 steps):

$$\left(2 \sqrt{2} (-a + b)^{1/4} \sqrt{c \cos[e + fx]} \right. \\ \left. \text{EllipticF} \left[\text{ArcSin} \left[\frac{(a + b)^{1/4} \sqrt{\frac{1 + \cos[e + fx] + \sin[e + fx]}{1 + \cos[e + fx] - \sin[e + fx]}}}{(-a + b)^{1/4}} \right], -1 \right] \sqrt{\frac{a + b \sin[e + fx]}{(a - b)(1 - \sin[e + fx])}} \right) / \\ \left((a + b)^{1/4} c f \sqrt{\frac{1 + \cos[e + fx] + \sin[e + fx]}{1 + \cos[e + fx] - \sin[e + fx]}} \sqrt{a + b \sin[e + fx]} \right)$$

Result (type 4, 4001 leaves):

$$- \left(\left(4 \cos \left[\frac{1}{2} (e + fx) \right] \right)^2 \text{EllipticF} \left[\text{ArcSin} \left[\sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2}) (1 + \tan \left[\frac{1}{2} (e + fx) \right])}{(a - b + \sqrt{-a^2 + b^2}) (-1 + \tan \left[\frac{1}{2} (e + fx) \right])}} \right], -1 \right] \right. \\ \left. (-1 + \tan \left[\frac{1}{2} (e + fx) \right]) \left(1 + \tan \left[\frac{1}{2} (e + fx) \right] \right) \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \tan \left[\frac{1}{2} (e + fx) \right]}{(a - b + \sqrt{-a^2 + b^2}) (-1 + \tan \left[\frac{1}{2} (e + fx) \right])}} \right. \\ \left. \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \tan \left[\frac{1}{2} (e + fx) \right]}{(-a + b + \sqrt{-a^2 + b^2}) (-1 + \tan \left[\frac{1}{2} (e + fx) \right])}} \right) / \left(f \sqrt{\cos[e + fx]} \right. \\ \left. \sqrt{c \cos[e + fx]} (a + b \sin[e + fx]) \sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2}) (1 + \tan \left[\frac{1}{2} (e + fx) \right])}{(a - b + \sqrt{-a^2 + b^2}) (-1 + \tan \left[\frac{1}{2} (e + fx) \right])}} \right. \\ \left. \left(- \left(\left(2 \text{EllipticF} \left[\text{ArcSin} \left[\sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2}) (1 + \tan \left[\frac{1}{2} (e + fx) \right])}{(a - b + \sqrt{-a^2 + b^2}) (-1 + \tan \left[\frac{1}{2} (e + fx) \right])}} \right], -1 \right] \right) \right) \right)$$

$$\begin{aligned}
 & \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right] \right) \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \tan\left[\frac{1}{2}(e+fx)\right]}{(a-b + \sqrt{-a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)}} \\
 & \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \tan\left[\frac{1}{2}(e+fx)\right]}{(-a+b + \sqrt{-a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)}} \Big/ \\
 & \left(\sqrt{\cos[e+fx]} \sqrt{a+b \sin[e+fx]} \sqrt{\frac{(-a-b + \sqrt{-a^2 + b^2}) \left(1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)}{(a-b + \sqrt{-a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)}} \right) - \\
 & \left(2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a-b + \sqrt{-a^2 + b^2}) \left(1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)}{(a-b + \sqrt{-a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)}}\right], -1\right] \right. \\
 & \left. \left(1 + \tan\left[\frac{1}{2}(e+fx)\right]\right) \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \tan\left[\frac{1}{2}(e+fx)\right]}{(a-b + \sqrt{-a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)}} \right. \\
 & \left. \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \tan\left[\frac{1}{2}(e+fx)\right]}{(-a+b + \sqrt{-a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)}} \Big/ \right. \\
 & \left. \left(\sqrt{\cos[e+fx]} \sqrt{a+b \sin[e+fx]} \sqrt{\frac{(-a-b + \sqrt{-a^2 + b^2}) \left(1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)}{(a-b + \sqrt{-a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)}} \right) + \\
 & \left(2b \cos\left[\frac{1}{2}(e+fx)\right] \right)^2 \sqrt{\cos[e+fx]} \operatorname{EllipticF}\left[\right. \\
 & \left. \operatorname{ArcSin}\left[\sqrt{\frac{(-a-b + \sqrt{-a^2 + b^2}) \left(1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)}{(a-b + \sqrt{-a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)}}\right], -1\right] \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]\right) \right. \\
 & \left. \left(1 + \tan\left[\frac{1}{2}(e+fx)\right]\right) \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \tan\left[\frac{1}{2}(e+fx)\right]}{(a-b + \sqrt{-a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)}} \right. \\
 & \left. \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \tan\left[\frac{1}{2}(e+fx)\right]}{(-a+b + \sqrt{-a^2 + b^2}) \left(-1 + \tan\left[\frac{1}{2}(e+fx)\right]\right)}} \Big/ \right)
 \end{aligned}$$

$$\begin{aligned}
 & \left((a + b \sin[ex + fx])^{3/2} \sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2})(1 + \tan[\frac{1}{2}(ex + fx)])}{(a - b + \sqrt{-a^2 + b^2})(-1 + \tan[\frac{1}{2}(ex + fx)])}} \right) + \\
 & \left(4 \cos[\frac{1}{2}(ex + fx)] \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2})(1 + \tan[\frac{1}{2}(ex + fx)])}{(a - b + \sqrt{-a^2 + b^2})(-1 + \tan[\frac{1}{2}(ex + fx)])}}\right]} \right], \right. \\
 & \quad \left. -1\right] \sin[\frac{1}{2}(ex + fx)] \left(-1 + \tan[\frac{1}{2}(ex + fx)]\right) \\
 & \quad \left(1 + \tan[\frac{1}{2}(ex + fx)]\right) \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \tan[\frac{1}{2}(ex + fx)]}{(a - b + \sqrt{-a^2 + b^2})(-1 + \tan[\frac{1}{2}(ex + fx)])}} \\
 & \quad \left. \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \tan[\frac{1}{2}(ex + fx)]}{(-a + b + \sqrt{-a^2 + b^2})(-1 + \tan[\frac{1}{2}(ex + fx)])}} \right) / \\
 & \left(\sqrt{\cos[ex + fx]} \sqrt{a + b \sin[ex + fx]} \sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2})(1 + \tan[\frac{1}{2}(ex + fx)])}{(a - b + \sqrt{-a^2 + b^2})(-1 + \tan[\frac{1}{2}(ex + fx)])}} \right) - \\
 & \left(2 \cos[\frac{1}{2}(ex + fx)]^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2})(1 + \tan[\frac{1}{2}(ex + fx)])}{(a - b + \sqrt{-a^2 + b^2})(-1 + \tan[\frac{1}{2}(ex + fx)])}}\right]} \right], \right. \\
 & \quad \left. -1\right] \sin[ex + fx] \left(-1 + \tan[\frac{1}{2}(ex + fx)]\right) \\
 & \quad \left(1 + \tan[\frac{1}{2}(ex + fx)]\right) \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \tan[\frac{1}{2}(ex + fx)]}{(a - b + \sqrt{-a^2 + b^2})(-1 + \tan[\frac{1}{2}(ex + fx)])}} \\
 & \quad \left. \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \tan[\frac{1}{2}(ex + fx)]}{(-a + b + \sqrt{-a^2 + b^2})(-1 + \tan[\frac{1}{2}(ex + fx)])}} \right) / \\
 & \left(\cos[ex + fx]^{3/2} \sqrt{a + b \sin[ex + fx]} \sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2})(1 + \tan[\frac{1}{2}(ex + fx)])}{(a - b + \sqrt{-a^2 + b^2})(-1 + \tan[\frac{1}{2}(ex + fx)])}} \right) + \\
 & \left(2 \cos[\frac{1}{2}(ex + fx)]^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a - b + \sqrt{-a^2 + b^2})(1 + \tan[\frac{1}{2}(ex + fx)])}{(a - b + \sqrt{-a^2 + b^2})(-1 + \tan[\frac{1}{2}(ex + fx)])}}\right]} \right], \right.
 \end{aligned}$$

$$\begin{aligned}
 & -1] \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right) \\
 & \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}{(a - b + \sqrt{-a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right)}} \\
 & \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}{(-a + b + \sqrt{-a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right)}} \\
 & \left(\frac{(-a - b + \sqrt{-a^2 + b^2}) \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2}{2(a - b + \sqrt{-a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right)} - \right. \\
 & \left. \left((-a - b + \sqrt{-a^2 + b^2}) \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right) \right) \right) / \\
 & \left. \left(2(a - b + \sqrt{-a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right)^2 \right) \right) / \\
 & \left(\sqrt{\operatorname{Cos}[e + f x]} \sqrt{a + b \operatorname{Sin}[e + f x]} \left(\frac{(-a - b + \sqrt{-a^2 + b^2}) \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right)}{(a - b + \sqrt{-a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right)} \right)^{3/2} \right) - \\
 & \left(2(a - b + \sqrt{-a^2 + b^2}) \operatorname{Cos}\left[\frac{1}{2}(e + f x)\right]^2 \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right)^2 \right. \\
 & \sqrt{\frac{b - \sqrt{-a^2 + b^2} + a \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}{(a - b + \sqrt{-a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right)}} \\
 & \sqrt{-\frac{b + \sqrt{-a^2 + b^2} + a \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right]}{(-a + b + \sqrt{-a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right)}} \\
 & \left(\frac{(-a - b + \sqrt{-a^2 + b^2}) \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2}{2(a - b + \sqrt{-a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right)} - \right. \\
 & \left. \left((-a - b + \sqrt{-a^2 + b^2}) \operatorname{Sec}\left[\frac{1}{2}(e + f x)\right]^2 \left(1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right) \right) \right) / \\
 & \left. \left(2(a - b + \sqrt{-a^2 + b^2}) \left(-1 + \operatorname{Tan}\left[\frac{1}{2}(e + f x)\right] \right)^2 \right) \right) / \left((-a - b + \sqrt{-a^2 + b^2}) \right)
 \end{aligned}$$

$$\begin{aligned}
 & \sqrt{\cos[e+fx]} \sqrt{a+b \sin[e+fx]} \sqrt{1 - \frac{(-a-b+\sqrt{-a^2+b^2})(1+\tan[\frac{1}{2}(e+fx)])}{(a-b+\sqrt{-a^2+b^2})(-1+\tan[\frac{1}{2}(e+fx)])}} \\
 & \sqrt{1 + \frac{(-a-b+\sqrt{-a^2+b^2})(1+\tan[\frac{1}{2}(e+fx)])}{(a-b+\sqrt{-a^2+b^2})(-1+\tan[\frac{1}{2}(e+fx)])}} - \\
 & \left(2 \cos\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a-b+\sqrt{-a^2+b^2})(1+\tan[\frac{1}{2}(e+fx)])}{(a-b+\sqrt{-a^2+b^2})(-1+\tan[\frac{1}{2}(e+fx)])}}\right]} \right], \right. \\
 & \quad \left. -1\right) \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]\right) \left(1+\tan\left[\frac{1}{2}(e+fx)\right]\right) \\
 & \sqrt{-\frac{b+\sqrt{-a^2+b^2}+a \tan\left[\frac{1}{2}(e+fx)\right]}{(a-b+\sqrt{-a^2+b^2})(-1+\tan[\frac{1}{2}(e+fx)])}} \\
 & \left(\frac{a \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{2(a-b+\sqrt{-a^2+b^2})(-1+\tan[\frac{1}{2}(e+fx)])} - \right. \\
 & \quad \left. \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2 (b-\sqrt{-a^2+b^2}+a \tan[\frac{1}{2}(e+fx)])}{2(a-b+\sqrt{-a^2+b^2})(-1+\tan[\frac{1}{2}(e+fx)])^2} \right) \Bigg) / \\
 & \left(\sqrt{\cos[e+fx]} \sqrt{a+b \sin[e+fx]} \sqrt{\frac{(-a-b+\sqrt{-a^2+b^2})(1+\tan[\frac{1}{2}(e+fx)])}{(a-b+\sqrt{-a^2+b^2})(-1+\tan[\frac{1}{2}(e+fx)])}} \right. \\
 & \quad \left. \sqrt{\frac{b-\sqrt{-a^2+b^2}+a \tan\left[\frac{1}{2}(e+fx)\right]}{(a-b+\sqrt{-a^2+b^2})(-1+\tan[\frac{1}{2}(e+fx)])}} - \right. \\
 & \left. \left(2 \cos\left[\frac{1}{2}(e+fx)\right]^2 \operatorname{EllipticF}\left[\operatorname{ArcSin}\left[\sqrt{\frac{(-a-b+\sqrt{-a^2+b^2})(1+\tan[\frac{1}{2}(e+fx)])}{(a-b+\sqrt{-a^2+b^2})(-1+\tan[\frac{1}{2}(e+fx)])}}\right]} \right], \right. \\
 & \quad \left. -1\right) \left(-1+\tan\left[\frac{1}{2}(e+fx)\right]\right) \left(1+\tan\left[\frac{1}{2}(e+fx)\right]\right) \\
 & \sqrt{\frac{b-\sqrt{-a^2+b^2}+a \tan\left[\frac{1}{2}(e+fx)\right]}{(a-b+\sqrt{-a^2+b^2})(-1+\tan[\frac{1}{2}(e+fx)])}}
 \end{aligned}$$

$$\left(\frac{a \operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2}{2(-a+b+\sqrt{-a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)} + \frac{\operatorname{Sec}\left[\frac{1}{2}(e+fx)\right]^2\left(b+\sqrt{-a^2+b^2}+a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)}{2(-a+b+\sqrt{-a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)^2} \right) \Bigg/ \left(\sqrt{\operatorname{Cos}[e+fx]} \sqrt{a+b \operatorname{Sin}[e+fx]} \sqrt{\frac{(-a-b+\sqrt{-a^2+b^2})\left(1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)}{(a-b+\sqrt{-a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)}} \sqrt{-\frac{b+\sqrt{-a^2+b^2}+a \operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]}{(-a+b+\sqrt{-a^2+b^2})\left(-1+\operatorname{Tan}\left[\frac{1}{2}(e+fx)\right]\right)}} \right) \Bigg) \Bigg) \Bigg)$$

Problem 617: Result unnecessarily involves imaginary or complex numbers.

$$\int (e \operatorname{Cos}[c+dx])^p (a+b \operatorname{Sin}[c+dx])^2 dx$$

Optimal (type 5, 157 leaves, 3 steps):

$$\frac{ab(3+p)(e \operatorname{Cos}[c+dx])^{1+p}}{de(1+p)(2+p)} - \left((b^2+a^2(2+p))(e \operatorname{Cos}[c+dx])^{1+p} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \operatorname{Cos}[c+dx]^2\right] \operatorname{Sin}[c+dx] \right) \Bigg/ \left(de(1+p)(2+p) \sqrt{\operatorname{Sin}[c+dx]^2} \right) - \frac{b(e \operatorname{Cos}[c+dx])^{1+p}(a+b \operatorname{Sin}[c+dx])}{de(2+p)}$$

Result (type 5, 288 leaves):

$$\frac{1}{d(1+p) \sqrt{\operatorname{Sin}[c+dx]^2}} (e \operatorname{Cos}[c+dx])^p \left(\frac{1}{-1+p} 2^{-p} ab(1+e^{2i(c+dx)})^{-1-p} (e^{-i(c+dx)}(1+e^{2i(c+dx)}))^{1+p} \operatorname{Cos}[c+dx]^{-p} \left(-(-1+p) \operatorname{Hypergeometric2F1}\left[\frac{1}{2}(-1-p), -p, \frac{1-p}{2}, -e^{2i(c+dx)}\right] + e^{2i(c+dx)}(1+p) \operatorname{Hypergeometric2F1}\left[\frac{1-p}{2}, -p, \frac{3-p}{2}, -e^{2i(c+dx)}\right] \right) \sqrt{\operatorname{Sin}[c+dx]^2} - \frac{1}{2} b^2 \operatorname{Hypergeometric2F1}\left[-\frac{1}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \operatorname{Cos}[c+dx]^2\right] \operatorname{Sin}[2(c+dx)] - \frac{1}{2} a^2 \operatorname{Hypergeometric2F1}\left[\frac{1}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \operatorname{Cos}[c+dx]^2\right] \operatorname{Sin}[2(c+dx)] \right)$$

Problem 618: Result unnecessarily involves complex numbers and more than

twice size of optimal antiderivative.

$$\int (e \cos [c+d x])^p (a+b \sin [c+d x]) dx$$

Optimal (type 5, 97 leaves, 2 steps):

$$-\frac{b (e \cos [c+d x])^{1+p}}{d e (1+p)} - \left(a (e \cos [c+d x])^{1+p} \operatorname{Hypergeometric2F1} \left[\frac{1}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \cos [c+d x]^2 \right] \sin [c+d x] \right) / \left(d e (1+p) \sqrt{\sin [c+d x]^2} \right)$$

Result (type 5, 233 leaves):

$$\frac{1}{2 d (1+p)} (e \cos [c+d x])^p \left(\frac{1}{-1+p} 2^{-p} b (1+e^{2 i (c+d x)})^{-1-p} (e^{-i (c+d x)} (1+e^{2 i (c+d x)}))^{1+p} \cos [c+d x]^{-p} \right. \\ \left. - (-1+p) \operatorname{Hypergeometric2F1} \left[\frac{1}{2} (-1-p), -p, \frac{1-p}{2}, -e^{2 i (c+d x)} \right] + e^{2 i (c+d x)} (1+p) \operatorname{Hypergeometric2F1} \left[\frac{1-p}{2}, -p, \frac{3-p}{2}, -e^{2 i (c+d x)} \right] \right) - \frac{a \operatorname{Hypergeometric2F1} \left[\frac{1}{2}, \frac{1+p}{2}, \frac{3+p}{2}, \cos [c+d x]^2 \right] \sin [2 (c+d x)]}{\sqrt{\sin [c+d x]^2}}$$

Problem 619: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c+d x])^p}{a+b \sin [c+d x]} dx$$

Optimal (type 6, 158 leaves, 1 step):

$$-\frac{1}{b d (1-p)} e \operatorname{AppellF1} \left[1-p, \frac{1-p}{2}, \frac{1-p}{2}, 2-p, \frac{a+b}{a+b \sin [c+d x]}, \frac{a-b}{a+b \sin [c+d x]} \right] \\ (e \cos [c+d x])^{-1+p} \left(-\frac{b (1-\sin [c+d x])}{a+b \sin [c+d x]} \right)^{\frac{1-p}{2}} \left(\frac{b (1+\sin [c+d x])}{a+b \sin [c+d x]} \right)^{\frac{1-p}{2}}$$

Result (type 6, 6000 leaves):

$$\left(a^2 (e \cos [c+d x])^p \tan [c+d x] (1+\tan [c+d x]^2)^{-1-\frac{p}{2}} \left(b \tan [c+d x] + a \sqrt{1+\tan [c+d x]^2} \right) \right. \\ \left. - \left(\left(3 a \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] \sqrt{1+\tan [c+d x]^2} \right) / \right. \right. \\ \left. \left. - 3 a^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + 2 (a^2 - b^2) \right) \right)$$

$$\begin{aligned}
 & \text{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\text{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c+dx]^2\right] + a^2 p \text{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\text{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c+dx]^2\right] \right) \text{Tan}[c+dx]^2 \Bigg) + \\
 & \left(2 b \text{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\text{Tan}[c+dx]^2, \frac{(-a^2+b^2) \text{Tan}[c+dx]^2}{a^2}\right] \text{Tan}[c+dx] \right) / \\
 & \left(-4 a^2 \text{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\text{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c+dx]^2\right] + \right. \\
 & \left. \left(2 (a^2 - b^2) \text{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\text{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c+dx]^2\right] + a^2 (1+p) \right. \right. \\
 & \left. \left. \text{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\text{Tan}[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c+dx]^2\right] \right) \text{Tan}[c+dx]^2 \right) \Bigg) / \\
 & \left(d (a + b \text{Sin}[c + dx]) \left(a + \frac{b \text{Tan}[c + dx]}{\sqrt{1 + \text{Tan}[c + dx]^2}} \right) (-b^2 \text{Tan}[c + dx]^2 + \right. \\
 & \left. a^2 (1 + \text{Tan}[c + dx]^2)) \right. \\
 & \left[- \frac{1}{\left(a + \frac{b \text{Tan}[c + dx]}{\sqrt{1 + \text{Tan}[c + dx]^2}} \right) (-b^2 \text{Tan}[c + dx]^2 + a^2 (1 + \text{Tan}[c + dx]^2))^2} \right. \\
 & \left. a^2 \text{Tan}[c + dx] (2 a^2 \text{Sec}[c + dx]^2 \text{Tan}[c + dx] - 2 b^2 \text{Sec}[c + dx]^2 \text{Tan}[c + dx]) \right. \\
 & \left. (1 + \text{Tan}[c + dx]^2)^{-1-\frac{p}{2}} \left(b \text{Tan}[c + dx] + a \sqrt{1 + \text{Tan}[c + dx]^2} \right) \right. \\
 & \left. \left(- \left(\left(3 a \text{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\text{Tan}[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + dx]^2\right] \right. \right. \right. \right. \\
 & \left. \left. \left. \sqrt{1 + \text{Tan}[c + dx]^2} \right) / \left(-3 a^2 \text{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\text{Tan}[c + dx]^2, \right. \right. \right. \right. \\
 & \left. \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + dx]^2\right] + \left(2 (a^2 - b^2) \text{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. -\text{Tan}[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + dx]^2\right] + a^2 p \text{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, \right. \right. \right. \right. \\
 & \left. \left. \left. 1, \frac{5}{2}, -\text{Tan}[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + dx]^2\right] \right) \text{Tan}[c + dx]^2 \right) \right) + \\
 & \left(2 b \text{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\text{Tan}[c + dx]^2, \frac{(-a^2+b^2) \text{Tan}[c + dx]^2}{a^2}\right] \text{Tan}[c + dx] \right) / \\
 & \left(-4 a^2 \text{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\text{Tan}[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + dx]^2\right] + \right. \\
 & \left. \left(2 (a^2 - b^2) \text{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\text{Tan}[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \text{Tan}[c + dx]^2\right] + \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & a^2 (1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\tan[c+dx]^2, \right. \\
 & \quad \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \tan[c+dx]^2 \Bigg) + \\
 & \frac{1}{\left(a + \frac{b \tan[c+dx]}{\sqrt{1+\tan[c+dx]^2}}\right) \left(-b^2 \tan[c+dx]^2 + a^2 (1+\tan[c+dx]^2)\right)} a^2 \tan[c+dx] \\
 & \quad \left(1 + \tan[c+dx]^2\right)^{-1-\frac{p}{2}} \left(b \sec[c+dx]^2 + \frac{a \sec[c+dx]^2 \tan[c+dx]}{\sqrt{1+\tan[c+dx]^2}}\right) \\
 & \quad \left(-\left(\left(3 a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \sqrt{1+\tan[c+dx]^2}\right) / \left(-3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c+dx]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right] + \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, \right. \right. \right. \right. \right. \\
 & \quad \left. \left. \left. -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right] + a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1, \frac{5}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \right) \tan[c+dx]^2\right) \Bigg) + \\
 & \quad \left(2 b \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[c+dx]^2, \frac{(-a^2+b^2) \tan[c+dx]^2}{a^2}\right] \tan[c+dx]\right) / \\
 & \quad \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right] + \right. \\
 & \quad \left. \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right] + \right. \right. \\
 & \quad \left. \left. a^2 (1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\tan[c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \right) \tan[c+dx]^2\right) \Bigg) - \\
 & \frac{1}{\left(a + \frac{b \tan[c+dx]}{\sqrt{1+\tan[c+dx]^2}}\right)^2 \left(-b^2 \tan[c+dx]^2 + a^2 (1+\tan[c+dx]^2)\right)} \\
 & a^2 \tan[c+dx] \left(1 + \tan[c+dx]^2\right)^{-1-\frac{p}{2}} \\
 & \quad \left(-\frac{b \sec[c+dx]^2 \tan[c+dx]^2}{\left(1 + \tan[c+dx]^2\right)^{3/2}} + \frac{b \sec[c+dx]^2}{\sqrt{1+\tan[c+dx]^2}}\right) \\
 & \quad \left(b \tan[c+dx] + a \sqrt{1+\tan[c+dx]^2}\right) \\
 & \quad \left(-\left(\left(3 a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \right. \right. \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& \sqrt{1 + \tan[c + dx]^2} \Big/ \left(-3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c + dx]^2, \right. \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] + \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] + a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, \right. \right. \right. \\
& \quad \left. \left. \left. 1, \frac{5}{2}, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] \right) \tan[c + dx]^2 \right) \Big/ \\
& \left(2 b \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[c + dx]^2, \frac{(-a^2 + b^2) \tan[c + dx]^2}{a^2}\right] \tan[c + dx] \right) \Big/ \\
& \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] + \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] + \right. \\
& \quad \left. a^2 (1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\tan[c + dx]^2, \right. \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] \right) \tan[c + dx]^2 \right) \Big/ \\
& \quad 1 \\
& \left(a + \frac{b \tan[c + dx]}{\sqrt{1 + \tan[c + dx]^2}} \right) \left(-b^2 \tan[c + dx]^2 + a^2 (1 + \tan[c + dx]^2) \right) \\
& 2 a^2 \left(-1 - \frac{p}{2} \right) \operatorname{Sec}[c + dx]^2 \\
& \tan[c + dx]^2 (1 + \tan[c + dx]^2)^{-2 - \frac{p}{2}} \\
& \left(b \tan[c + dx] + a \sqrt{1 + \tan[c + dx]^2} \right) \\
& \left(- \left(\left(3 a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] \right. \right. \right. \right. \\
& \quad \left. \left. \left. \sqrt{1 + \tan[c + dx]^2} \right) \Big/ \left(-3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c + dx]^2, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] + \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] + a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, \right. \right. \right. \right. \\
& \quad \left. \left. \left. \left. 1, \frac{5}{2}, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] \right) \tan[c + dx]^2 \right) \right) \Big/ \\
& \left(2 b \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[c + dx]^2, \frac{(-a^2 + b^2) \tan[c + dx]^2}{a^2}\right] \tan[c + dx] \right) \Big/ \\
& \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] + \right. \\
& \quad \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\tan[c + dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2\right] + \right. \\
& \quad \left. \left. \left(-1 + \frac{b^2}{a^2}\right) \tan[c + dx]^2 \right) \tan[c + dx]^2 \right) \Big/
\end{aligned}$$

$$a^2 (1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \tan[c+dx]^2 \Bigg) +$$

 1

$$\left(a + \frac{b \tan[c+dx]}{\sqrt{1+\tan[c+dx]^2}}\right) \left(-b^2 \tan[c+dx]^2 + a^2 (1 + \tan[c+dx]^2)\right)$$

$$a^2 \operatorname{Sec}[c+dx]^2$$

$$(1 + \tan[c+dx]^2)^{-1-\frac{p}{2}}$$

$$\left(b \tan[c+dx] + a \sqrt{1 + \tan[c+dx]^2}\right)$$

$$\left(-\left(\left(3 a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right]\right.\right.\right.$$

$$\left.\left.\left.\sqrt{1 + \tan[c+dx]^2}\right)\right) / \left(-3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c+dx]^2, \right.\right.$$

$$\left.\left.\left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right] + \left(2 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, \right.\right.\right.$$

$$\left.\left.\left.-\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right] + a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, \right.\right.$$

$$\left.\left.\left.1, \frac{5}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right]\right) \tan[c+dx]^2 \Bigg) +$$

$$\left(2 b \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[c+dx]^2, \frac{(-a^2 + b^2) \tan[c+dx]^2}{a^2}\right] \tan[c+dx]\right) /$$

$$\left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right] + \right.$$

$$\left(2 (a^2 - b^2) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right] + \right.$$

$$a^2 (1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\tan[c+dx]^2, \right.$$

$$\left.\left.\left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right]\right) \tan[c+dx]^2 \Bigg) +$$

 1

$$\left(a + \frac{b \tan[c+dx]}{\sqrt{1+\tan[c+dx]^2}}\right) \left(-b^2 \tan[c+dx]^2 + a^2 (1 + \tan[c+dx]^2)\right)$$

$$a^2 \operatorname{Tan}[c+dx]$$

$$(1 + \tan[c+dx]^2)^{-1-\frac{p}{2}}$$

$$\left(b \tan[c+dx] + a \sqrt{1 + \tan[c+dx]^2}\right)$$

$$\left(-\left(\left(3 a \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan[c+dx]^2, \left(-1 + \frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \operatorname{Sec}[c+dx]^2\right.\right.\right.$$

$$\left.\left.\left.\tan[c+dx]\right)\right) / \left(\sqrt{1 + \tan[c+dx]^2} \left(-3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, \right.\right.\right.$$

$$\begin{aligned}
 & -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right)+\left(2\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]\right) \tan [c+d x]^2\right)\right)- \\
 & \left(3 a\left(-\frac{1}{3} p \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{p}{2}, 1, \frac{5}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x]+\frac{2}{3}\left(-1+\frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x]\right) \sqrt{1+\tan [c+d x]^2}\right) / \\
 & \left(-3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+\left(2\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]\right) \tan [c+d x]^2\right)+ \\
 & \left(2 b \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan [c+d x]^2, \frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2}\right] \operatorname{Sec}[c+d x]^2\right) / \\
 & \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+\left(2\left(a^2-b^2\right) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+a^2\right.\right. \\
 & \left.\left.(1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]\right) \tan [c+d x]^2\right)+\left(2 b \tan [c+d x]\left(\frac{1}{a^2}\left(-a^2+b^2\right) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\tan [c+d x]^2, \frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2}\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x]-\right.\right. \\
 & \left.\left.\frac{1}{2}(1+p) \operatorname{AppellF1}\left[2, 1+\frac{1+p}{2}, 1, 3, -\tan [c+d x]^2, \frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2}\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x]\right)\right) / \\
 & \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+\left(2\left(a^2-b^2\right) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+a^2\right.\right. \\
 & \left.\left.(1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]\right) \tan [c+d x]^2\right)+ \\
 & \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right) \tan [c+d x]^2\right)
 \end{aligned}$$

$$\begin{aligned}
 & \left(3 a \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] \sqrt{1 + \operatorname{Tan}[c+d x]^2} \right. \\
 & \quad \left(2 \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] + \right. \right. \\
 & \quad \left. \left. a^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] \right) \right. \\
 & \quad \left. \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x] - 3 a^2 \left(-\frac{1}{3} p \operatorname{AppellF1} \left[\frac{3}{2}, 1 + \frac{p}{2}, 1, \frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x] + \right. \\
 & \quad \left. \frac{2}{3} \left(-1 + \frac{b^2}{a^2} \right) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x] \right) + \operatorname{Tan}[c+d x]^2 \left(2 (a^2 - b^2) \left(-\frac{3}{5} p \operatorname{AppellF1} \left[\frac{5}{2}, \right. \right. \right. \\
 & \quad \left. \left. 1 + \frac{p}{2}, 2, \frac{7}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] \operatorname{Sec}[c+d x]^2 \right. \\
 & \quad \left. \operatorname{Tan}[c+d x] + \frac{12}{5} \left(-1 + \frac{b^2}{a^2} \right) \operatorname{AppellF1} \left[\frac{5}{2}, \frac{p}{2}, 3, \frac{7}{2}, -\operatorname{Tan}[c+d x]^2, \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x] \right) + a^2 p \left(\frac{6}{5} \left(-1 + \frac{b^2}{a^2} \right) \right. \\
 & \quad \left. \operatorname{AppellF1} \left[\frac{5}{2}, \frac{2+p}{2}, 2, \frac{7}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] \right. \\
 & \quad \left. \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x] - \frac{3}{5} (2+p) \operatorname{AppellF1} \left[\frac{5}{2}, 1 + \frac{2+p}{2}, 1, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x] \right) \right) \right) \Bigg) / \\
 & \left(-3 a^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] + \right. \\
 & \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] + \right. \\
 & \quad \left. a^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\operatorname{Tan}[c+d x]^2, \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] \right) \operatorname{Tan}[c+d x]^2 \right)^2 - \\
 & \left(2 b \operatorname{AppellF1} \left[1, \frac{1+p}{2}, 1, 2, -\operatorname{Tan}[c+d x]^2, \frac{(-a^2 + b^2) \operatorname{Tan}[c+d x]^2}{a^2} \right] \operatorname{Tan}[c+d x] \right. \\
 & \quad \left(2 \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[2, \frac{1+p}{2}, 2, 3, -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] + \right. \right. \\
 & \quad \left. \left. a^2 (1+p) \operatorname{AppellF1} \left[2, \frac{3+p}{2}, 1, 3, -\operatorname{Tan}[c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \operatorname{Tan}[c+d x]^2 \right] \right) \right. \\
 & \quad \left. \operatorname{Sec}[c+d x]^2 \operatorname{Tan}[c+d x] - 4 a^2 \left(\left(-1 + \frac{b^2}{a^2} \right) \operatorname{AppellF1} \left[2, \frac{1+p}{2}, 2, 3, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2] \operatorname{Sec}[c+d x]^2 \tan [c+d x] - \\
 & \frac{1}{2}(1+p) \operatorname{AppellF1}\left[2, 1+\frac{1+p}{2}, 1, 3, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \\
 & \operatorname{Sec}[c+d x]^2 \tan [c+d x] + \tan [c+d x]^2\left(2\left(a^2-b^2\right)\left(\frac{8}{3}\left(-1+\frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[3, \frac{1+p}{2}, 3, 4, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \operatorname{Sec}[c+d x]^2\right.\right. \\
 & \left.\left.\tan [c+d x]-\frac{2}{3}(1+p) \operatorname{AppellF1}\left[3, 1+\frac{1+p}{2}, 2, 4, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x]\right)+a^2(1+p)\left(\frac{4}{3}\left(-1+\frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[3, \frac{3+p}{2}, 2, 4, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x]-\frac{2}{3}(3+p) \operatorname{AppellF1}\left[3, 1+\frac{3+p}{2}, 1, 4, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x]\right)\right)\right) / \\
 & \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1+p}{2}, 1, 2, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+2\left(a^2-b^2\right) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+a^2(1+p) \operatorname{AppellF1}\left[2, \frac{3+p}{2}, 1, 3, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]\right) \tan [c+d x]^2\right)^2\right)
 \end{aligned}$$

Problem 620: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c+d x])^p}{(a+b \sin [c+d x])^2} dx$$

Optimal (type 6, 170 leaves, 1 step):

$$\begin{aligned}
 & -\left(\left[e \operatorname{AppellF1}\left[2-p, \frac{1-p}{2}, \frac{1-p}{2}, 3-p, \frac{a+b}{a+b \sin [c+d x]}, \frac{a-b}{a+b \sin [c+d x]}\right] (e \cos [c+d x])^{-1+p}\right.\right. \\
 & \left.\left.\left(-\frac{b(1-\sin [c+d x])}{a+b \sin [c+d x]}\right)^{\frac{1-p}{2}}\left(\frac{b(1+\sin [c+d x])}{a+b \sin [c+d x]}\right)^{\frac{1-p}{2}}\right) / (b d(2-p)(a+b \sin [c+d x]))\right)
 \end{aligned}$$

Result (type 6, 6875 leaves):

$$\begin{aligned}
 & \left(a^2 (e \cos [c + d x])^p \tan [c + d x] (1 + \tan [c + d x]^2)^{-p/2} \right. \\
 & \left(\left(3 (a^2 + b^2) \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan [c + d x]^2, \frac{(-a^2 + b^2) \tan [c + d x]^2}{a^2} \right] \right) / \right. \\
 & \left(\left(-3 a^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + \right. \right. \\
 & \left. \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + a^2 p \right. \right. \\
 & \left. \left. \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] \right) \tan [c + d x]^2 \right) \\
 & \left. \left. (-b^2 \tan [c + d x]^2 + a^2 (1 + \tan [c + d x]^2)) \right) \right) + \frac{1}{(b^2 \tan [c + d x]^2 - a^2 (1 + \tan [c + d x]^2))^2} \\
 & 2 a b \left(- \left(\left(3 a b \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan [c + d x]^2, \frac{(-a^2 + b^2) \tan [c + d x]^2}{a^2} \right] \right) / \right. \right. \\
 & \left(-3 a^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + \right. \\
 & \left(4 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 3, \frac{5}{2}, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + \right. \\
 & \left. a^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 2, \frac{5}{2}, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] \right) \\
 & \left. \tan [c + d x]^2 \right) \right) + \left(2 (-a^2 + b^2) \operatorname{AppellF1} \left[1, \frac{1}{2} (-1 + p), 2, 2, \right. \right. \\
 & \left. \left. -\tan [c + d x]^2, \frac{(-a^2 + b^2) \tan [c + d x]^2}{a^2} \right] \tan [c + d x] \sqrt{1 + \tan [c + d x]^2} \right) / \\
 & \left(-4 a^2 \operatorname{AppellF1} \left[1, \frac{1}{2} (-1 + p), 2, 2, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + \right. \\
 & \left(4 (a^2 - b^2) \operatorname{AppellF1} \left[2, \frac{1}{2} (-1 + p), 3, 3, -\tan [c + d x]^2, \right. \right. \\
 & \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + a^2 (-1 + p) \operatorname{AppellF1} \left[2, \frac{1+p}{2}, 2, 3, \right. \right. \\
 & \left. \left. -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] \right) \tan [c + d x]^2 \right) \right) / \\
 & \left((-a^2 + b^2) d (a + b \sin [c + d x])^2 \left(-\frac{1}{-a^2 + b^2} a^2 p \sec [c + d x]^2 \tan [c + d x]^2 \right. \right. \\
 & \left. \left. (1 + \tan [c + d x]^2)^{-1-\frac{p}{2}} \right. \right. \\
 & \left. \left(\left(3 (a^2 + b^2) \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan [c + d x]^2, \frac{(-a^2 + b^2) \tan [c + d x]^2}{a^2} \right] \right) / \right. \right. \\
 & \left. \left(\left(-3 a^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + \right. \\
 & \quad \left. a^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] \right) \\
 & \quad \left. \tan [c + d x]^2 \right) \left(-b^2 \tan [c + d x]^2 + a^2 (1 + \tan [c + d x]^2) \right) \Bigg) + \\
 & \frac{1}{(b^2 \tan [c + d x]^2 - a^2 (1 + \tan [c + d x]^2))^2} 2 a b \\
 & \left(- \left(\left(3 a b \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan [c + d x]^2, \frac{(-a^2 + b^2) \tan [c + d x]^2}{a^2} \right] \right) / \right. \right. \\
 & \quad \left(-3 a^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + \right. \\
 & \quad \left(4 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 3, \frac{5}{2}, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + \right. \\
 & \quad \left. \left. a^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 2, \frac{5}{2}, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] \right) \right. \\
 & \quad \left. \left. \tan [c + d x]^2 \right) \right) + \left(2 (-a^2 + b^2) \operatorname{AppellF1} \left[1, \frac{1}{2} (-1+p), 2, 2, \right. \right. \\
 & \quad \left. \left. -\tan [c + d x]^2, \frac{(-a^2 + b^2) \tan [c + d x]^2}{a^2} \right] \tan [c + d x] \sqrt{1 + \tan [c + d x]^2} \right) / \\
 & \left(-4 a^2 \operatorname{AppellF1} \left[1, \frac{1}{2} (-1+p), 2, 2, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + \right. \\
 & \quad \left(4 (a^2 - b^2) \operatorname{AppellF1} \left[2, \frac{1}{2} (-1+p), 3, 3, -\tan [c + d x]^2, \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + a^2 (-1+p) \operatorname{AppellF1} \left[2, \frac{1+p}{2}, 2, 3, \right. \right. \\
 & \quad \left. \left. -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] \right) \tan [c + d x]^2 \Bigg) \Bigg) + \\
 & \frac{1}{-a^2 + b^2} a^2 \sec [c + d x]^2 (1 + \tan [c + d x]^2)^{-p/2} \left(\left(3 (a^2 + b^2) \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, \right. \right. \right. \\
 & \quad \left. \left. 1, \frac{3}{2}, -\tan [c + d x]^2, \frac{(-a^2 + b^2) \tan [c + d x]^2}{a^2} \right] \right) / \\
 & \left(\left(-3 a^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + \right. \right. \\
 & \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + \right. \\
 & \quad \left. \left. a^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] \right) \right. \\
 & \quad \left. \left. \tan [c + d x]^2 \right) \left(-b^2 \tan [c + d x]^2 + a^2 (1 + \tan [c + d x]^2) \right) \right) \Bigg) +
 \end{aligned}$$

$$\begin{aligned}
 & \frac{1}{(b^2 \tan [c+d x]^2 - a^2 (1 + \tan [c+d x]^2))^2} 2 a b \\
 & \left(- \left(\left(3 a b \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan [c+d x]^2, \frac{(-a^2 + b^2) \tan [c+d x]^2}{a^2} \right] \right) / \right. \right. \\
 & \quad \left(-3 a^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + \right. \\
 & \quad \left(4 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 3, \frac{5}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + \right. \\
 & \quad \left. \left. a^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 2, \frac{5}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] \right) \right. \\
 & \quad \left. \left. \tan [c+d x]^2 \right) \right) + \left(2 (-a^2 + b^2) \operatorname{AppellF1} \left[1, \frac{1}{2} (-1+p), 2, 2, \right. \right. \\
 & \quad \left. \left. -\tan [c+d x]^2, \frac{(-a^2 + b^2) \tan [c+d x]^2}{a^2} \right] \tan [c+d x] \sqrt{1 + \tan [c+d x]^2} \right) / \\
 & \left(-4 a^2 \operatorname{AppellF1} \left[1, \frac{1}{2} (-1+p), 2, 2, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + \right. \\
 & \quad \left(4 (a^2 - b^2) \operatorname{AppellF1} \left[2, \frac{1}{2} (-1+p), 3, 3, -\tan [c+d x]^2, \right. \right. \\
 & \quad \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + a^2 (-1+p) \operatorname{AppellF1} \left[2, \frac{1+p}{2}, 2, 3, \right. \right. \\
 & \quad \left. \left. -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] \right) \tan [c+d x]^2 \left. \right) \left. \right) + \\
 & \frac{1}{-a^2 + b^2} a^2 \tan [c+d x] (1 + \tan [c+d x]^2)^{-p/2} \left(- \left(\left(3 (a^2 + b^2) \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, \right. \right. \right. \right. \\
 & \quad \left. \left. \left. 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{(-a^2 + b^2) \tan [c+d x]^2}{a^2} \right] \right) / \right. \\
 & \quad \left. \left(2 a^2 \operatorname{Sec} [c+d x]^2 \tan [c+d x] - 2 b^2 \operatorname{Sec} [c+d x]^2 \tan [c+d x] \right) \right) / \\
 & \left(\left(-3 a^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + \right. \right. \\
 & \quad \left(2 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] + \right. \\
 & \quad \left. \left. a^2 p \operatorname{AppellF1} \left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan [c+d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c+d x]^2 \right] \right) \right. \\
 & \quad \left. \left. \tan [c+d x]^2 \right) \left(-b^2 \tan [c+d x]^2 + a^2 (1 + \tan [c+d x]^2)^2 \right) \right) \left. \right) + \\
 & \left(3 (a^2 + b^2) \left(-\frac{1}{3} p \operatorname{AppellF1} \left[\frac{3}{2}, 1 + \frac{p}{2}, 1, \frac{5}{2}, -\tan [c+d x]^2, \frac{(-a^2 + b^2) \tan [c+d x]^2}{a^2} \right] \right. \right. \\
 & \quad \left. \left. \operatorname{Sec} [c+d x]^2 \tan [c+d x] + \frac{1}{3 a^2} 2 (-a^2 + b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
& -\tan [c+d x]^2, \frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2}] \operatorname{Sec}[c+d x]^2 \tan [c+d x] \Big) \Big) / \\
& \left(\left(-3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] + \right. \right. \\
& \left. \left(2\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] + \right. \right. \\
& \left. \left. a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \right) \right. \\
& \left. \left. \tan [c+d x]^2\right)\left(-b^2 \tan [c+d x]^2+a^2\left(1+\tan [c+d x]^2\right)\right)\right) - \\
& \frac{1}{\left(b^2 \tan [c+d x]^2-a^2\left(1+\tan [c+d x]^2\right)\right)^3} 4 a b\left(-2 a^2 \operatorname{Sec}[c+d x]^2 \tan [c+d x] + \right. \\
& \left. 2 b^2 \operatorname{Sec}[c+d x]^2 \tan [c+d x]\right) \\
& \left(-\left(\left(3 a b \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan [c+d x]^2, \frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2}\right] \right) \Big) / \right. \\
& \left(-3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] + \right. \\
& \left(4\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 3, \frac{5}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] + \right. \\
& \left. a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 2, \frac{5}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \right) \\
& \left. \tan [c+d x]^2\right) + \left(2\left(-a^2+b^2\right) \operatorname{AppellF1}\left[1, \frac{1}{2}(-1+p), 2, 2, \right. \right. \\
& \left. \left. -\tan [c+d x]^2, \frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2}\right] \tan [c+d x] \sqrt{1+\tan [c+d x]^2}\right) \Big) / \\
& \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1}{2}(-1+p), 2, 2, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] + \right. \\
& \left(4\left(a^2-b^2\right) \operatorname{AppellF1}\left[2, \frac{1}{2}(-1+p), 3, 3, -\tan [c+d x]^2, \right. \right. \\
& \left. \left. \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] + a^2(-1+p) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, \right. \right. \\
& \left. \left. 3, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \right) \tan [c+d x]^2 \Big) - \\
& \left(3\left(a^2+b^2\right) \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2}, -\tan [c+d x]^2, \frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2}\right] \right. \\
& \left(2\left(2\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] + \right. \right. \\
& \left. \left. a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2}, -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \right) \right. \\
& \left. \left. \operatorname{Sec}[c+d x]^2 \tan [c+d x] - 3 a^2\left(-\frac{1}{3} p \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{p}{2}, 1, \frac{5}{2}, \right. \right. \right. \right.
\end{aligned}$$

$$\begin{aligned}
 & -\tan [c+d x]^2, \left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2 \sec [c+d x]^2 \tan [c+d x]+ \\
 & \frac{2}{3}\left(-1+\frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2},-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \\
 & \sec [c+d x]^2 \tan [c+d x]+ \tan [c+d x]^2\left(2\left(a^2-b^2\right)\left(-\frac{3}{5} p \operatorname{AppellF1}\left[\frac{5}{2},\right.\right.\right. \\
 & \left.\left.\left.1+\frac{p}{2}, 2, \frac{7}{2},-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \sec [c+d x]^2\right.\right. \\
 & \tan [c+d x]+\frac{12}{5}\left(-1+\frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{p}{2}, 3, \frac{7}{2},-\tan [c+d x]^2,\right. \\
 & \left.\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \sec [c+d x]^2 \tan [c+d x]+a^2 p\left(\frac{6}{5}\left(-1+\frac{b^2}{a^2}\right)\right. \\
 & \left.\operatorname{AppellF1}\left[\frac{5}{2}, \frac{2+p}{2}, 2, \frac{7}{2},-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \right. \\
 & \left.\sec [c+d x]^2 \tan [c+d x]-\frac{3}{5}(2+p) \operatorname{AppellF1}\left[\frac{5}{2}, 1+\frac{2+p}{2}, 1, \frac{7}{2},\right.\right. \\
 & \left.\left.-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right] \sec [c+d x]^2 \tan [c+d x]\right)\right)\right)\right) / \\
 & \left(\left(-3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 1, \frac{3}{2},-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+ \right.\right. \\
 & \left.\left(2\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 2, \frac{5}{2},-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+ \right.\right. \\
 & \left.\left.a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 1, \frac{5}{2},-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]\right)\right. \\
 & \left.\tan [c+d x]^2\right)^2\left(-b^2 \tan [c+d x]^2+a^2\left(1+\tan [c+d x]^2\right)\right)\right)+ \\
 & \frac{1}{\left(b^2 \tan [c+d x]^2-a^2\left(1+\tan [c+d x]^2\right)\right)^2} 2 a b \\
 & \left(-\left(\left(3 a b\left(-\frac{1}{3} p \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{p}{2}, 2, \frac{5}{2},-\tan [c+d x]^2,\frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2}\right] \right.\right.\right.\right. \\
 & \left.\left.\left.\sec [c+d x]^2 \tan [c+d x]+\frac{1}{3 a^2} 4\left(-a^2+b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 3, \frac{5}{2},\right.\right.\right.\right. \\
 & \left.\left.\left.-\tan [c+d x]^2,\frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2}\right] \sec [c+d x]^2 \tan [c+d x]\right)\right)\right) / \\
 & \left(-3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2},-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+ \right. \\
 & \left(4\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 3, \frac{5}{2},-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+ \right. \\
 & \left.\left.a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 2, \frac{5}{2},-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]\right)\right. \\
 & \left.\tan [c+d x]^2\right)\right)+\left(2\left(-a^2+b^2\right) \operatorname{AppellF1}\left[1, \frac{1}{2}(-1+p), 2, 2,\right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & -\tan [c+d x]^2, \frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2}] \operatorname{Sec}[c+d x]^2 \tan [c+d x]^2 \Big/ \\
 & \left(\sqrt{1+\tan [c+d x]^2}\left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1}{2}(-1+p), 2, 2, -\tan [c+d x]^2,\right.\right.\right. \\
 & \quad \left.\left.\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+4\left(a^2-b^2\right) \operatorname{AppellF1}\left[2, \frac{1}{2}(-1+p), 3, 3,\right.\right. \\
 & \quad \left.\left.-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+a^2(-1+p) \operatorname{AppellF1}\left[2,\right.\right. \\
 & \quad \left.\left.\frac{1+p}{2}, 2, 3,-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]\right) \tan [c+d x]^2 \Big) + \\
 & \left(2\left(-a^2+b^2\right) \operatorname{AppellF1}\left[1, \frac{1}{2}(-1+p), 2, 2,-\tan [c+d x]^2,\right.\right. \\
 & \quad \left.\left.\frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2}\right] \operatorname{Sec}[c+d x]^2 \sqrt{1+\tan [c+d x]^2}\right) \Big/ \\
 & \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1}{2}(-1+p), 2, 2,-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+ \right. \\
 & \quad \left.4\left(a^2-b^2\right) \operatorname{AppellF1}\left[2, \frac{1}{2}(-1+p), 3, 3,-\tan [c+d x]^2,\right.\right. \\
 & \quad \left.\left.\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+a^2(-1+p) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2,\right.\right. \\
 & \quad \left.\left.3,-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]\right) \tan [c+d x]^2 \Big) + \\
 & \left(2\left(-a^2+b^2\right) \tan [c+d x]\left(-\frac{1}{2}(-1+p) \operatorname{AppellF1}\left[2, 1+\frac{1}{2}(-1+p), 2,\right.\right.\right. \\
 & \quad \left.\left.3,-\tan [c+d x]^2,\frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2}\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x]+ \right. \\
 & \quad \left.\frac{1}{a^2} 2\left(-a^2+b^2\right) \operatorname{AppellF1}\left[2, \frac{1}{2}(-1+p), 3, 3,-\tan [c+d x]^2,\right.\right. \\
 & \quad \left.\left.\frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2}\right] \operatorname{Sec}[c+d x]^2 \tan [c+d x]\right) \sqrt{1+\tan [c+d x]^2} \Big) \Big/ \\
 & \left(-4 a^2 \operatorname{AppellF1}\left[1, \frac{1}{2}(-1+p), 2, 2,-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+ \right. \\
 & \quad \left.4\left(a^2-b^2\right) \operatorname{AppellF1}\left[2, \frac{1}{2}(-1+p), 3, 3,-\tan [c+d x]^2,\right.\right. \\
 & \quad \left.\left.\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+a^2(-1+p) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2,\right.\right. \\
 & \quad \left.\left.3,-\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]\right) \tan [c+d x]^2 \Big) + \\
 & \left(3 a b \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan [c+d x]^2,\frac{\left(-a^2+b^2\right) \tan [c+d x]^2}{a^2}\right]\right. \\
 & \quad \left.2\left(4\left(a^2-b^2\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 3, \frac{5}{2}, -\tan [c+d x]^2,\left(-1+\frac{b^2}{a^2}\right) \tan [c+d x]^2\right]+ \right.\right.
 \end{aligned}$$

$$\begin{aligned}
 & a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 2, \frac{5}{2}, -\tan[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \\
 & \operatorname{Sec}[c+dx]^2 \tan[c+dx] - 3 a^2 \left(-\frac{1}{3} p \operatorname{AppellF1}\left[\frac{3}{2}, 1+\frac{p}{2}, 2, \frac{5}{2}, \right. \right. \\
 & \quad \left. \left. -\tan[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] + \right. \\
 & \quad \frac{4}{3} \left(-1+\frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 3, \frac{5}{2}, -\tan[c+dx]^2, \right. \\
 & \quad \left. \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] \left. \right) + \tan[c+dx]^2 \\
 & \left(4(a^2-b^2) \left(-\frac{3}{5} p \operatorname{AppellF1}\left[\frac{5}{2}, 1+\frac{p}{2}, 3, \frac{7}{2}, -\tan[c+dx]^2, \right. \right. \right. \\
 & \quad \left. \left. \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] + \frac{18}{5} \left(-1+\frac{b^2}{a^2}\right) \right. \\
 & \quad \left. \operatorname{AppellF1}\left[\frac{5}{2}, \frac{p}{2}, 4, \frac{7}{2}, -\tan[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \right. \\
 & \quad \left. \operatorname{Sec}[c+dx]^2 \tan[c+dx] \right) + a^2 p \left(\frac{12}{5} \left(-1+\frac{b^2}{a^2}\right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{2+p}{2}, \right. \right. \\
 & \quad \left. \left. 3, \frac{7}{2}, -\tan[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \operatorname{Sec}[c+dx]^2 \right. \\
 & \quad \left. \tan[c+dx] - \frac{3}{5} (2+p) \operatorname{AppellF1}\left[\frac{5}{2}, 1+\frac{2+p}{2}, 2, \frac{7}{2}, -\tan[c+dx]^2, \right. \right. \\
 & \quad \left. \left. \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \operatorname{Sec}[c+dx]^2 \tan[c+dx] \right) \left. \right) \left. \right) \left. \right) / \\
 & \left(-3 a^2 \operatorname{AppellF1}\left[\frac{1}{2}, \frac{p}{2}, 2, \frac{3}{2}, -\tan[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] + \right. \\
 & \quad \left(4(a^2-b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{p}{2}, 3, \frac{5}{2}, -\tan[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] + \right. \\
 & \quad \left. a^2 p \operatorname{AppellF1}\left[\frac{3}{2}, \frac{2+p}{2}, 2, \frac{5}{2}, -\tan[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \right) \\
 & \quad \left. \tan[c+dx]^2\right)^2 - \left(2(-a^2+b^2) \operatorname{AppellF1}\left[1, \frac{1}{2}(-1+p), 2, 2, \right. \right. \\
 & \quad \left. \left. -\tan[c+dx]^2, \frac{(-a^2+b^2) \tan[c+dx]^2}{a^2}\right] \tan[c+dx] \sqrt{1+\tan[c+dx]^2} \right. \\
 & \quad \left. \left(2 \left(4(a^2-b^2) \operatorname{AppellF1}\left[2, \frac{1}{2}(-1+p), 3, 3, -\tan[c+dx]^2, \right. \right. \right. \right. \\
 & \quad \left. \left. \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] + a^2(-1+p) \operatorname{AppellF1}\left[2, \frac{1+p}{2}, 2, 3, \right. \right. \\
 & \quad \left. \left. -\tan[c+dx]^2, \left(-1+\frac{b^2}{a^2}\right) \tan[c+dx]^2\right] \right) \operatorname{Sec}[c+dx]^2 \tan[c+dx] - \right. \\
 & \quad \left. 4 a^2 \left(-\frac{1}{2}(-1+p) \operatorname{AppellF1}\left[2, 1+\frac{1}{2}(-1+p), 2, 3, -\tan[c+dx]^2, \right. \right. \right.
 \end{aligned}$$

$$\begin{aligned}
 & \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \operatorname{Sec} [c + d x]^2 \tan [c + d x] + \\
 & 2 \left(-1 + \frac{b^2}{a^2} \right) \operatorname{AppellF1} \left[2, \frac{1}{2} (-1 + p), 3, 3, -\tan [c + d x]^2, \right. \\
 & \left. \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \operatorname{Sec} [c + d x]^2 \tan [c + d x] \right) + \\
 & \tan [c + d x]^2 \left(4 (a^2 - b^2) \left(-\frac{2}{3} (-1 + p) \operatorname{AppellF1} \left[3, 1 + \frac{1}{2} (-1 + p), \right. \right. \right. \\
 & \left. \left. \left. 3, 4, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \operatorname{Sec} [c + d x]^2 \right. \right. \right. \\
 & \left. \tan [c + d x] + 4 \left(-1 + \frac{b^2}{a^2} \right) \operatorname{AppellF1} \left[3, \frac{1}{2} (-1 + p), 4, 4, \right. \right. \\
 & \left. \left. -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \operatorname{Sec} [c + d x]^2 \tan [c + d x] \right) \right) + \\
 & a^2 (-1 + p) \left(\frac{8}{3} \left(-1 + \frac{b^2}{a^2} \right) \operatorname{AppellF1} \left[3, \frac{1 + p}{2}, 3, 4, -\tan [c + d x]^2, \right. \right. \\
 & \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \operatorname{Sec} [c + d x]^2 \tan [c + d x] - \right. \right. \\
 & \left. \left. \frac{2}{3} (1 + p) \operatorname{AppellF1} \left[3, 1 + \frac{1 + p}{2}, 2, 4, -\tan [c + d x]^2, \right. \right. \right. \\
 & \left. \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \operatorname{Sec} [c + d x]^2 \tan [c + d x] \right) \right) \right) \right) \Bigg/ \\
 & \left(-4 a^2 \operatorname{AppellF1} \left[1, \frac{1}{2} (-1 + p), 2, 2, -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + \right. \\
 & \left. \left(4 (a^2 - b^2) \operatorname{AppellF1} \left[2, \frac{1}{2} (-1 + p), 3, 3, -\tan [c + d x]^2, \right. \right. \right. \\
 & \left. \left. \left. \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right] + a^2 (-1 + p) \operatorname{AppellF1} \left[2, \frac{1 + p}{2}, 2, 3, \right. \right. \right. \\
 & \left. \left. \left. -\tan [c + d x]^2, \left(-1 + \frac{b^2}{a^2} \right) \tan [c + d x]^2 \right) \tan [c + d x]^2 \right) \right) \right) \Bigg)
 \end{aligned}$$

Problem 621: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^p}{(a + b \sin [c + d x])^3} dx$$

Optimal (type 6, 170 leaves, 1 step):

$$\begin{aligned}
 & - \left(\left[e \operatorname{AppellF1} \left[3 - p, \frac{1 - p}{2}, \frac{1 - p}{2}, 4 - p, \frac{a + b}{a + b \sin [c + d x]}, \frac{a - b}{a + b \sin [c + d x]} \right] (e \cos [c + d x])^{-1 + p} \right. \right. \\
 & \left. \left. \left(-\frac{b (1 - \sin [c + d x])}{a + b \sin [c + d x]} \right)^{\frac{1 - p}{2}} \left(\frac{b (1 + \sin [c + d x])}{a + b \sin [c + d x]} \right)^{\frac{1 - p}{2}} \right) \Bigg/ (b d (3 - p) (a + b \sin [c + d x])^2) \right)
 \end{aligned}$$

Result (type 6, 20 626 leaves): Display of huge result suppressed!

Problem 622: Unable to integrate problem.

$$\int \frac{(e \cos [c + d x])^p}{(a + b \sin [c + d x])^8} dx$$

Optimal (type 6, 170 leaves, 1 step):

$$- \left(\left[e \operatorname{AppellF1} \left[8 - p, \frac{1 - p}{2}, \frac{1 - p}{2}, 9 - p, \frac{a + b}{a + b \sin [c + d x]}, \frac{a - b}{a + b \sin [c + d x]} \right] (e \cos [c + d x])^{-1 + p} \right. \right. \\ \left. \left. \left(- \frac{b (1 - \sin [c + d x])}{a + b \sin [c + d x]} \right)^{\frac{1 - p}{2}} \left(\frac{b (1 + \sin [c + d x])}{a + b \sin [c + d x]} \right)^{\frac{1 - p}{2}} \right] / (b d (8 - p) (a + b \sin [c + d x])^7) \right)$$

Result (type 8, 25 leaves):

$$\int \frac{(e \cos [c + d x])^p}{(a + b \sin [c + d x])^8} dx$$

Problem 623: Result more than twice size of optimal antiderivative.

$$\int (e \cos [c + d x])^p (a + b \sin [c + d x])^{5/2} dx$$

Optimal (type 6, 156 leaves, 2 steps):

$$\frac{1}{7 b d} 2 e \operatorname{AppellF1} \left[\frac{7}{2}, \frac{1 - p}{2}, \frac{1 - p}{2}, \frac{9}{2}, \frac{a + b \sin [c + d x]}{a - b}, \frac{a + b \sin [c + d x]}{a + b} \right] \\ (e \cos [c + d x])^{-1 + p} (a + b \sin [c + d x])^{7/2} \left(1 - \frac{a + b \sin [c + d x]}{a - b} \right)^{\frac{1 - p}{2}} \left(1 - \frac{a + b \sin [c + d x]}{a + b} \right)^{\frac{1 - p}{2}}$$

Result (type 6, 2612 leaves):

$$\frac{1}{2 d} \cos [c + d x]^{-p} (e \cos [c + d x])^p \\ \left(- \left(\left(10 (a^2 - b^2)^2 (2 a^2 + b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{1 - p}{2}, \frac{1 - p}{2}, \frac{5}{2}, \frac{a + b \sin [c + d x]}{a - \sqrt{b^2}}, \right. \right. \right. \right. \\ \left. \left. \frac{a + b \sin [c + d x]}{a + \sqrt{b^2}} \right] \cos [c + d x]^{1 + p} (a + b \sin [c + d x])^{3/2} \right. \\ \left. \left(-\sqrt{b^2} + b \sin [c + d x] \right) \left(\sqrt{b^2} + b \sin [c + d x] \right) (1 - \sin [c + d x]^2)^{-\frac{1 - p}{2}} \right. \\ \left. \left. \left(- \frac{a^2 - b^2 - 2 a (a + b \sin [c + d x]) + (a + b \sin [c + d x])^2}{b^2} \right)^{\frac{1}{2} (-3 + p)} \right) \right) / \\ \left(3 b^3 (a - \sqrt{b^2}) (a + \sqrt{b^2}) \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{1 - p}{2}, \frac{1 - p}{2}, \frac{5}{2}, \frac{a + b \sin [c + d x]}{a - \sqrt{b^2}}, \right. \right. \right. \right.$$

$$\begin{aligned}
 & \left. \left. \left. \left. \frac{a+b \operatorname{Sin}[c+d x]}{a+\sqrt{b^2}} \right] + (-1+p) \left(\left(-a+\sqrt{b^2} \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{7}{2}, \right. \right. \right. \right. \right. \\
 & \left. \left. \left. \frac{a+b \operatorname{Sin}[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \operatorname{Sin}[c+d x]}{a+\sqrt{b^2}} \right] - \left(a+\sqrt{b^2} \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{3-p}{2}, \frac{p}{2}, \right. \right. \right. \\
 & \left. \left. \left. \frac{1-p}{2}, \frac{7}{2}, \frac{a+b \operatorname{Sin}[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \operatorname{Sin}[c+d x]}{a+\sqrt{b^2}} \right] \right) (a+b \operatorname{Sin}[c+d x]) \right) \right) \right) - \\
 & \frac{1}{15 b^3} 8 a \left(a^2-b^2 \right) \operatorname{Cos}[c+d x]^{1+p} (a+b \operatorname{Sin}[c+d x])^{3/2} \left(-\sqrt{b^2}+b \operatorname{Sin}[c+d x] \right) \\
 & \left(\sqrt{b^2}+b \operatorname{Sin}[c+d x] \right) \left(1-\operatorname{Sin}[c+d x]^2 \right)^{-\frac{1-p}{2}} \\
 & \left(-\frac{a^2-b^2-2 a(a+b \operatorname{Sin}[c+d x])+(a+b \operatorname{Sin}[c+d x])^2}{b^2} \right)^{\frac{1}{2}(-3+p)} \\
 & \left(-\left(\left(25 a \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{5}{2}, \frac{a+b \operatorname{Sin}[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \operatorname{Sin}[c+d x]}{a+\sqrt{b^2}} \right] \right) / \right. \right. \\
 & \left. \left(5 \left(a^2-b^2 \right) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{5}{2}, \frac{a+b \operatorname{Sin}[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \operatorname{Sin}[c+d x]}{a+\sqrt{b^2}} \right] \right) + \right. \\
 & \left. (-1+p) \left(\left(-a+\sqrt{b^2} \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{7}{2}, \frac{a+b \operatorname{Sin}[c+d x]}{a-\sqrt{b^2}}, \right. \right. \right. \\
 & \left. \left. \frac{a+b \operatorname{Sin}[c+d x]}{a+\sqrt{b^2}} \right] - \left(a+\sqrt{b^2} \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{3-p}{2}, \frac{1-p}{2}, \frac{7}{2}, \right. \right. \\
 & \left. \left. \frac{a+b \operatorname{Sin}[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \operatorname{Sin}[c+d x]}{a+\sqrt{b^2}} \right] \right) (a+b \operatorname{Sin}[c+d x]) \right) \right) \right) + \\
 & \left(21 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{7}{2}, \frac{a+b \operatorname{Sin}[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \operatorname{Sin}[c+d x]}{a+\sqrt{b^2}} \right] \right) \\
 & (a+b \operatorname{Sin}[c+d x]) \right) \left. \right) / \\
 & \left(7 \left(a^2-b^2 \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{7}{2}, \frac{a+b \operatorname{Sin}[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \operatorname{Sin}[c+d x]}{a+\sqrt{b^2}} \right] + \right. \\
 & \left. (-1+p) \left(\left(-a+\sqrt{b^2} \right) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{9}{2}, \frac{a+b \operatorname{Sin}[c+d x]}{a-\sqrt{b^2}}, \right. \right. \right. \\
 & \left. \left. \frac{a+b \operatorname{Sin}[c+d x]}{a+\sqrt{b^2}} \right] - \left(a+\sqrt{b^2} \right) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{3-p}{2}, \frac{1-p}{2}, \frac{9}{2}, \right. \right. \\
 & \left. \left. \frac{a+b \operatorname{Sin}[c+d x]}{a-\sqrt{b^2}}, \frac{a+b \operatorname{Sin}[c+d x]}{a+\sqrt{b^2}} \right] \right) (a+b \operatorname{Sin}[c+d x]) \right) \right) \right) + \\
 & \left(1 / \left(105 b \left(-2 a^2+b^2+4 a(a+b \operatorname{Sin}[c+d x]) - 2(a+b \operatorname{Sin}[c+d x])^2 \right) \right) \right) \\
 & 2 \\
 & \left(a^2-b^2 \right) \\
 & \operatorname{Cos}[c+d x]^{1+p} \\
 & \operatorname{Cos}\left[2(c+d x)\right] \\
 & (a+b \operatorname{Sin}[c+d x])^{3/2}
 \end{aligned}$$

$$\begin{aligned}
 & \left(-\sqrt{b^2} + b \sin[c + dx] \right) \\
 & \left(\sqrt{b^2} + b \sin[c + dx] \right) \\
 & (1 - \sin[c + dx])^2)^{-\frac{1-p}{2}} \\
 & \left(-\frac{a^2 - b^2 - 2a(a + b \sin[c + dx]) + (a + b \sin[c + dx])^2}{b^2} \right)^{\frac{1}{2}(-3+p)} \\
 & \left(-\left(\left(175(2a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{5}{2}, \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}}\right] \right) \right) / \right. \\
 & \quad \left(5(a^2 - b^2) \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{5}{2}, \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}}\right] + \right. \\
 & \quad \left. (-1+p) \left(\left(-a + \sqrt{b^2} \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{7}{2}, \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \right. \right. \\
 & \quad \left. \left. \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}} \right] - \left(a + \sqrt{b^2} \right) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{3-p}{2}, \frac{1-p}{2}, \frac{7}{2}, \right. \right. \\
 & \quad \left. \left. \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}} \right] \right) (a + b \sin[c + dx]) \right) \left. \right) + \\
 & \left(588a \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{7}{2}, \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}}\right] \right) \\
 & \quad \left. (a + b \sin[c + dx]) \right) / \\
 & \left(7(a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{7}{2}, \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}}\right] + \right. \\
 & \quad \left. (-1+p) \left(\left(-a + \sqrt{b^2} \right) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{9}{2}, \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \right. \right. \right. \\
 & \quad \left. \left. \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}} \right] - \left(a + \sqrt{b^2} \right) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{3-p}{2}, \frac{1-p}{2}, \frac{9}{2}, \right. \right. \\
 & \quad \left. \left. \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}} \right] \right) (a + b \sin[c + dx]) \right) - \\
 & \left(270 \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{9}{2}, \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}}\right] \right) \\
 & \quad \left. (a + b \sin[c + dx])^2 \right) / \\
 & \left(9(a^2 - b^2) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{9}{2}, \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}}\right] + \right. \\
 & \quad \left. (-1+p) \left(\left(-a + \sqrt{b^2} \right) \operatorname{AppellF1}\left[\frac{9}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{11}{2}, \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \right. \right. \right. \\
 & \quad \left. \left. \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}} \right] - \left(a + \sqrt{b^2} \right) \operatorname{AppellF1}\left[\frac{9}{2}, \frac{3-p}{2}, \frac{1-p}{2}, \frac{11}{2}, \right. \right. \\
 & \quad \left. \left. \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}} \right] \right) \right.
 \end{aligned}$$

$$\left(\left(\frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}} \right) (a + b \sin[c + dx]) \right) \Bigg)$$

Problem 624: Result more than twice size of optimal antiderivative.

$$\int (e \cos[c + dx])^p (a + b \sin[c + dx])^{3/2} dx$$

Optimal (type 6, 156 leaves, 2 steps):

$$\frac{1}{5 b d} 2 e \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{7}{2}, \frac{a + b \sin[c + dx]}{a - b}, \frac{a + b \sin[c + dx]}{a + b}\right] (e \cos[c + dx])^{-1+p} (a + b \sin[c + dx])^{5/2} \left(1 - \frac{a + b \sin[c + dx]}{a - b}\right)^{\frac{1-p}{2}} \left(1 - \frac{a + b \sin[c + dx]}{a + b}\right)^{\frac{1-p}{2}}$$

Result (type 6, 447 leaves):

$$\begin{aligned} & - \left(\left(14 (a^2 - b^2)^2 \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{7}{2}, \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}}\right] (e \cos[c + dx])^p \operatorname{Sec}[c + dx]^3 (a + b \sin[c + dx])^{5/2} \left(-\sqrt{b^2} + b \sin[c + dx]\right) \right. \right. \\ & \left. \left(\sqrt{b^2} + b \sin[c + dx] \right) \right) / \left(5 b^3 (a - \sqrt{b^2}) (a + \sqrt{b^2}) d \right. \\ & \left. \left(7 (a^2 - b^2) \operatorname{AppellF1}\left[\frac{5}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{7}{2}, \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}}\right] + (-1 + p) \right. \right. \\ & \left. \left((-a + \sqrt{b^2}) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{9}{2}, \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}}\right] - \right. \right. \\ & \left. \left. (a + \sqrt{b^2}) \operatorname{AppellF1}\left[\frac{7}{2}, \frac{3-p}{2}, \frac{1-p}{2}, \frac{9}{2}, \frac{a + b \sin[c + dx]}{a - \sqrt{b^2}}, \frac{a + b \sin[c + dx]}{a + \sqrt{b^2}}\right] \right) (a + \right. \\ & \left. \left. b \sin[c + dx] \right) \right) \Bigg) \Bigg) \Bigg) \end{aligned}$$

Problem 625: Result more than twice size of optimal antiderivative.

$$\int (e \cos[c + dx])^p \sqrt{a + b \sin[c + dx]} dx$$

Optimal (type 6, 156 leaves, 2 steps):

$$\frac{1}{3 b d} 2 e \operatorname{AppellF1}\left[\frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{5}{2}, \frac{a + b \sin[c + dx]}{a - b}, \frac{a + b \sin[c + dx]}{a + b}\right] (e \cos[c + dx])^{-1+p} (a + b \sin[c + dx])^{3/2} \left(1 - \frac{a + b \sin[c + dx]}{a - b}\right)^{\frac{1-p}{2}} \left(1 - \frac{a + b \sin[c + dx]}{a + b}\right)^{\frac{1-p}{2}}$$

Result (type 6, 447 leaves):

$$\begin{aligned}
 & - \left(\left(10 (a^2 - b^2)^2 \operatorname{AppellF1} \left[\frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{5}{2}, \frac{a+b \sin[c+dx]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+dx]}{a+\sqrt{b^2}} \right] \right. \right. \\
 & \quad \left. \left. (e \cos[c+dx])^p \operatorname{Sec}[c+dx]^3 (a+b \sin[c+dx])^{3/2} \left(-\sqrt{b^2} + b \sin[c+dx] \right) \right. \right. \\
 & \quad \left. \left. \left(\sqrt{b^2} + b \sin[c+dx] \right) \right) \right) / \left(3 b^3 (a-\sqrt{b^2}) (a+\sqrt{b^2}) d \right. \\
 & \quad \left. \left(5 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{5}{2}, \frac{a+b \sin[c+dx]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+dx]}{a+\sqrt{b^2}} \right] + (-1+p) \right. \right. \\
 & \quad \left. \left((-a+\sqrt{b^2}) \operatorname{AppellF1} \left[\frac{5}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{7}{2}, \frac{a+b \sin[c+dx]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+dx]}{a+\sqrt{b^2}} \right] - \right. \right. \\
 & \quad \left. \left. (a+\sqrt{b^2}) \operatorname{AppellF1} \left[\frac{5}{2}, \frac{3-p}{2}, \frac{1-p}{2}, \frac{7}{2}, \frac{a+b \sin[c+dx]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+dx]}{a+\sqrt{b^2}} \right] \right) \right) (a+ \\
 & \quad \left. \left. \left. \left. b \sin[c+dx] \right) \right) \right) \right)
 \end{aligned}$$

Problem 626: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos[c+dx])^p}{\sqrt{a+b \sin[c+dx]}} dx$$

Optimal (type 6, 154 leaves, 2 steps):

$$\begin{aligned}
 & \frac{1}{b d} 2 e \operatorname{AppellF1} \left[\frac{1}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{3}{2}, \frac{a+b \sin[c+dx]}{a-b}, \frac{a+b \sin[c+dx]}{a+b} \right] \\
 & (e \cos[c+dx])^{-1+p} \sqrt{a+b \sin[c+dx]} \left(1 - \frac{a+b \sin[c+dx]}{a-b} \right)^{\frac{1-p}{2}} \left(1 - \frac{a+b \sin[c+dx]}{a+b} \right)^{\frac{1-p}{2}}
 \end{aligned}$$

Result (type 6, 445 leaves):

$$\begin{aligned}
 & - \left(\left(6 (a^2 - b^2)^2 \operatorname{AppellF1} \left[\frac{1}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{3}{2}, \frac{a+b \sin[c+dx]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+dx]}{a+\sqrt{b^2}} \right] \right. \right. \\
 & \quad \left. \left. (e \cos[c+dx])^p \operatorname{Sec}[c+dx]^3 \sqrt{a+b \sin[c+dx]} \left(-\sqrt{b^2} + b \sin[c+dx] \right) \right. \right. \\
 & \quad \left. \left. \left(\sqrt{b^2} + b \sin[c+dx] \right) \right) \right) / \left(b^3 (a-\sqrt{b^2}) (a+\sqrt{b^2}) d \right. \\
 & \quad \left. \left(3 (a^2 - b^2) \operatorname{AppellF1} \left[\frac{1}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{3}{2}, \frac{a+b \sin[c+dx]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+dx]}{a+\sqrt{b^2}} \right] + (-1+p) \right. \right. \\
 & \quad \left. \left((-a+\sqrt{b^2}) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{5}{2}, \frac{a+b \sin[c+dx]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+dx]}{a+\sqrt{b^2}} \right] - \right. \right. \\
 & \quad \left. \left. (a+\sqrt{b^2}) \operatorname{AppellF1} \left[\frac{3}{2}, \frac{3-p}{2}, \frac{1-p}{2}, \frac{5}{2}, \frac{a+b \sin[c+dx]}{a-\sqrt{b^2}}, \frac{a+b \sin[c+dx]}{a+\sqrt{b^2}} \right] \right) \right) (a+ \\
 & \quad \left. \left. \left. \left. b \sin[c+dx] \right) \right) \right) \right)
 \end{aligned}$$

Problem 627: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^p}{(a + b \sin [c + d x])^{3/2}} dx$$

Optimal (type 6, 154 leaves, 2 steps):

$$-\left(\left(2 e \operatorname{AppellF1} \left[-\frac{1}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{1}{2}, \frac{a+b \sin [c+d x]}{a-b}, \frac{a+b \sin [c+d x]}{a+b} \right] (e \cos [c+d x])^{-1+p} \right. \right. \\ \left. \left. \left(1 - \frac{a+b \sin [c+d x]}{a-b} \right)^{\frac{1-p}{2}} \left(1 - \frac{a+b \sin [c+d x]}{a+b} \right)^{\frac{1-p}{2}} \right) / \left(b d \sqrt{a+b \sin [c+d x]} \right) \right)$$

Result (type 6, 444 leaves):

$$\left(2 (a^2 - b^2)^2 \operatorname{AppellF1} \left[-\frac{1}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{1}{2}, \frac{a+b \sin [c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin [c+d x]}{a+\sqrt{b^2}} \right] \right. \\ \left. (e \cos [c+d x])^p \operatorname{Sec} [c+d x]^3 \left(\sqrt{b^2} - b \sin [c+d x] \right) \left(\sqrt{b^2} + b \sin [c+d x] \right) \right) / \\ \left(b^3 (a - \sqrt{b^2}) (a + \sqrt{b^2}) d \sqrt{a+b \sin [c+d x]} \right) \\ \left((-a^2 + b^2) \operatorname{AppellF1} \left[-\frac{1}{2}, \frac{1-p}{2}, \frac{1-p}{2}, \frac{1}{2}, \frac{a+b \sin [c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin [c+d x]}{a+\sqrt{b^2}} \right] - \right. \\ \left. (-1+p) \left((-a + \sqrt{b^2}) \operatorname{AppellF1} \left[\frac{1}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{3}{2}, \frac{a+b \sin [c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin [c+d x]}{a+\sqrt{b^2}} \right] - \right. \right. \\ \left. \left. (a + \sqrt{b^2}) \operatorname{AppellF1} \left[\frac{1}{2}, \frac{3-p}{2}, \frac{1-p}{2}, \frac{3}{2}, \frac{a+b \sin [c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin [c+d x]}{a+\sqrt{b^2}} \right] \right) (a + \right. \\ \left. b \sin [c+d x]) \right) \left. \right)$$

Problem 628: Result more than twice size of optimal antiderivative.

$$\int \frac{(e \cos [c + d x])^p}{(a + b \sin [c + d x])^{5/2}} dx$$

Optimal (type 6, 156 leaves, 2 steps):

$$-\left(\left(2 e \operatorname{AppellF1} \left[-\frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, -\frac{1}{2}, \frac{a+b \sin [c+d x]}{a-b}, \frac{a+b \sin [c+d x]}{a+b} \right] (e \cos [c+d x])^{-1+p} \right. \right. \\ \left. \left. \left(1 - \frac{a+b \sin [c+d x]}{a-b} \right)^{\frac{1-p}{2}} \left(1 - \frac{a+b \sin [c+d x]}{a+b} \right)^{\frac{1-p}{2}} \right) / \left(3 b d (a + b \sin [c+d x])^{3/2} \right) \right)$$

Result (type 6, 446 leaves):

$$\begin{aligned}
 & - \left(\left(2 (a^2 - b^2)^2 \operatorname{AppellF1} \left[-\frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, -\frac{1}{2}, \frac{a+b \sin [c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin [c+d x]}{a+\sqrt{b^2}} \right] \right. \right. \\
 & \quad \left. \left. (e \cos [c+d x])^p \sec [c+d x]^3 \left(\sqrt{b^2} - b \sin [c+d x] \right) \left(\sqrt{b^2} + b \sin [c+d x] \right) \right) \right) / \\
 & \left(3 b^3 (a - \sqrt{b^2}) (a + \sqrt{b^2}) d (a + b \sin [c+d x])^{3/2} \right. \\
 & \quad \left((a^2 - b^2) \operatorname{AppellF1} \left[-\frac{3}{2}, \frac{1-p}{2}, \frac{1-p}{2}, -\frac{1}{2}, \frac{a+b \sin [c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin [c+d x]}{a+\sqrt{b^2}} \right] - (-1+p) \right. \\
 & \quad \left((-a + \sqrt{b^2}) \operatorname{AppellF1} \left[-\frac{1}{2}, \frac{1-p}{2}, \frac{3-p}{2}, \frac{1}{2}, \frac{a+b \sin [c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin [c+d x]}{a+\sqrt{b^2}} \right] - \right. \\
 & \quad \left. \left. (a + \sqrt{b^2}) \operatorname{AppellF1} \left[-\frac{1}{2}, \frac{3-p}{2}, \frac{1-p}{2}, \frac{1}{2}, \frac{a+b \sin [c+d x]}{a-\sqrt{b^2}}, \frac{a+b \sin [c+d x]}{a+\sqrt{b^2}} \right] \right) (a + \right. \\
 & \quad \left. \left. b \sin [c+d x] \right) \right) \left. \right) \left. \right)
 \end{aligned}$$

Problem 629: Unable to integrate problem.

$$\int (e \cos [c+d x])^p (a+b \sin [c+d x])^m dx$$

Optimal (type 6, 158 leaves, 2 steps):

$$\begin{aligned}
 & \frac{1}{b d (1+m)} e \operatorname{AppellF1} \left[1+m, \frac{1-p}{2}, \frac{1-p}{2}, 2+m, \frac{a+b \sin [c+d x]}{a-b}, \frac{a+b \sin [c+d x]}{a+b} \right] \\
 & (e \cos [c+d x])^{-1+p} (a+b \sin [c+d x])^{1+m} \left(1 - \frac{a+b \sin [c+d x]}{a-b} \right)^{\frac{1-p}{2}} \left(1 - \frac{a+b \sin [c+d x]}{a+b} \right)^{\frac{1-p}{2}}
 \end{aligned}$$

Result (type 8, 25 leaves):

$$\int (e \cos [c+d x])^p (a+b \sin [c+d x])^m dx$$

Problem 630: Result unnecessarily involves complex numbers and more than twice size of optimal antiderivative.

$$\int \cos [c+d x]^7 (a+b \sin [c+d x])^m dx$$

Optimal (type 3, 254 leaves, 3 steps):

$$\begin{aligned}
 & - \frac{(a^2 - b^2)^3 (a+b \sin [c+d x])^{1+m}}{b^7 d (1+m)} + \frac{6 a (a^2 - b^2)^2 (a+b \sin [c+d x])^{2+m}}{b^7 d (2+m)} - \\
 & \frac{3 (5 a^4 - 6 a^2 b^2 + b^4) (a+b \sin [c+d x])^{3+m}}{b^7 d (3+m)} + \frac{4 a (5 a^2 - 3 b^2) (a+b \sin [c+d x])^{4+m}}{b^7 d (4+m)} - \\
 & \frac{3 (5 a^2 - b^2) (a+b \sin [c+d x])^{5+m}}{b^7 d (5+m)} + \frac{6 a (a+b \sin [c+d x])^{6+m}}{b^7 d (6+m)} - \frac{(a+b \sin [c+d x])^{7+m}}{b^7 d (7+m)}
 \end{aligned}$$

Result (type 3, 1639 leaves):

$$\frac{1}{d} (a + b \sin[c + dx])^m$$

$$\left(- \left((a (11520 a^6 - 48384 a^4 b^2 + 80640 a^2 b^4 - 80640 b^6 - 12096 a^4 b^2 m + 50232 a^2 b^4 m - 112224 b^6 m + 1728 a^4 b^2 m^2 + 3324 a^2 b^4 m^2 - 54542 b^6 m^2 - 840 a^2 b^4 m^3 - 13125 b^6 m^3 - 12 a^2 b^4 m^4 - 1829 b^6 m^4 - 147 b^6 m^5 - 5 b^6 m^6)) / (16 b^7 (1+m) (2+m) (3+m) (4+m) (5+m) (6+m) (7+m)) \right) + \right.$$

$$\left((176400 b^6 + 46080 a^6 m - 182016 a^4 b^2 m + 279936 a^2 b^4 m + 194868 b^6 m - 42624 a^4 b^2 m^2 + 169440 a^2 b^4 m^2 + 78968 b^6 m^2 + 1152 a^4 b^2 m^3 + 29328 a^2 b^4 m^3 + 16299 b^6 m^3 + 1632 a^2 b^4 m^4 + 2027 b^6 m^4 + 48 a^2 b^4 m^5 + 153 b^6 m^5 + 5 b^6 m^6) \left(- \frac{i \cos[c + dx]}{128 b^6} + \frac{\sin[c + dx]}{128 b^6} \right) \right) / \left((1+m) (2+m) (3+m) (4+m) (5+m) (6+m) (7+m) \right) + \right.$$

$$\left((176400 b^6 + 46080 a^6 m - 182016 a^4 b^2 m + 279936 a^2 b^4 m + 194868 b^6 m - 42624 a^4 b^2 m^2 + 169440 a^2 b^4 m^2 + 78968 b^6 m^2 + 1152 a^4 b^2 m^3 + 29328 a^2 b^4 m^3 + 16299 b^6 m^3 + 1632 a^2 b^4 m^4 + 2027 b^6 m^4 + 48 a^2 b^4 m^5 + 153 b^6 m^5 + 5 b^6 m^6) \left(\frac{i \cos[c + dx]}{128 b^6} + \frac{\sin[c + dx]}{128 b^6} \right) \right) / \left((1+m) (2+m) (3+m) (4+m) (5+m) (6+m) (7+m) \right) + \right.$$

$$\left((1920 a^4 m - 7104 a^2 b^2 m + 10008 b^4 m - 1696 a^2 b^2 m^2 + 6370 b^4 m^2 - 32 a^2 b^2 m^3 + 1411 b^4 m^3 + 134 b^4 m^4 + 5 b^4 m^5) \left(\frac{3 a \cos[2(c + dx)]}{64 b^5} - \frac{3 i a \sin[2(c + dx)]}{64 b^5} \right) \right) / \left((2+m) (3+m) (4+m) (5+m) (6+m) (7+m) \right) + \right.$$

$$\left((1920 a^4 m - 7104 a^2 b^2 m + 10008 b^4 m - 1696 a^2 b^2 m^2 + 6370 b^4 m^2 - 32 a^2 b^2 m^3 + 1411 b^4 m^3 + 134 b^4 m^4 + 5 b^4 m^5) \left(\frac{3 a \cos[2(c + dx)]}{64 b^5} + \frac{3 i a \sin[2(c + dx)]}{64 b^5} \right) \right) / \left((2+m) (3+m) (4+m) (5+m) (6+m) (7+m) \right) + \right.$$

$$\left((5880 b^4 - 640 a^4 m + 2208 a^2 b^2 m + 3602 b^4 m + 552 a^2 b^2 m^2 + 797 b^4 m^2 + 24 a^2 b^2 m^3 + 78 b^4 m^3 + 3 b^4 m^4) \left(- \frac{3 i \cos[3(c + dx)]}{128 b^4} + \frac{3 \sin[3(c + dx)]}{128 b^4} \right) \right) / \left((3+m) (4+m) (5+m) (6+m) (7+m) \right) + \left((5880 b^4 - 640 a^4 m + 2208 a^2 b^2 m + 3602 b^4 m + 552 a^2 b^2 m^2 + 797 b^4 m^2 + 24 a^2 b^2 m^3 + 78 b^4 m^3 + 3 b^4 m^4) \left(\frac{3 i \cos[3(c + dx)]}{128 b^4} + \frac{3 \sin[3(c + dx)]}{128 b^4} \right) \right) / \left((3+m) (4+m) (5+m) (6+m) (7+m) \right) + \right.$$

$$\left((20 a^2 m - 64 b^2 m - 17 b^2 m^2 - b^2 m^3) \left(- \frac{3 a \cos[4(c + dx)]}{32 b^3} - \frac{3 i a \sin[4(c + dx)]}{32 b^3} \right) \right) / \left((3+m) (4+m) (5+m) (6+m) (7+m) \right) + \right.$$

$$\begin{aligned}
 & ((4+m)(5+m)(6+m)(7+m)) + \\
 & \left((20a^2m - 64b^2m - 17b^2m^2 - b^2m^3) \left(-\frac{3a \operatorname{Cos}[4(c+dx)]}{32b^3} + \frac{3i a \operatorname{Sin}[4(c+dx)]}{32b^3} \right) \right) / \\
 & ((4+m)(5+m)(6+m)(7+m)) + \\
 & \frac{(294b^2 + 24a^2m + 79b^2m + 5b^2m^2) \left(-\frac{i \operatorname{Cos}[5(c+dx)]}{128b^2} + \frac{\operatorname{Sin}[5(c+dx)]}{128b^2} \right)}{(5+m)(6+m)(7+m)} + \\
 & \frac{(294b^2 + 24a^2m + 79b^2m + 5b^2m^2) \left(\frac{i \operatorname{Cos}[5(c+dx)]}{128b^2} + \frac{\operatorname{Sin}[5(c+dx)]}{128b^2} \right)}{(5+m)(6+m)(7+m)} + \\
 & \frac{\frac{a m \operatorname{Cos}[6(c+dx)]}{64b} - \frac{i a m \operatorname{Sin}[6(c+dx)]}{64b}}{(6+m)(7+m)} + \\
 & \frac{\frac{a m \operatorname{Cos}[6(c+dx)]}{64b} + \frac{i a m \operatorname{Sin}[6(c+dx)]}{64b}}{(6+m)(7+m)} + \\
 & \frac{-\frac{1}{128} i \operatorname{Cos}[7(c+dx)] + \frac{1}{128} \operatorname{Sin}[7(c+dx)]}{7+m} + \\
 & \left. \frac{\frac{1}{128} i \operatorname{Cos}[7(c+dx)] + \frac{1}{128} \operatorname{Sin}[7(c+dx)]}{7+m} \right)
 \end{aligned}$$

Problem 634: Unable to integrate problem.

$$\int \operatorname{Sec}[c+dx] (a+b \operatorname{Sin}[c+dx])^m dx$$

Optimal (type 5, 115 leaves, 5 steps):

$$\begin{aligned}
 & - \left(\left(\operatorname{Hypergeometric2F1} \left[1, 1+m, 2+m, \frac{a+b \operatorname{Sin}[c+dx]}{a-b} \right] (a+b \operatorname{Sin}[c+dx])^{1+m} \right) / \right. \\
 & \quad \left. (2(a-b)d(1+m)) \right) + \\
 & \left(\operatorname{Hypergeometric2F1} \left[1, 1+m, 2+m, \frac{a+b \operatorname{Sin}[c+dx]}{a+b} \right] (a+b \operatorname{Sin}[c+dx])^{1+m} \right) / \\
 & \quad (2(a+b)d(1+m))
 \end{aligned}$$

Result (type 8, 21 leaves):

$$\int \operatorname{Sec}[c+dx] (a+b \operatorname{Sin}[c+dx])^m dx$$

Problem 635: Unable to integrate problem.

$$\int \operatorname{Sec}[c+dx]^3 (a+b \operatorname{Sin}[c+dx])^m dx$$

Optimal (type 5, 183 leaves, 6 steps):

$$\begin{aligned}
& - \left(\left((a-b(1-m)) \operatorname{Hypergeometric2F1} \left[1, 1+m, 2+m, \frac{a+b \sin [c+d x]}{a-b} \right] (a+b \sin [c+d x])^{1+m} \right) / \right. \\
& \quad \left. (4(a-b)^2 d(1+m)) \right) + \\
& \left((a+b-b m) \operatorname{Hypergeometric2F1} \left[1, 1+m, 2+m, \frac{a+b \sin [c+d x]}{a+b} \right] (a+b \sin [c+d x])^{1+m} \right) / \\
& \quad (4(a+b)^2 d(1+m)) - \frac{\operatorname{Sec}[c+d x]^2 (b-a \sin [c+d x]) (a+b \sin [c+d x])^{1+m}}{2(a^2-b^2) d}
\end{aligned}$$

Result (type 8, 23 leaves):

$$\int \operatorname{Sec}[c+d x]^3 (a+b \sin [c+d x])^m dx$$

Problem 636: Unable to integrate problem.

$$\int \operatorname{Sec}[c+d x]^5 (a+b \sin [c+d x])^m dx$$

Optimal (type 5, 305 leaves, 7 steps):

$$\begin{aligned}
& - \left(\left((3 a^2 - 3 a b (2-m) + b^2 (3-4 m+m^2)) \operatorname{Hypergeometric2F1} \left[1, 1+m, 2+m, \frac{a+b \sin [c+d x]}{a-b} \right] \right. \right. \\
& \quad \left. \left. (a+b \sin [c+d x])^{1+m} \right) / (16(a-b)^3 d(1+m)) \right) + \\
& \left((3 a^2 + 3 a b (2-m) + b^2 (3-4 m+m^2)) \operatorname{Hypergeometric2F1} \left[1, 1+m, 2+m, \frac{a+b \sin [c+d x]}{a+b} \right] \right. \\
& \quad \left. (a+b \sin [c+d x])^{1+m} \right) / (16(a+b)^3 d(1+m)) - \\
& \frac{\operatorname{Sec}[c+d x]^4 (b-a \sin [c+d x]) (a+b \sin [c+d x])^{1+m}}{4(a^2-b^2) d} + \\
& \frac{1}{8(a^2-b^2)^2 d} \\
& \operatorname{Sec}[c+d x]^2 (a+b \sin [c+d x])^{1+m} \\
& (b(b^2(3-m) - a^2(1+m)) + a(3a^2 - b^2(5-2m)) \sin [c+d x])
\end{aligned}$$

Result (type 8, 23 leaves):

$$\int \operatorname{Sec}[c+d x]^5 (a+b \sin [c+d x])^m dx$$

Problem 637: Unable to integrate problem.

$$\int \operatorname{Cos}[c+d x]^4 (a+b \sin [c+d x])^m dx$$

Optimal (type 6, 129 leaves, 2 steps):

$$\left(\text{AppellF1}\left[1+m, -\frac{3}{2}, -\frac{3}{2}, 2+m, \frac{a+b \sin[c+dx]}{a-b}, \frac{a+b \sin[c+dx]}{a+b}\right] \cos[c+dx]^3 \right. \\ \left. (a+b \sin[c+dx])^{1+m} \right) / \left(b d (1+m) \left(1 - \frac{a+b \sin[c+dx]}{a-b}\right)^{3/2} \left(1 - \frac{a+b \sin[c+dx]}{a+b}\right)^{3/2} \right)$$

Result (type 8, 23 leaves):

$$\int \cos[c+dx]^4 (a+b \sin[c+dx])^m dx$$

Problem 638: Unable to integrate problem.

$$\int \cos[c+dx]^2 (a+b \sin[c+dx])^m dx$$

Optimal (type 6, 127 leaves, 2 steps):

$$\left(\text{AppellF1}\left[1+m, -\frac{1}{2}, -\frac{1}{2}, 2+m, \frac{a+b \sin[c+dx]}{a-b}, \frac{a+b \sin[c+dx]}{a+b}\right] \cos[c+dx] \right. \\ \left. (a+b \sin[c+dx])^{1+m} \right) / \left(b d (1+m) \sqrt{1 - \frac{a+b \sin[c+dx]}{a-b}} \sqrt{1 - \frac{a+b \sin[c+dx]}{a+b}} \right)$$

Result (type 8, 23 leaves):

$$\int \cos[c+dx]^2 (a+b \sin[c+dx])^m dx$$

Problem 639: Unable to integrate problem.

$$\int \sec[c+dx]^2 (a+b \sin[c+dx])^m dx$$

Optimal (type 6, 129 leaves, 2 steps):

$$\frac{1}{b d (1+m)} \text{AppellF1}\left[1+m, \frac{3}{2}, \frac{3}{2}, 2+m, \frac{a+b \sin[c+dx]}{a-b}, \frac{a+b \sin[c+dx]}{a+b}\right] \\ \sec[c+dx]^3 (a+b \sin[c+dx])^{1+m} \left(1 - \frac{a+b \sin[c+dx]}{a-b}\right)^{3/2} \left(1 - \frac{a+b \sin[c+dx]}{a+b}\right)^{3/2}$$

Result (type 8, 23 leaves):

$$\int \sec[c+dx]^2 (a+b \sin[c+dx])^m dx$$

Problem 640: Unable to integrate problem.

$$\int \sec[c+dx]^4 (a+b \sin[c+dx])^m dx$$

Optimal (type 6, 129 leaves, 2 steps):

$$\frac{1}{b d (1+m)} \text{AppellF1}\left[1+m, \frac{5}{2}, \frac{5}{2}, 2+m, \frac{a+b \sin [c+d x]}{a-b}, \frac{a+b \sin [c+d x]}{a+b}\right] \\ \sec [c+d x]^5 (a+b \sin [c+d x])^{1+m} \left(1-\frac{a+b \sin [c+d x]}{a-b}\right)^{5/2} \left(1-\frac{a+b \sin [c+d x]}{a+b}\right)^{5/2}$$

Result (type 8, 23 leaves):

$$\int \sec [c+d x]^4 (a+b \sin [c+d x])^m dx$$

Problem 641: Unable to integrate problem.

$$\int (e \cos [c+d x])^{5/2} (a+b \sin [c+d x])^m dx$$

Optimal (type 6, 134 leaves, 2 steps):

$$\left(e \text{AppellF1}\left[1+m, -\frac{3}{4}, -\frac{3}{4}, 2+m, \frac{a+b \sin [c+d x]}{a-b}, \frac{a+b \sin [c+d x]}{a+b}\right] (e \cos [c+d x])^{3/2} \right. \\ \left. (a+b \sin [c+d x])^{1+m} \right) / \left(b d (1+m) \left(1-\frac{a+b \sin [c+d x]}{a-b}\right)^{3/4} \left(1-\frac{a+b \sin [c+d x]}{a+b}\right)^{3/4} \right)$$

Result (type 8, 27 leaves):

$$\int (e \cos [c+d x])^{5/2} (a+b \sin [c+d x])^m dx$$

Problem 642: Unable to integrate problem.

$$\int (e \cos [c+d x])^{3/2} (a+b \sin [c+d x])^m dx$$

Optimal (type 6, 134 leaves, 2 steps):

$$\left(e \text{AppellF1}\left[1+m, -\frac{1}{4}, -\frac{1}{4}, 2+m, \frac{a+b \sin [c+d x]}{a-b}, \frac{a+b \sin [c+d x]}{a+b}\right] \sqrt{e \cos [c+d x]} \right. \\ \left. (a+b \sin [c+d x])^{1+m} \right) / \left(b d (1+m) \left(1-\frac{a+b \sin [c+d x]}{a-b}\right)^{1/4} \left(1-\frac{a+b \sin [c+d x]}{a+b}\right)^{1/4} \right)$$

Result (type 8, 27 leaves):

$$\int (e \cos [c+d x])^{3/2} (a+b \sin [c+d x])^m dx$$

Problem 643: Unable to integrate problem.

$$\int \sqrt{e \cos [c+d x]} (a+b \sin [c+d x])^m dx$$

Optimal (type 6, 134 leaves, 2 steps):

$$\left(e \operatorname{AppellF1}\left[1+m, \frac{1}{4}, \frac{1}{4}, 2+m, \frac{a+b \sin [c+d x]}{a-b}, \frac{a+b \sin [c+d x]}{a+b}\right] (a+b \sin [c+d x])^{1+m} \left(1-\frac{a+b \sin [c+d x]}{a-b}\right)^{1/4} \left(1-\frac{a+b \sin [c+d x]}{a+b}\right)^{1/4}\right) / (b d (1+m) \sqrt{e \cos [c+d x]})$$

Result (type 8, 27 leaves):

$$\int \sqrt{e \cos [c+d x]} (a+b \sin [c+d x])^m dx$$

Problem 644: Unable to integrate problem.

$$\int \frac{(a+b \sin [c+d x])^m}{\sqrt{e \cos [c+d x]}} dx$$

Optimal (type 6, 134 leaves, 2 steps):

$$\left(e \operatorname{AppellF1}\left[1+m, \frac{3}{4}, \frac{3}{4}, 2+m, \frac{a+b \sin [c+d x]}{a-b}, \frac{a+b \sin [c+d x]}{a+b}\right] (a+b \sin [c+d x])^{1+m} \left(1-\frac{a+b \sin [c+d x]}{a-b}\right)^{3/4} \left(1-\frac{a+b \sin [c+d x]}{a+b}\right)^{3/4}\right) / (b d (1+m) (e \cos [c+d x])^{3/2})$$

Result (type 8, 27 leaves):

$$\int \frac{(a+b \sin [c+d x])^m}{\sqrt{e \cos [c+d x]}} dx$$

Problem 645: Unable to integrate problem.

$$\int \frac{(a+b \sin [c+d x])^m}{(e \cos [c+d x])^{3/2}} dx$$

Optimal (type 6, 134 leaves, 2 steps):

$$\left(e \operatorname{AppellF1}\left[1+m, \frac{5}{4}, \frac{5}{4}, 2+m, \frac{a+b \sin [c+d x]}{a-b}, \frac{a+b \sin [c+d x]}{a+b}\right] (a+b \sin [c+d x])^{1+m} \left(1-\frac{a+b \sin [c+d x]}{a-b}\right)^{5/4} \left(1-\frac{a+b \sin [c+d x]}{a+b}\right)^{5/4}\right) / (b d (1+m) (e \cos [c+d x])^{5/2})$$

Result (type 8, 27 leaves):

$$\int \frac{(a+b \sin [c+d x])^m}{(e \cos [c+d x])^{3/2}} dx$$

Problem 646: Unable to integrate problem.

$$\int \frac{(a+b \sin [c+d x])^m}{(e \cos [c+d x])^{5/2}} dx$$

Optimal (type 6, 134 leaves, 2 steps):

$$\left(e \operatorname{AppellF1}\left[1+m, \frac{7}{4}, \frac{7}{4}, 2+m, \frac{a+b \sin [c+d x]}{a-b}, \frac{a+b \sin [c+d x]}{a+b}\right] (a+b \sin [c+d x])^{1+m} \left(1-\frac{a+b \sin [c+d x]}{a-b}\right)^{7/4} \left(1-\frac{a+b \sin [c+d x]}{a+b}\right)^{7/4}\right) / (b d (1+m) (e \cos [c+d x])^{7/2})$$

Result (type 8, 27 leaves):

$$\int \frac{(a+b \sin [c+d x])^m}{(e \cos [c+d x])^{5/2}} dx$$

Problem 647: Unable to integrate problem.

$$\int (e \cos [c+d x])^{-4-m} (a+b \sin [c+d x])^m dx$$

Optimal (type 5, 598 leaves, 9 steps):

$$\begin{aligned} & -\frac{(e \cos [c+d x])^{-3-m} (a+b \sin [c+d x])^{1+m}}{(a-b) d e (3+m)} + \frac{2 b (e \cos [c+d x])^{-1-m} (a+b \sin [c+d x])^{1+m}}{(a-b)^2 d e^3 (1+m) (3+m)} + \\ & \frac{a (e \cos [c+d x])^{-3-m} (1+\sin [c+d x]) (a+b \sin [c+d x])^{1+m}}{(a^2-b^2) d e (3+m)} + \\ & \frac{(a(3 b+a(2+m)) (e \cos [c+d x])^{-3-m} (1-\sin [c+d x]) (1+\sin [c+d x]) (a+b \sin [c+d x])^{1+m})}{((a-b) (a+b)^2 d e (1+m) (3+m))} / \\ & \left(2^{\frac{3-m}{2}} a b (e \cos [c+d x])^{-1-m} \operatorname{Hypergeometric2F1}\left[\frac{1}{2}(-1-m), \frac{1+m}{2}, \frac{1-m}{2}, \right. \right. \\ & \left. \left. \frac{(a-b)(1-\sin [c+d x])}{2(a+b \sin [c+d x])}\right] \left(\frac{(a+b)(1+\sin [c+d x])}{a+b \sin [c+d x]}\right)^{\frac{1+m}{2}} (a+b \sin [c+d x])^{1+m}\right) / \\ & \left((a-b)^2 (a+b) d e^3 (1+m) (3+m) \right) - \left(2^{-\frac{1-m}{2}} a (2 a b-b^2+a^2(2+m)) (e \cos [c+d x])^{-3-m} \right. \\ & \left. \operatorname{Hypergeometric2F1}\left[\frac{1-m}{2}, \frac{3+m}{2}, \frac{3-m}{2}, \frac{(a-b)(1-\sin [c+d x])}{2(a+b \sin [c+d x])}\right] (1-\sin [c+d x])^2 \right. \\ & \left. \left(\frac{(a+b)(1+\sin [c+d x])}{a+b \sin [c+d x]}\right)^{\frac{3+m}{2}} (a+b \sin [c+d x])^{1+m}\right) / \left((a-b) (a+b)^3 d e (1-m) (3+m) \right) \end{aligned}$$

Result (type 8, 29 leaves):

$$\int (e \cos [c+d x])^{-4-m} (a+b \sin [c+d x])^m dx$$

Problem 648: Unable to integrate problem.

$$\int (e \cos [c+d x])^{-3-m} (a+b \sin [c+d x])^m dx$$

Optimal (type 5, 311 leaves, ? steps):

$$\begin{aligned} & \left((e \cos [c + d x])^{-m} \operatorname{Sec}[c + d x]^4 (-1 + \sin [c + d x]) (1 + \sin [c + d x]) (a + b \sin [c + d x])^{1+m} \right) / \\ & \left((a - b) d e^3 (2 + m) + (-2 b + a (2 + m)) (e \cos [c + d x])^{-m} \operatorname{Sec}[c + d x]^4 \right. \\ & \left. (-1 + \sin [c + d x]) (1 + \sin [c + d x])^2 (a + b \sin [c + d x])^{1+m} \right) / \left((a - b)^2 d e^3 m (2 + m) \right) - \\ & \left((-b^2 + a^2 (1 + m)) (e \cos [c + d x])^{-m} \operatorname{Hypergeometric2F1}\left[\frac{m}{2}, 1 + m, 2 + m, \right. \right. \\ & \left. \left. -\frac{2(a + b \sin [c + d x])}{(a - b)(-1 + \sin [c + d x])} \right] \operatorname{Sec}[c + d x]^4 (1 + \sin [c + d x])^3 \right. \\ & \left. \left(\frac{(a + b)(1 + \sin [c + d x])}{(a - b)(-1 + \sin [c + d x])} \right)^{\frac{1}{2}(-2+m)} (a + b \sin [c + d x])^{1+m} \right) / \left((a - b)^3 d e^3 m (1 + m) \right) \end{aligned}$$

Result (type 8, 29 leaves):

$$\int (e \cos [c + d x])^{-3-m} (a + b \sin [c + d x])^m dx$$

Problem 649: Unable to integrate problem.

$$\int (e \cos [c + d x])^{-2-m} (a + b \sin [c + d x])^m dx$$

Optimal (type 5, 201 leaves, 3 steps):

$$\begin{aligned} & -\frac{(e \cos [c + d x])^{-1-m} (a + b \sin [c + d x])^{1+m}}{(a - b) d e (1 + m)} + \left(2^{\frac{1}{2}-\frac{m}{2}} a (e \cos [c + d x])^{-1-m} \right. \\ & \left. \operatorname{Hypergeometric2F1}\left[\frac{1}{2}(-1 - m), \frac{1 + m}{2}, \frac{1 - m}{2}, \frac{(a - b)(1 - \sin [c + d x])}{2(a + b \sin [c + d x])}\right] \right. \\ & \left. \left(\frac{(a + b)(1 + \sin [c + d x])}{a + b \sin [c + d x]} \right)^{\frac{1+m}{2}} (a + b \sin [c + d x])^{1+m} \right) / \left((a^2 - b^2) d e (1 + m) \right) \end{aligned}$$

Result (type 8, 29 leaves):

$$\int (e \cos [c + d x])^{-2-m} (a + b \sin [c + d x])^m dx$$

Problem 650: Unable to integrate problem.

$$\int (e \cos [c + d x])^{-1-m} (a + b \sin [c + d x])^m dx$$

Optimal (type 5, 132 leaves, 1 step):

$$\frac{1}{(a+b)d(1+m)}$$

$$e (e \cos [c+dx])^{-2-m} \text{Hypergeometric2F1}\left[1+m, \frac{2+m}{2}, 2+m, \frac{2(a+b \sin [c+dx])}{(a+b)(1+\sin [c+dx])}\right]$$

$$(1-\sin [c+dx]) \left(-\frac{(a-b)(1-\sin [c+dx])}{(a+b)(1+\sin [c+dx])}\right)^{m/2} (a+b \sin [c+dx])^{1+m}$$

Result (type 8, 29 leaves):

$$\int (e \cos [c+dx])^{-1-m} (a+b \sin [c+dx])^m dx$$

Problem 651: Unable to integrate problem.

$$\int (e \cos [c+dx])^{-m} (a+b \sin [c+dx])^m dx$$

Optimal (type 6, 152 leaves, 2 steps):

$$\frac{1}{bd(1+m)} e \text{AppellF1}\left[1+m, \frac{1+m}{2}, \frac{1+m}{2}, 2+m, \frac{a+b \sin [c+dx]}{a-b}, \frac{a+b \sin [c+dx]}{a+b}\right]$$

$$(e \cos [c+dx])^{-1-m} (a+b \sin [c+dx])^{1+m} \left(1 - \frac{a+b \sin [c+dx]}{a-b}\right)^{\frac{1+m}{2}} \left(1 - \frac{a+b \sin [c+dx]}{a+b}\right)^{\frac{1+m}{2}}$$

Result (type 8, 27 leaves):

$$\int (e \cos [c+dx])^{-m} (a+b \sin [c+dx])^m dx$$

Problem 652: Unable to integrate problem.

$$\int (e \cos [c+dx])^{1-m} (a+b \sin [c+dx])^m dx$$

Optimal (type 6, 142 leaves, 2 steps):

$$\frac{1}{bd(1+m)} e \text{AppellF1}\left[1+m, \frac{m}{2}, \frac{m}{2}, 2+m, \frac{a+b \sin [c+dx]}{a-b}, \frac{a+b \sin [c+dx]}{a+b}\right]$$

$$(e \cos [c+dx])^{-m} (a+b \sin [c+dx])^{1+m} \left(1 - \frac{a+b \sin [c+dx]}{a-b}\right)^{m/2} \left(1 - \frac{a+b \sin [c+dx]}{a+b}\right)^{m/2}$$

Result (type 8, 29 leaves):

$$\int (e \cos [c+dx])^{1-m} (a+b \sin [c+dx])^m dx$$

Problem 653: Unable to integrate problem.

$$\int (e \cos [c+dx])^{2-m} (a+b \sin [c+dx])^m dx$$

Optimal (type 6, 152 leaves, 2 steps):

$$\frac{1}{b d (1+m)} e \operatorname{AppellF1}\left[1+m, \frac{1}{2}(-1+m), \frac{1}{2}(-1+m), 2+m, \frac{a+b \sin [c+d x]}{a-b}, \frac{a+b \sin [c+d x]}{a+b}\right]$$

$$(e \cos [c+d x])^{1-m} (a+b \sin [c+d x])^{1+m}$$

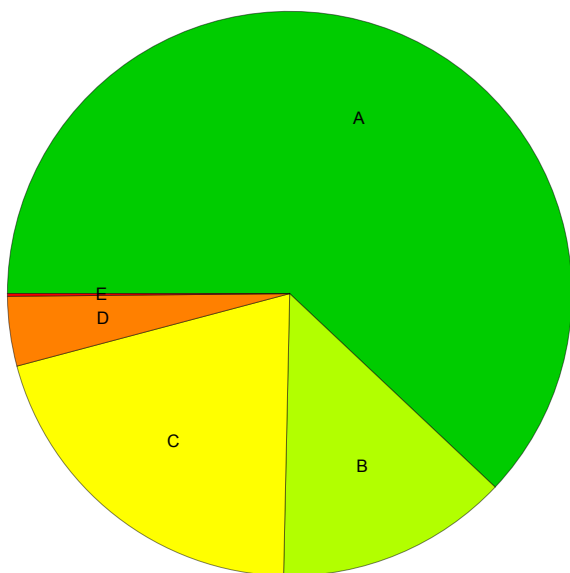
$$\left(1-\frac{a+b \sin [c+d x]}{a-b}\right)^{\frac{1}{2}(-1+m)} \left(1-\frac{a+b \sin [c+d x]}{a+b}\right)^{\frac{1}{2}(-1+m)}$$

Result (type 8, 29 leaves):

$$\int (e \cos [c+d x])^{2-m} (a+b \sin [c+d x])^m dx$$

Summary of Integration Test Results

653 integration problems



A - 405 optimal antiderivatives

B - 87 more than twice size of optimal antiderivatives

C - 134 unnecessarily complex antiderivatives

D - 26 unable to integrate problems

E - 1 integration timeouts